

Geotechnical Engineering.

1. —→ Introduction
—→ Index properties of soil.

2. —→ permeability
—→ Effective stress & seepage through soil.

3. —→ Stress Distribution in soil.
—→ compaction

4. —→ Consolidation

5. —→ Shear strength of soil.

father of Soil Mechanics —→ 'Karl Terzaghi'

Geotechnical Engineering

UNIT-1

Introduction: Soil formation:-

→ Soils are formed by weathering of rock and decomposition of organic matter.

→ Based on source of soils are classified into two types.

→ Organic soil

→ Inorganic soil.

* → Organic soils are called as Cumulative soils
Ex: peat, humus, muck.

Geological Cycle:-

→ Weathering of rocks - Transportation - Deposition - Uplift.

Types of Weathering:-

→ 1. physical weathering & chemical weathering.

* Physical weathering:-

→ It is due to physical effects like, temperature, abrasion, wedging action of ice, penetration of plant roots.

→ physical weathering results in no change in chemical composition of particles.

↳ It produces coarse grained and non cohesive soil.

Ex: Gravel, sand,

Chemical weathering:-

↳ It is due to chemical action oxidation, hydration, carbonation, solution, leaching, hydrolysis etc.

↳ Original rock minerals are transformed into clay minerals.

↳ It results in fine grained and cohesive soils.

Ex: clays.

Sedimentary Soils:-

↳ These soil particles created at one location, transported and finally deposited in another location.

Source of Transportation Deposition	Type of soil:
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↳ River	→ Alluvial soil Ex: silt, sand
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↳ Lake	→ Lacustrine soil Ex: Varved clay
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↳ Sea	→ Marine soil
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↳ Wind	→ Aeolian soil Ex: Sand dune, loess
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↳ Gravitation	→ Colluvial soil, Ex: Talus.
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↳ Glacier	→ Glacier deposited soil Ex: Drift, till, outwash.
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Residual soil:

↳ These are soils which remain on the parent rock without getting transported.

Ex: Black. Cotton soil, laterite soils.

Soil structure:

↳ Soil structure is a geometrical arrangement of soil particle in a soil mass.

↳ The behaviour of soil depends on the soil structure.

Important type of soil structure:

↳ The soil structure are classified into based on.

Depending upon the particle size and mode of formation

↳ The following soil structure are:

1) → Single grained

2) → Honey-comb

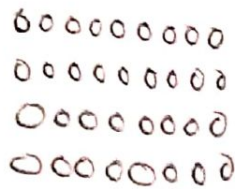
3) → flocculated.

4) → Dispersed

5) → Composite structure

Single grained structure:

→ It is present in soil like gravel and sand.



Loosest packing

→ If particles are assumed as spheres, the loosest and densest packing.



Densest packing:

→ The void ratio for the loosest state is 0.91

→ The void ratio for the densest packing 0.85

Honey - Comb structure:



→ present in fine sand or silts to be deposited

such that particles when settle develop a particle to particle contact. It is said to be below 0.0075 mm & 0.075 mm.

Ex: sands, silts.

Flocculated structure:

- ↳ the flocculated soil structure occurs in clays.
- ↳ formed when there is net attractive force b/w particles.
- ↳ edge to face orientation.
- ↳ has high shear strength, low compressibility, high permeability.

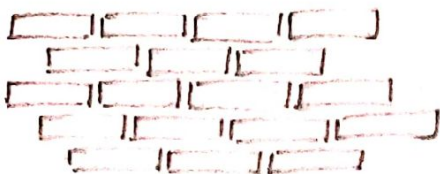
Structure:



Dispersed structure:

- ↳ the dispersed structure occurs in remoulded clays.
- ↳ face to face orientation.
- ↳ formed when there is net repulsive force b/w particles.
- ↳ has low shear strength, high compressibility, and low permeability.

Structure:



Composite structure:

→ When the soil contains different type of particles, a composite structure is formed.

Remoulding:

→ Remoulding causes a loss of strength in cohesive soils.

Thixotropy:

→ The phenomenon of regaining of lost strength with the passage of time, with no change in water content is known as thixotropy.

clay mineralogy:

- ↳ It deals with the structure of clay minerals.
- ↳ The most significant properties of clay depends upon the type of minerals.

Basic structural units of clay minerals:-

↳ Tetrahedral unit.

↳ Octahedral unit.

Tetrahedral unit:-

- ↳ It consists of one silicon ion surrounded by 4 oxides forming tetrahedral unit.

Octahedral unit:-

- ↳ It consists of 6 hydroxides forming a configuration of octahedra and having aluminium atom at the centre.

Isomorphism:-

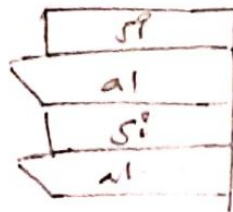
- ↳ It is possible when the one atom in a base unit may be replaced by another atom. It is known as isomorphism substitution.

Types of clay minerals:

- 1 → Kaolinite
- 2 → Illite
- 3 → Montmorillonite

Kaolinite:

- ↳ In this type of clay the basic unit is formed by atomic bond of silica sheet and aluminium sheet.
- ↳ Stable mineral
- ↳ Causes no swelling and no shrinkage present
- ↳ predominantly in china clay.



Illite clay:

- ↳ In this Illite clay the basic structure of this clay consists of silica sheet, aluminium sheet, and silica sheet and potassium ions are present

In blow.
↳ Illite clay causes due to medium swelling and shrinkage



Montmorillonite:

↳ In this type of clay is similar to Illite clay where water molecules and cations are present in between the layer of clay.

↳ Montmorillonite clay causes due to high shrinkage & high swelling.

↳ High percentage is present in Bentonite followed by black cotton soils.

Halloisite:

↳ In this Hallosite clay properties due to kaolinite.

Specific surface area:

↳ In this total surface area of soil particles per unit weight or per unit volume of soil.

↳ Montmorillonite clay minerals has largest specific surface area (about $800 \text{ m}^2/\text{gm}$).

Range of particle size

1. Gravel: \rightarrow 80mm to 4.75mm
2. Sand \rightarrow 4.75mm to 0.075mm
3. Silt \rightarrow 0.075mm to 0.002mm
4. clay \rightarrow < 0.002 mm.

\rightarrow The majority of Naturally occurring collapsing soil
 \rightarrow Aeolian

properties of soils:-

1) Soil phase system:-

→ It consist 3 types:

1) Un-saturated

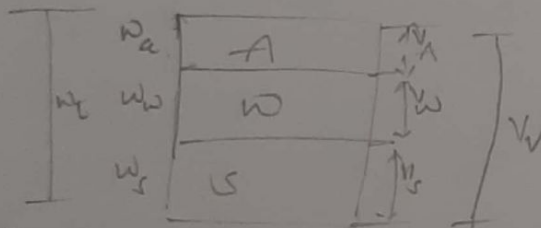
2) fully saturated

3) fully Dried:

1) Un-saturated:-

→ Un-saturated soil consist of solid + water + air

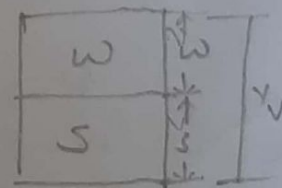
→ It is also termed as three phase system.



2) fully saturated:-

→ It consist of solid + water

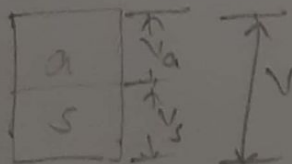
→ It is known as two-phase system.



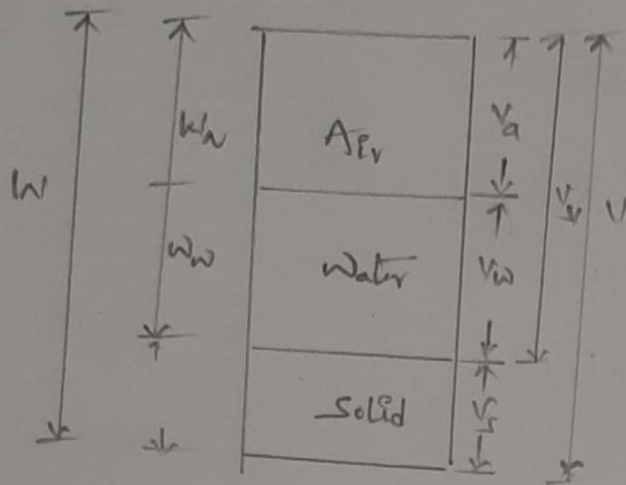
3) fully Dried:-

→ It consist of solid + air.

→ It is known as 2-phase system.

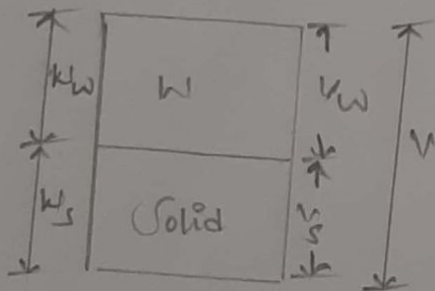


Phase Diagram:



3-phase diagram. \rightarrow partially saturated

2-phase system:



Saturated

Dry

- $V \rightarrow$ Total Volume
- $W \rightarrow$ Total Weight of soil
- $V_a \rightarrow$ Volume of air
- $V_s \rightarrow$ Volume of solid
- $V_w \rightarrow$ Volume of water
- $W_a \rightarrow$ Weight of air
- $W_w \rightarrow$ Weight of water
- $W_s \rightarrow$ Weight of solid

Void ratio: (e) :-

→ Void ratio is defined as the ratio b/w Volume of Voids to Volume of Solids

$$e = \frac{\text{Vol. of Voids}}{\text{Vol. of Solids}} = \frac{V_v}{V_s}$$

→ Range: Can have any value greater than zero.

→ Some times e may also be greater than one

porosity: (n) :-

→ porosity is defined as the ratio b/w Volume of Voids to Total Volume soil.

$$n = \frac{\text{Vol. of Voids}}{\text{Total Vol. of Soil}} \times 100 = \frac{V_v}{V} \times 100$$

→ It is also called as percentage Voids.

→ Range: $0 < n < 100\%$

→ Relation between n & e is $n = \frac{e}{1+e} \therefore e = \frac{n}{1-n}$

Water content: (w) :-

→ It is also called as moisture content and it is defined as ratio of weight of water to weight of Solids Engineer Soil

$$w = \frac{W_w}{W_s} \times 100$$

Degree of Saturation (S_r) :

↳ It is defined as Volume of water to Volume of Voids

$$S_r = \frac{\text{Vol. of water}}{\text{Vol. of Voids}} \times 100$$

$$= \frac{V_w}{V_v} \times 100$$

↳ Range: $0 \leq S_r \leq 100\%$

↳ for fully saturated $S_r = 1$ or 100% .

↳ for dry soil, $S_r = 0$.

Air Content (a_c) :

↳ It is defined as Volume of air to Volume of Voids

$$a_c = \frac{\text{Vol. of air}}{\text{Vol. of Voids}} \times 100$$

↳ for saturated soil, $a_c = 0$

↳ Dry soil, $a_c = 100\%$

↳ Range: $0 \leq a_c \leq 100\%$

↳ $a_c + S_r = 100\%$

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percentage air Voids: n_a :

→ It is defined as the ratio b/w Volume of air to Total Volume

$$n_a = \frac{\text{Vol. of Air}}{\text{Total Volume}} \times 100$$

→ for a saturated soil $n_a = 0$

→ for dry soil $n_a = n$

→ Range: $0 \leq n_a \leq n$

→ $n_a = n \cdot n_c$

Water Content (or) moisture Content (w):

→ It is defined as the ratio b/w weight of water to weight of solids

$$w = \frac{\text{wt. of water}}{\text{wt. of solids}} \times 100 = \frac{W_w}{W_s} \times 100$$

→ Range: Can have any value greater than 0

Sometimes it can be $> 100\%$.

Bulk unit weight of soil (γ):

→ It is the ratio b/w total weight to total volume of soil.

$$\gamma = \frac{\text{Total wt}}{\text{Total vol. of soil}} = \frac{W_w + W_s + W_a}{V}$$

Dry unit weight of soil (γ_d):

→ It is the ratio b/w weight of solids to total volume of soil.

$$\gamma_d = \frac{\text{wt of solids}}{\text{Total vol. of soil}} = \frac{W_s}{V}$$

Unit weight of solids (γ_s):

→ It is the ratio b/w weight of solids to volume solids

$$\gamma_s = \frac{\text{Wt. of solids}}{\text{Volume of solids}} = \frac{W_s}{V_s}$$

→ While γ_s is constant for given soil the γ_d is not constant.

Saturated unit weight: (γ_{sat}) :-

→ It is bulk unit weight when soil is fully saturated.

→ It is also equal to total weight of soil when fully saturated per unit of total volume

Submerged unit weight (γ_{sub} or γ') :-

→ It is the submerged weight of soil solids per unit of total volume of soil

$$\gamma' = \gamma_{sat} - \gamma_w$$

→ It is based on Archimedes principle.

Specific Gravity of Soil Solids or Soil (G_s or G_r) :-

→ It is the ratio of weight of given volume of soil solids at a given temperature to the weight of an equal volume of distilled water at that temperature

→ As per IS code standard temperature for measuring G_s is 27°C

$$G_s = \frac{\gamma_s}{\gamma_w}$$

For a given soil, G_s remains constant. Generally G_s for

→ Inorganic solids lies between 2.60-2.85

→ Organic solids → 1.2 to 1.4.

Apparent or Mass or Bulk Specific Gravity of Soil :-

$$G_m = \frac{\gamma}{\gamma_w} \text{ partially saturated soil}$$

$$G_m = \frac{\gamma_d}{\gamma_w} \text{ for dry soil}$$

$$G_m = \frac{\gamma_{sat}}{\gamma_w} \text{ for saturated soil}$$

G_m is not constant

$$G_m < G_s$$

Some important relationships :-

$$\rightarrow 1, e = \frac{w \cdot G_s}{S_r}$$

$$\rightarrow 2, \gamma = \frac{\gamma_w (G_s + e S_r)}{1 + e}$$

$$\rightarrow 3, \gamma_{sat} = \frac{\gamma_w (G_s + e)}{1 + e}$$

$$\rightarrow 4, \gamma_d = \frac{\gamma_w \cdot G_s}{1 + e}$$

$$\rightarrow 5, \gamma_d = \frac{\gamma}{1 + w}$$

$$\rightarrow 6, \gamma_d = \frac{(1 - n_a) \cdot \gamma_w \cdot G_s}{1 + w \cdot G_s}$$

$$\rightarrow 7, \gamma = \gamma_d + S_r (\gamma_{sat} - \gamma_d)$$

$\rightarrow \gamma_{sub} = \gamma_{sat} - \gamma_w \rightarrow$ Archimedes' principle:

Apparatus:Uses:

- Casagrande's → Determination of Consistency limit
- Hydrometer → Determination of Grain size distribution
- plate load test → Determination of Safe load bearing capacity
- oedometer → Consolidation characteristics.

Equipment:property of Soil:

- pycnometer → Specific Gravity
- permeameter → Co-efficient of permeability
- Vane Shear → Cohesion.
- Pipette → Grain size.

problems:

→ The specific gravity of a soil sample is 2.7 & its void ratio is 0.945. If it is fully saturated what will be the moisture content of soil?

Sol: $G = 2.7$ $e = 0.945$

fully saturated soil $S_r = 1$

using the relation. $e = \frac{wG}{S_r}$

$$0.945 = \frac{w \cdot 2.7}{1}$$

$$\frac{0.945}{2.7} = w$$

$$w = 0.35 \text{ or } 35\%$$

A sample of dry soil weighs 120m and its volume 80ml. if the specific gravity is 2.80 the void ratio of the sample is

$$G = 2.80$$

Dry wt, $W_s = 120 \text{ gm}$

Volume, $V = 80 \text{ ml}$ or 80 cc

$$\gamma_d = \frac{120}{80} = 1.5 \text{ gm/cc}$$

$$\gamma_d = \frac{wG}{1+e}$$

$$1.5 = \frac{1 \times 2.86}{1+e} = e = 0.86.$$

→ 1 cubic meter of wet soil weight 20 kN, and its Dry Weight is 18 kN. Specific Gravity of Solids is 2.67. Determine the water content, porosity, void ratio, and Degree of Saturation.

Sol: Given data.

$$\text{Volume} = 1 \text{ m}^3$$

$$\text{Weight of water} = 20 \text{ kN}$$

$$\text{Dry weight} = 18 \text{ kN}$$

$$\text{Sp. Gravity} = 2.67$$

$$1. \text{ Water content } w = \frac{W_w}{W_s} \times 100$$

$$2. \text{ porosity } n = \frac{V_v}{V} \times 100$$

$$3. \text{ Void ratio} = e = \frac{V_v}{V_s}$$

$$4. \text{ Degree of Saturation } S = \frac{V_w}{V_v} \times 100$$

$$W_w = W - W_s$$

$$W_w = \text{Wet wt of Solids} - \text{Dry wt of Solids}$$

$$= 20 - 18$$

$$W_w = 2 \text{ kN}$$

$$V_v = V - V_s$$

$$V_s = \frac{W_s}{G_s \cdot \gamma_w}$$

$$\gamma_w = \frac{W_w}{V_w}$$

$$V_w = \frac{W_w}{\gamma_w} = \frac{2}{9.8} = 0.204 \text{ m}^3$$

$$V_s = \frac{W_s}{G_s \cdot \gamma_w} = \frac{18}{2.67 \times 9.8}$$

$$W_s = 18 \text{ kN}$$

$$V_s = \frac{1P}{2.67 \times 9.81} = \frac{kA}{kA/m^3}$$

$$V_s = 0.68 m^3$$

$$V_v = V - V_s$$

$$V_v = 1 - 0.68$$

$$V_v = 0.32 m^3$$

$$2. \text{ porosity } (\eta) = \frac{V_v}{V_s} \times 100$$

$$\eta = \frac{0.32}{0.68} \times 100 \quad \frac{m^3}{m^3}$$

$$\eta = 46.72$$

$$3. \text{ Void ratio } (e) = \frac{V_v}{V_s} \quad \frac{m^3}{m^3}$$

$$= \frac{0.32}{0.68}$$

$$e = 0.4672$$

$$4. \text{ Degree of saturation } (S) = \frac{V_w}{V_v} \times 100$$

$$V_w = \frac{W}{\gamma_w} \quad \frac{kA}{kA/m^3}$$

$$= \frac{2}{9.81} m^3$$

$$S = \frac{0.203}{0.32} \times 100 \quad \frac{m^3}{m^3}$$

$$S = 63.4$$

→ The weight of moisture soil is 25 kN and its volume is 0.01 m^3 . after drying the soil in an oven weight reduced to 16 kN. Take $G = 2.7$ calculate water content Dry Density Void ratio porosity and degree of saturation.

Sol: Given that

$$\text{Volume (V)} = 0.01 \text{ m}^3$$

$$\text{wt of moist soil} = 25 \text{ kN}$$

$$G = 2.7$$

$$\text{Dry wt} = 16 \text{ kN}$$

$$1. \text{ water content (w)} = \frac{W_w}{W_s} \times 100$$

$$2. \text{ Dry Density}$$

$$3. \text{ Void ratio (e)} = \frac{V_v}{V_s}$$

$$4. \text{ porosity (n)} = \frac{V_v}{V_s} \times 100$$

$$5. \text{ Degree of saturation } S = \frac{V_w}{V_v} \times 100$$

$$W_w = \text{wt. of Solids} - \text{Dry wt. of soil}$$

$$= 25 - 16$$

$$W_w = 9 \text{ kN}$$

$$1. \text{ water Density (wt)} = \frac{W_w}{W_s} \times 100$$

$$= \frac{9}{16} \times 100$$

$$= 56.25\%$$

$$2. \text{ Void ratio } (e) = \frac{V_v}{V_s}$$

$$V_v = V - V_s$$

$$V_s = \frac{W_s}{\gamma_s \cdot \gamma_w}$$

$$= \frac{16}{9.81 \times 2.71}$$

$$V_s = 0.601 \text{ m}^3$$

$$V_v = V - V_s$$

$$= 1 - 0.601$$

$$V_v = 0.399 \text{ m}^3$$

$$2. \text{ porosity } (n) = \frac{V_v}{V_s} \times 100$$

$$= \frac{0.399}{0.601} \times 100$$

$$n = 66.8$$

$$3. \text{ Void ratio } (e) = \frac{V_v}{V_s}$$

$$= \frac{0.399}{0.601}$$

$$e = 0.663$$

$$4. \text{ Degree of Saturation } S = \frac{V_w}{V_v} \times 100$$

$$V_w = \frac{W_w}{\gamma_w} = \frac{9}{9.81}$$

$$V_w = 0.9177$$

$$= \frac{0.917}{0.399} \times 100$$

$$S = 229.8$$

→ The mass moisture soil is 20kg and its volume 0.01m³.
 find the mass reduce to 16.5kg after drying determine
 the dry density. Density of moist soil. water content
 void ratio porosity and degree of saturation and take
 specific gravity 2.67

Sol: Given

$$Wt \text{ moist soil} = 20 \text{ kg}$$

$$\text{Volume (V)} = 0.01 \text{ m}^3$$

$$\text{Dry. wt} = 16.5 \text{ kg}$$

$$G_s = 2.67$$

$$G_w = 1$$

i, Dry Density:

$$\# \frac{\text{wt Dry Density}}{\text{Volume}}$$

$$\# \text{ moist soil Density} = \frac{\text{Soil Density}}{\text{Volume}}$$

$$\text{ii, water content (w)} = \frac{W_w}{W_s} \times 100$$

$$\text{iii, Void ratio (e)} = \frac{V_v}{V_s}$$

$$\text{iv, porosity (n)} = \frac{V_v}{V_s} \times 100$$

$$\text{v, Degree of saturation (S)} = \frac{V_w}{V_v} \times 100$$

$$W_w = Wt. \text{ of Solids} - \text{Dry wt. of soil}$$

$$= 20 - 16.5$$

$$W_w = 3.5 \text{ kg}$$

$$= \frac{8.5}{16.5} \times 100$$

$$w = 21.21\%$$

$$\frac{\text{wt of Dry density}}{\text{Volume}}$$

$$= \frac{16.5}{0.011} = 1500 \text{ kg/m}^3$$

$$\frac{\text{wt of Dry density of soil}}{\text{Volume}}$$

$$= \frac{20}{0.011} = 1818.18 \text{ kg/m}^3$$

$$1. \text{ porosity } (n) = \frac{V_v}{V_s} \times 100$$

$$V_v = V - V_s$$

$$V_s = \frac{W_s}{\gamma_s \cdot 20}$$

$$= \frac{16.5}{2.67 \times 1}$$

$$V_s = 6.17 \text{ kg/m}^3$$

$$= 0.11 - 6.17$$

$$V_v = -6.06 \text{ kg}$$

$$\text{Void ratio } (e) = \frac{V_v}{V_s}$$

$$= \frac{-6.06}{6.17}$$

$$e = -0.98 \text{ m}^3$$

$$\text{Degree of saturation } (S) = \frac{V_w}{V_v} \times 100$$

$$V_w = \frac{W_w}{\gamma_w} = \frac{3.5}{1}$$

$$V_w = 3.5 \text{ kg}$$

$$= \frac{3.5}{0.06} \times 100$$

$$S = 57.75 \%$$

→ If the volume of voids is equal to the volume of solids in a soil mass then the values of porosity & void ratio.

$$\text{Given: } V_v = V_s$$

$$\text{porosity } n = \frac{V_v}{V} = \frac{V_v}{V_s + V_v} = \frac{1}{2} = 0.5$$

$$\text{Void ratio } e = \frac{V_v}{V_s} = \frac{1}{1} = 1$$

$$= 0.5 \text{ to } 1.0$$

→ The porosity of a soil sample is 30% and sp. Gravity of its particle is 2.75. Then the saturated unit wt is equal to.

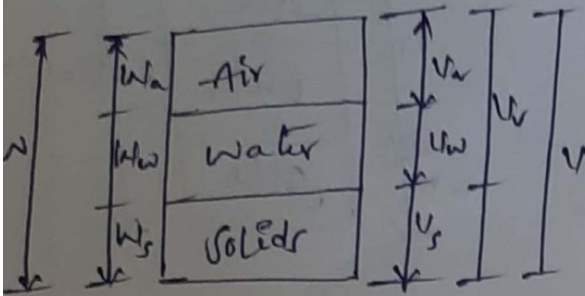
$$\gamma_{\text{sat}} = \frac{(G+e)\gamma_w}{1+e} = e = \frac{n}{1-n} = \frac{0.3}{1-0.3}$$

$$= \frac{(2.75+e)\gamma_w}{1+e}$$

$$e = 0.43$$

$$= \frac{(2.75+0.43) \times 1}{1+0.43} = 222 \text{ g/cm}^3$$

Relations:



$$V = V_a + V_w + V_s \quad \therefore V_v = V_a + V_w$$

$$W = W_a + W_w + W_s$$

$$\boxed{W = W_w + W_s}$$

Relation b/w W , W_s , w :

$$W = W_a + W_w + W_s$$

$$W = W_w + W_s$$

$$W = W_s \left(1 + \frac{W_w}{W_s} \right)$$

$$W = W_s (1 + w)$$

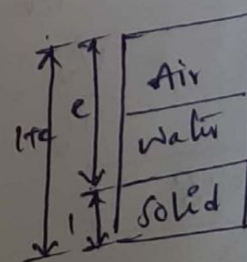
$$\boxed{W_s = \frac{W}{1 + w}}$$

Relation b/w e & n :

$$\text{porosity: } (n) = \frac{V_v}{V}$$

$$n = \frac{V_v}{V_v + V_s} = \frac{\frac{V_v}{V_s}}{\frac{V_v + V_s}{V_s}} = \frac{e}{1 + e}$$

$$\boxed{n = \frac{e}{1 + e}}$$



$$V_v = e$$

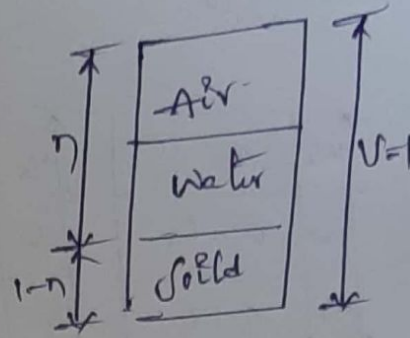
$$V_s = 1$$

$$V = 1 + e$$

Void ratio: $e: \frac{V_v}{V_s}$

$$e = \frac{V_v}{V - V_s}$$
$$= \frac{V_v/V}{V - V_s/V} = \frac{n}{1-n}$$

$$\boxed{e = \frac{n}{1-n}}$$



Relation b/w n, n_a, a_c :-

$$n_a = \frac{V_a}{V}$$

$$n_a = \frac{V_v}{V} \cdot \frac{V_a}{V_v}$$

$$\boxed{n_a = n \cdot a_c}$$

Relation b/w a_c & s :-

$$a_c + s = \frac{V_a}{V_v} + \frac{V_w}{V_v}$$

$$= \frac{V_a + V_w}{V_v}$$

$$= \frac{V_v}{V_v} = 1$$

$$\boxed{a_c + s = 1}$$

→ Air content

$$\therefore a_c = \frac{V_a}{V_v}$$

$$\therefore s = \frac{V_w}{V_v}$$

→ Degree of saturation.

Relation b/w n_a , e & s :

$$n_a = \frac{V_a}{V} = \frac{V_v - V_w}{V_v + V_s} = \frac{V_v \left(1 - \frac{V_w}{V_v}\right)}{V_s \left(1 + \frac{V_v}{V_s}\right)}$$

$$\boxed{n_a = \frac{e(1-s)}{(1+e)}}$$

Relation b/w γ , γ_d & w :

$$\gamma = \frac{W}{V} = \frac{W_s + W_w}{V}$$

$$\gamma = \frac{W_s \left(1 + \frac{W_w}{W_s}\right)}{V}$$

$$\gamma = \frac{W_s (1+w)}{V}$$

$$\gamma = \gamma_d (1+w)$$

$$\boxed{\gamma_d = \frac{\gamma}{1+w}}$$

$$\frac{W_w}{W_s} = w \rightarrow \text{water content}$$

$$\frac{W_s}{V} = \gamma_d \rightarrow \text{dry unit weight of soil}$$

Relation b/w e, s, w & G :

$$\text{Void ratio: } (e) = \frac{V_v}{V_s}$$

$$= \frac{V_v}{V_w} \times \frac{V_w}{V_s}$$

$$\gamma_s = \frac{W_s}{V_s} \Rightarrow ; \gamma_w = \frac{W_w}{V_w}$$

$$V_s = \frac{W_s}{\gamma_s}$$

$$V_w = \frac{W_w}{\gamma_w}$$

$$\therefore \frac{V_w}{V_v} = s$$

Degree of
saturation

$$e = \frac{1}{s} \cdot \left(\frac{(W_w / \gamma_w)}{(W_s / \gamma_s)} \right)$$

$$= \frac{1}{s} \cdot \left(\frac{W_w}{\gamma_w} \times \frac{\gamma_s}{W_s} \right)$$

$$= \frac{1}{s} \cdot \left(\frac{W_w}{W_s} \cdot \frac{\gamma_s}{\gamma_w} \right)$$

$$\therefore G = \frac{\gamma_s}{\gamma_w}$$

$$\therefore \gamma_s = G \cdot \gamma_w$$

$$e = \frac{1}{s} \times w \times G$$

$$\boxed{e \cdot s = w \cdot G}$$

Relation b/w γ_t , G , c , w & γ_w :

$$\gamma_t = \frac{W}{V} = \frac{W_s + W_w}{V_s + V_v}$$

$$= \frac{W_s \left(1 + \frac{W_w}{W_s}\right)}{V_s \left(1 + \frac{V_v}{V_s}\right)}$$

$$\gamma_t = \gamma_s \frac{(1+w)}{1+c}$$

$$\gamma_t = \frac{G \cdot \gamma_w \left(1 + \frac{S \cdot c}{G}\right)}{1+c}$$

$$\gamma_t = \frac{G \cdot \gamma_w (G + S \cdot c)}{1+c}$$

$$\gamma_t = \frac{\gamma_w (G + S \cdot c)}{1+c}$$

If soil is fully saturated $\gamma_t = \gamma_{sat}$ & $S = 1$

$$\gamma_{sat} = \frac{\gamma_w (G + c)}{1+c}$$

If soil is fully dry $\gamma_t = \gamma_{dry}$ & $S = 0$

$$\gamma_{dry} = \frac{\gamma_w \cdot G}{1+c}$$

If soil is fully submerged $\gamma_t = \gamma' = \gamma_{sat} - \gamma_w$

$$\gamma' = \frac{\gamma_w (G + c)}{1+c} - \gamma_w$$

$$\therefore G = \frac{\gamma_s}{\gamma_w}$$

$$\therefore \gamma_w \cdot G = \gamma_s$$

$$S \cdot c = W \cdot G$$

$$W = \frac{S \cdot c}{G}$$

$$= \gamma_w \left(\frac{q+c}{1+c} - 1 \right)$$

$$= \gamma_w \left(\frac{q+c-1-c}{1+c} \right)$$

$$\boxed{\gamma' = \frac{\gamma_w (q-1)}{1+c}}$$

Relation b/w γ_d , q , ω & n_a :-

$$V = V_a + V_w + V_s$$

$$1 = \frac{V_a}{V} + \frac{V_w}{V} + \frac{V_s}{V}$$

$$1 = n_a + \frac{V_w}{V} + \frac{V_s}{V}$$

$$1 - n_a = \frac{V_w}{V} + \frac{V_s}{V}$$

$$\gamma_s = \frac{W_s}{V_s} \Rightarrow V_s = \frac{W_s}{\gamma_s} = \frac{W_s}{q \cdot \gamma_w}$$

$$q = \frac{\gamma_s}{\gamma_w} \\ \therefore q \gamma_w = \gamma_s$$

$$\gamma_w = \frac{W_w}{V_w} \Rightarrow V_w = \frac{W_w}{\gamma_w} = \boxed{\frac{W_w}{q \cdot \gamma_s}}$$

$$V_w = \frac{W_w}{\gamma_w}$$

$$= \frac{W_s}{\gamma_w} \cdot \frac{W_w}{W_s}$$

$$\therefore \frac{W_w}{W_s} = \omega$$

$$\boxed{V_w = \frac{W_s}{\gamma_w} \cdot \omega}$$

$$1 - \eta_a = \frac{W_s}{V} + \frac{W_w}{V}$$

$$= \frac{1}{V} \left[\frac{W_s}{\eta_s} \right] + \frac{1}{V} \left[\frac{W_s}{\eta_w} \right] \cdot \omega$$

$$q = \frac{\eta_s}{\eta_w}$$

$$\eta_s = q \cdot \eta_w$$

$$= \frac{1}{V} \left[\frac{W_s}{q \cdot \eta_w} \right] + \frac{W_s}{V} \left[\frac{\omega}{\eta_w} \right]$$

$$= \frac{W_s}{V} \cdot \frac{1}{q \cdot \eta_w} + \frac{W_s}{V} \cdot \frac{\omega}{\eta_w}$$

$$= \frac{\eta_d}{q \cdot \eta_w} + \frac{\eta_d \cdot \omega}{\eta_w}$$

$$1 - \eta_a = \frac{\eta_d}{\eta_w} \left(\frac{1}{q} + \omega \right)$$

$$1 - \eta_a = \frac{\eta_d}{\eta_w} \left(\frac{1 + q \cdot \omega}{q} \right)$$

$$\frac{\eta_d}{\eta_w} = \frac{q(1 - \eta_a)}{1 + \omega \cdot q}$$

$$\boxed{\eta_d = \frac{\eta_w \cdot q \cdot (1 - \eta_a)}{1 + \omega \cdot q}}$$

If $\eta_a = 0$ soil becomes fully saturated at given ω

$$\eta_d = \frac{q \cdot \eta_w}{1 + \omega \cdot q}$$

Relation b/w γ , ω , q , η , ρ & $\eta\omega$:

$$\eta\tau = \left(\frac{q + \rho e}{1 + \rho e} \right) \eta\omega$$

$$\frac{\eta\tau}{\eta\omega} = \frac{q + \rho e}{1 + \rho e}$$

$$\text{But } \rho e = \omega \cdot q$$

$$e = \frac{\omega \cdot q}{\gamma}$$

$$\frac{\eta\tau}{\eta\omega} = \frac{q + \omega \cdot q}{1 + \frac{\omega \cdot q}{\gamma}}$$

$$\frac{\eta\tau}{\eta\omega} = \frac{q(1 + \omega)}{\left(1 + \frac{\omega \cdot q}{\gamma}\right)}$$

$$\left(1 + \frac{\omega \cdot q}{\gamma}\right) = q(1 + \omega) \cdot \frac{\eta\omega}{\eta\tau}$$

$$\frac{\eta\omega}{\eta\tau} (1 + \omega) = \frac{1}{q} \left(1 + \frac{\omega \cdot q}{\gamma}\right) = \frac{1}{q} + \frac{\omega}{\gamma}$$

$$\frac{1}{q} + \frac{\omega}{\gamma} = \frac{\eta\omega}{\eta\tau} (1 + \omega)$$

$$\frac{\omega}{\gamma} = \frac{\eta\omega}{\eta\tau} (1 + \omega) - \frac{1}{q}$$

$$\boxed{\gamma = \frac{\omega}{\left(\frac{\eta\omega}{\eta\tau} (1 + \omega) - \frac{1}{q}\right)}}$$

A oven dry soil sample has mass sp. gravity of 1.5 g/cc
 If bulk density of soil in its natural state is 2 g/cc
 then w_c of soil in natural soil be.

$$G = 1.5 \text{ g/cc}$$

$$P_d = 2 \text{ g/cc}$$

$$G_m = \frac{\gamma_d}{\gamma_w}$$

$$\gamma_d = G_m \cdot \gamma_w$$

$$\gamma_d = 1.5 \cdot (\gamma_w = 1)$$

$$\gamma_d = 1.5 \text{ g/cc}$$

$$\gamma = 2 \text{ g/cc}$$

$$\gamma_d = \frac{\gamma}{1+w} = \frac{2}{1+w} = 1.5.$$

→ A soil sample has a porosity of 40%. The sp. g. of solids is 2.70. Calculate a, void ratio, b, dry density, c, unit weight if the soil is 50% saturated d, unit weight if the soil is completely saturated.

Given $n = 40\% = 0.4$, $G = 2.70$

$$a) e = \frac{n}{1-n} = \frac{0.4}{1-0.4} = 0.667$$

$$b) \gamma_d = \frac{G \cdot \gamma_w}{1+e} = \frac{2.7 \times 9.81}{1+0.667} = 15.89 \text{ kN/m}^3 \quad \therefore \gamma_w = 9.81 \text{ kN/m}^3$$

$$c) e = \frac{w \cdot G}{\gamma} \quad \therefore w = \frac{e \cdot \gamma}{G} = \frac{0.667 \times 0.5}{2.70} = 0.124$$

$$\gamma_d = 15.89 \text{ kN/m}^3$$

$$\gamma = \gamma_d (1+w) = 15.89 (1+0.124) = 17.85 \text{ kN/m}^3$$

$$\gamma = \frac{\gamma_w (G + e \cdot w)}{1+e} = \frac{9.81 (2.70 + 0.667 \times 0.5)}{1+0.667} = 17.85 \text{ kN/m}^3$$

d) The soil is fully saturated $e = w_{\text{sat}} \cdot G$

$$w_{\text{sat}} = \frac{e}{G} = \frac{0.667}{2.70} = 0.247$$

$$\gamma_{\text{sat}} = \gamma_d (1+w_{\text{sat}}) = 15.89 \times 1.247 = 19.87 \text{ kN/m}^3$$

$$\begin{aligned} \gamma_{\text{sat}} &= G \gamma_w (1-n) + \gamma_w n = 2.7 \times 9.81 (1-0.4) + 9.81 \times 0.4 \\ &= 15.89 + 3.92 = 19.81 \text{ kN/m}^3 \end{aligned}$$

The in-situ % voids of a sand deposit is 34% for determining the density index, dried sand from this stratum was first filled loosely in a 1000 cm³ mould and was then vibrated to give a maximum density. The loose dry mass in the mould was 1610 g & the dry dense mass at maximum compaction was found to be 1960 g. Determine the density index if the sp-gravity of the sand particle is 2.67.

$$\text{Given } n = 34\% = 0.34$$

$$e = \frac{n}{1-n} = \frac{0.34}{1-0.34} = \frac{0.34}{0.66} = 0.515$$

$$\gamma_d = \frac{G \gamma_w}{1+e} = \frac{2.67 \times 9.81}{1+0.515} = 17.289$$

$$(\gamma_d)_{\max} = \frac{1960}{1000} \times 9.81 = 19.42 \text{ kN/m}^3 \quad (\gamma_d)_{\min} = \frac{1610}{1000} \times 9.81 = 15.79 \text{ kN/m}^3$$

$$e_{\min} = \frac{G \gamma_w}{\gamma_d(\max)} - 1 = \frac{2.67 \times 9.81}{19.42} - 1 = 0.349$$

$$e_{\max} = \frac{G \gamma_w}{\gamma_d(\min)} - 1 = \frac{2.67 \times 9.81}{15.79} - 1 = 0.659$$

$$I_D = \frac{e_{\max} - e}{e_{\max} - e_{\min}} = \frac{0.659 - 0.515}{0.659 - 0.349} = 0.465 = 46.5\%$$

→ The sp. gravity of soil equals 1.64. The sp. gravity of solids is 2.70. Determine the void ratio under the assumption that the soil is perfectly dry. What would be the voids ratio, if the sample is assumed to have a water content of 8%.

When the sample is dry $G_m = \frac{\gamma_d}{\gamma_w} = 1.64$

$$\gamma_d = 1.64 \gamma_w$$

$$\gamma_d = 1.64 \times 9.81 = 16.09 \text{ kN/m}^3$$

$$e = \frac{G_s \gamma_w}{\gamma_d} - 1 = \frac{2.7 \times 9.81}{16.09} - 1 = 0.646$$

The sample has the water content $w = 8\%$. $G_m = \frac{\gamma}{\gamma_w} = 1.64$.

$$\gamma = 1.64 \gamma_w = 1.64 \times 9.81 = 16.09 \text{ kN/m}^3$$

$$\gamma_d = \frac{\gamma}{1+w} = \frac{16.09}{1+0.08} = 14.9 \text{ kN/m}^3$$

$$e = \frac{G_s \gamma_w}{\gamma_d} - 1 = \frac{2.7 \times 9.81}{14.9} - 1 = 0.76$$

↳ Calculate the unit-weights & sp. gravities of solids

a) a soil composed of pure quartz

b) a soil composed of 60% quartz, 25% mica & 15% iron oxide.

Assume that both solid soils are saturated and have void ratio of 0.63 Take the avg G for quartz = 2.66
for mica = 3.0 & iron oxide = 3.8

a) pure quartz: $G = 2.66$

$$\gamma_{sat} = \frac{G + e}{1 + e} \gamma_w = \frac{2.66 + 0.63}{1 + 0.63} \times 9.81 = 19.8 \text{ kN/m}^3$$

b) for the composite soil:

$$G_{avg} = (2.66 \times 0.6) + (3.0 \times 0.25) + (3.8 \times 0.15) = 1.60 + 0.75 + 0.57 = 2.92$$

$$\gamma_{sat} = \frac{2.92 + 0.63}{1 + 0.63} \times 9.81 = 21.36 \text{ kN/m}^3$$

1.22
One cubic meter of wet soil weighs 19.80 kN
If the sp. gravity of soil particles is 2.70 & water content
is 11%. find the void ratio, dry density & degree of
saturation.

$$\text{Bulk unit weight, } = 19.80 \text{ kN/m}^3$$

$$\text{Water content } w = 11\% = 0.11$$

$$\text{Dry unit weight, } \gamma_d = \frac{\gamma}{(1+w)} = \frac{19.80}{(1+0.11)} \text{ kN/m}^3 = 17.84 \text{ kN/m}^3$$

$$\text{Specific gravity of soil particle } G = 2.70$$

$$\gamma_d = \frac{G \cdot \gamma_w}{1+e}$$

$$\text{Unit wt of water } \gamma_w = 9.81 \text{ kN/m}^3$$

$$17.84 = \frac{2.70 \times 9.81}{(1+e)}$$

$$(1+e) = \frac{2.70 \times 9.81}{17.84} = 1.485$$

$$1+e = 1.485$$

$$e = 1.485 - 1$$

$$e = 0.485$$

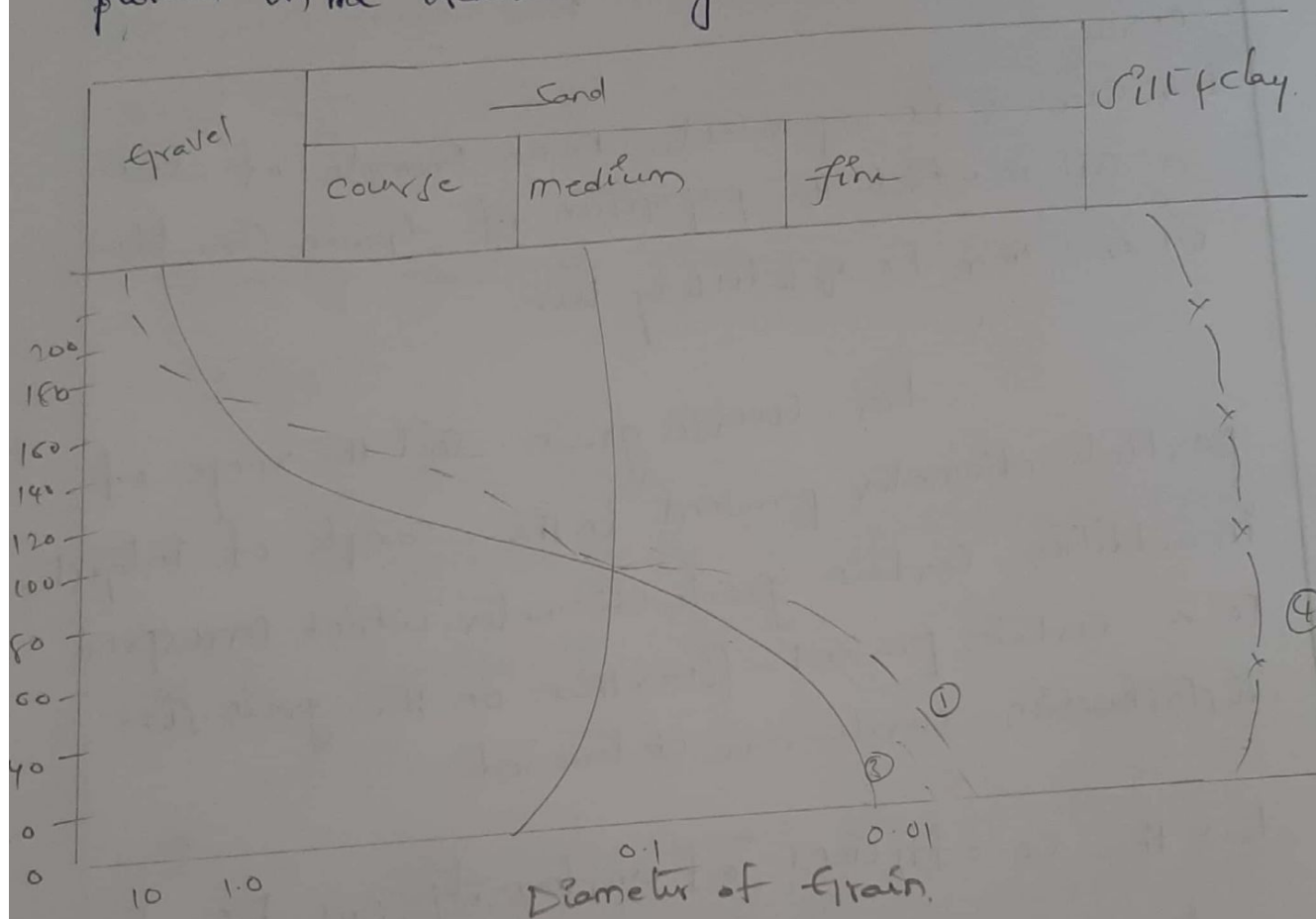
$$\text{Degree of saturation } S = \frac{wG}{e}$$

$$S = \frac{0.11 \times 2.70}{0.485} = 0.6124$$

$$\text{Degree of saturation} = 61.24\%$$

Grain size distribution curves:-

→ The result of grain size analysis are usually represented in the form of a graph the ordinate are cumulative weight as a percentage of total weight is plotted on the ordinate using an arithmetic scale.



→ A well graded soil as a good representation of grain size over a wide range and its gradation curve is smooth.

Curve 1:

→ Curve 1 is represented a well graded soil, with particle varying from gravel to fines aggregate.

Curve 2

→ Curve 2 is represented a poorly graded sand of uniform gradation.

Curve 3:

→ Curve 3 is represented to an example of such a soil in which the proportion of grain size below 0.1 and 1mm is relatively low.

For coarse grain soil the range of particle diameter present in the sample of interest in addition certain grade diameter which correspond to a certain present finer than on the grain size distribution curve are determined.

→ The co-efficient of uniformity (C_u) = $\frac{D_{60}}{D_{10}}$ is a shape of parameter is defined as

$$C_u = \frac{D_{60}}{D_{10}}$$

D_{60} → grain size diameter in mm.

Another shape parameter the co-efficient of curvature 'C_c' defined

$$C_c = \frac{D_{30}^2}{D_{10} \times D_{60}}$$

Where:

d_{30} → Grain diameter in mm corresponding to 30% finer

C_u → Co-efficient of Curvature.

for well graded soil C_u lies b/w '143' and C_u must be greater than 4 for gravel & greater than 6 for sand.

Generally Grain size diameter is classified by

2 types:

1) Sieve Analysis.

2) Hydrometer Analysis (Mekel Mechanical Analysis).

Sieve Analysis:

1) Sieves are made by weaving two sets of wires at right angle to each other. Sieve sizes are given in terms of mesh openings per unit length.

According to Indian standard sieve number is mesh width in mm (or micron) $\mu = 0.001 \text{ mm}$.

Analysis is done by sieving of dry sample of down weight through series of sieves sample placed one below other in decreasing order of size.

→ whole set is horizontally shaken for 10 min till weight of soil retained in each sieve term constant.

→ By determining weight of soil sample retained on each sieve the following are made.

→ Percentage retained on sieve

$$= \frac{\text{Weight of soil retained on the sieve}}{\text{Weight of total soil.}}$$

Cumulative percentage retained on any sieve:

$$= \text{Sum of percentages retained on all} \\ \text{— Coarser sieve}$$

percentage finer than only sieve opening =

$$100 - \text{Cumulative percentage retained}$$

Hydrometer Analysis:

In Hydrometer Analysis the soil sample about 40 to 60 gm of dried soil, whose particle size is less than 0.075 mm (or) 75 micron is accurately weighed and mixed with distilled water to form a paste.

The contents is transferred to a cup of mechanical mixer using a set of distilled water and then stirred well for 15 min & then transfer the jar to make 1000 cc suspension.

It is then vigorously shaken and kept vertically on a solid base.

Stop watch is started simultaneously. The hydrometer is inserted slowly and readings are taken at 0.5 m (1/2 m), 1 m, 2 m, 3 m, 4 m, 5 m, 6 m, etc.

A stable correction is applied on these readings. The diameter of particle is calculated according to Stokes law.

to Stokes law.

$$\text{Terminal Velocity, } V_s = \frac{1}{18} \frac{d^2 (\gamma_s - \gamma_w)}{\mu} \quad \text{or} \quad V_s = \frac{g}{18} \frac{[\gamma_s - 1] d^2}{\nu}$$

d = diameter of particle, γ_s → unit weight of particle
 μ = dynamic viscosity of water, ν → kinematic viscosity of water = μ/ρ

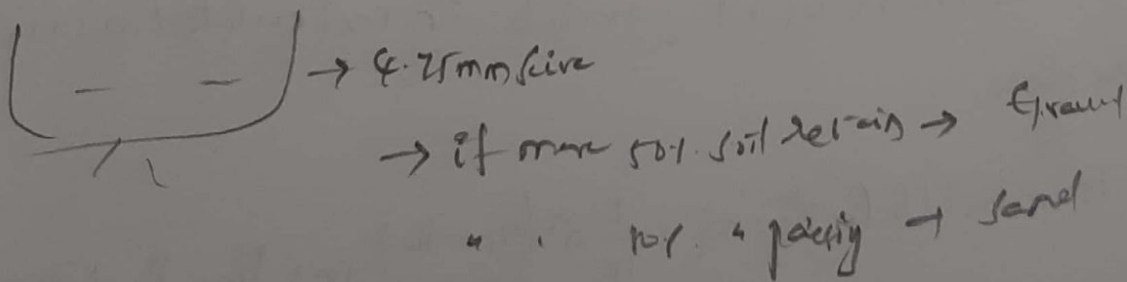
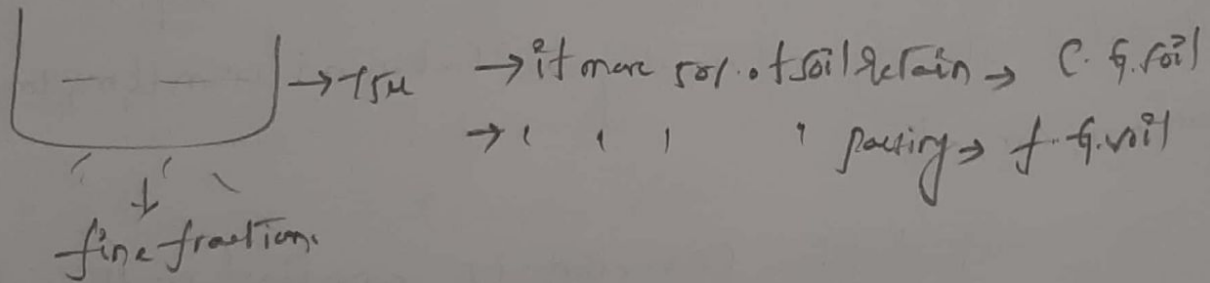
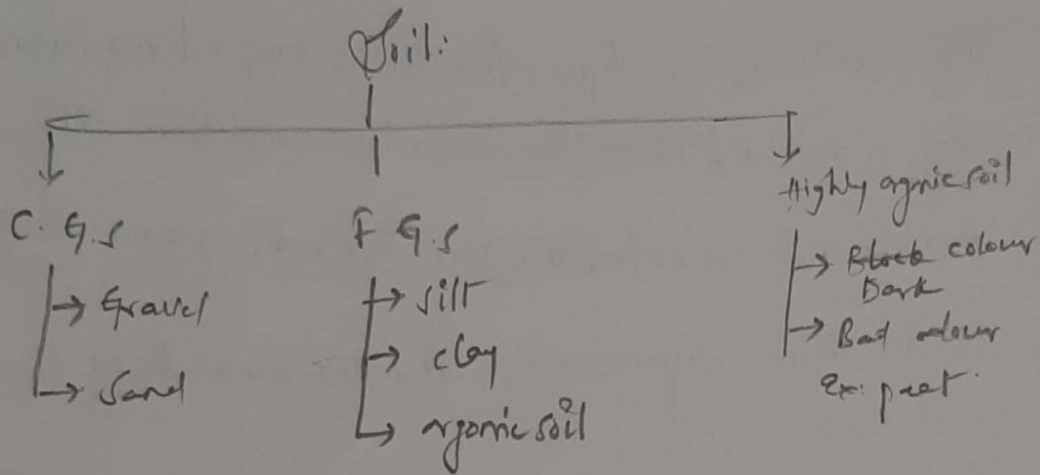
γ_s → specific gravity of solids

Approximate version of Stokes law

$$V_s = 9000d^2$$

V = Velocity in mm/sec

d = Diameter of particle in mm.



Consistency limit
(or)

Limits of consistency (Atterberg's limit):

- ↳ Mostly used for fine grained soil.
- ↳ Atterberg divided the entire range from liquid to solid state into four states.

- 1) Liquid state
- 2) plastic state
- 3) Semi solid state
- 4) Solid state.

Atterberg limit are the water content at which soil mass passes from one state to another state.

Liquid Limit: (w_L):

→ It is the minimum water content at which the soil is still in the liquid state.

→ But has a small shearing strength against flowing.

→ Casagrande's apparatus is used to determine liquid limit. The shear strength of the soil at liquid limit is 2.7 kN/m².

Plastic Limit: (w_p):

→ It is the minimum water content at which the soil can be rolled into a thread of 3mm in diameter without crumbling.

→ It is determined by plastic limit test or thread test.

Shrinkage Limit: (w_s):

→ It is the moisture content at which further loss of moisture content does not cause a decrease in the volume of soil.

→ Shrinkage limit is lowest water content at which a soil can be still completely saturated.

Liquidity Index (I_L):-

$$I_L = \frac{W - W_p}{I_p}$$

↳ The Liquidity Index is also known as water plasticity ratio.

Consistency Index, or Relative consistency: -

$$I_c = \frac{L_L - W}{I_p}$$

It is useful in the study of the field behaviour of saturated fine grained soil.

Range:- I_c can be greater than or less than 1.

If $I_c = 1$, soil is at its plastic limit.

$I_c = 0$, soil is at liquid limit

$I_c > 1$ soil is in semi solid state and is stiff

* Important Indices: ÷

a) plasticity Index (I_p): ÷

$$I_p = (\text{Liquid Limit} - \text{plastic Limit})$$

$$I_p = (w_L - w_p)$$

↳ It is relatively more for plastic clays.

I_p (Y) plasticity.

0 → Non plastic

< 7 → Low plastic

7-17 → Medium plastic

> 17 → highly plastic

* Shrinkage Index (I_s): -

$$I_s = (\text{plastic limit} - \text{shrinkage limit})$$

$$I_s = (w_p - w_s)$$

* Toughness Index (I_T): ÷

$$I_T = I_p / I_f = \text{plasticity Index} / \text{flow Index}.$$

permeability:-

→ It is the property of the soil, which allows passage of fluid through it.

permeable soil:-

→ when a soil has continuous voids

→ A soil is said to be highly permeable when

$$k > 10^{-1} \text{ cm/sec}$$

Ex: Gravel, sand

→ Soil said to be impermeable when

$$k < 10^{-7} \text{ cm/sec.}$$

Ex: stiff clay.

Seepage:-

→ Seepage is the flow of water under gravitational force in a permeable medium.

Laminar flow:-

→ the flow is termed as laminar flow when all the particles of water move in parallel path without corresponding the other particle.

Turbulent flow:-

→ In this type of flow all the particles of water move in more zig-zag.

Soil Water: -

↳ The water which is present in the void space of soil mass is known as Soil water.

↳ The soil water may be in two types:

* → Held water.

* → Gravitational water.

Held water: ÷

↳ The water held in the void spaces of soil mass due to some forces of attraction is called as held water.

↳ It is further classified into 2 types.

* → Adsorbed water.

* → Structural water.

Adsorbed water: ÷

↳ It is a thin layer of water that surrounds the surface of clay particle due to certain physical force of attraction.

Structural water: ÷

↳ It is defined as the water which is combined chemically to the crystalline structure of the clay particle.

The structural water is impossible to separate even at the temperature of 110° Celsius.

Gravitational water: :-

↳ The water which moves freely through the pore space of soil mass under the influence of gravitational force is termed as gravitational water.

↳ They are two types:

* → Free water.

* → Capillary water.

Free water: :-

↳ The water which translocate under the influence of gravitational force is called as free water.

↳ It is divided into two types:

* → Surface water.

* → Ground water.

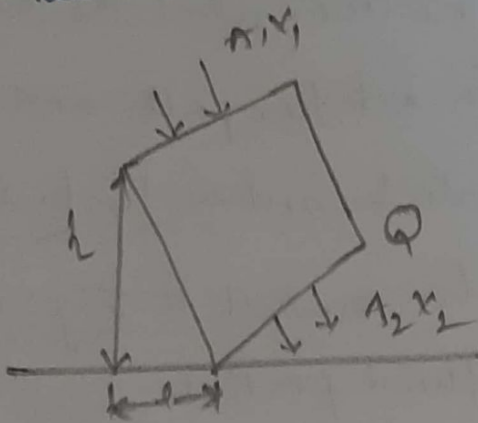
Capillary water: -

The water which is held by the force of capillary action is called capillary water.

Capillary rise: :-

Arise in a liquid above the level of zero pressure due to net upward force produced by attraction of the water molecules to a solid surface.

Darcy's law:



→ In 1856 Darcy demonstrated experimentally that for laminar flow in a homogeneous soil the velocity of flow is given by

$$v = ki \Rightarrow \frac{Q}{A} = ki \Rightarrow Q = kiA$$

$$Q = kiA \quad (\because Q = Av)$$

$$\therefore \frac{Q}{A} = v \quad \therefore \frac{Q}{v} = A$$

Where:

k = Co-efficient of permeability

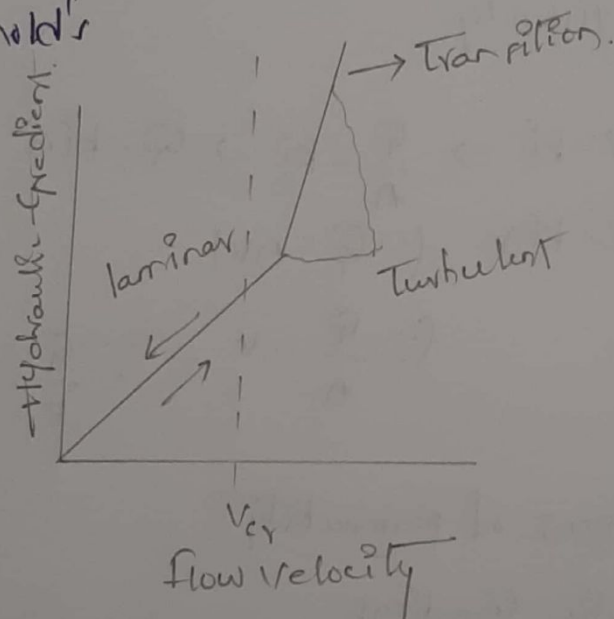
i = Hydraulic Gradient.

→ Darcy's law is valid as long as the flow is laminar. It is applied to the soil fraction finer than the grain

Flow of water through soil: ÷

→ Flow of fluid is described as laminar if a fluid particle flows in a definite path and does not lose the path of other particles and as turbulent where random velocity fluctuations result in zig-zag and cross-cross paths of fluid particles.

→ The fundamental law to determine whether the flow is laminar or turbulent was formulated by Reynolds.



→ The flow velocity is proportional to the hydraulic gradient as long as the flow is laminar.

→ As a velocity increases a critical state is reached at which eddies begin to form near the wall of the tube and the relationship between flow velocity and hydraulic gradient becomes uncertain.

↳ A further increasing velocity again leads to definite relationship this time is represented by continuous curved line

↳ The velocity at which laminar flow changes to turbulent flow a change occurs and it is called as lower critical velocity (V_{cr}).

↳ As a below lower critical velocity V_{cr} the flow is always laminar.

↳ Reynold's found that lower critical velocity is inversely proportional to the diameter of the tube or pipe

↳ Reynold's develop a general formula which is applicable for any fluid it is independent of system unit.

$$\frac{V_{cr} \cdot d \cdot \gamma_w}{\eta} = 2000$$

d = tube diameter

γ_w = unit weight of water

η = viscosity of fluid

g = gravitational force

V_{cr} = critical velocity

Importance of permeability:-

↳ The following important of permeability are

- * → Seepage through earth dam and canals
- * → A uplift pressure under hydraulic structure and safety again it's piping.

Factors affecting permeability: ÷

- 1, Effect of grain size:
- 2, Effect of shape
- 3, Effect of void ratio.

* Effect of grain size ÷

↳ The co-efficient of permeability of soil is proportional to the square of representative particle size

$$k = C D_{10}^2$$

where C - constant varies from 0.4 to 1.2 with Avg Value 1.

* Effect of shape ÷

↳ for same void ratio the soil with angular particles are less permeable than those with rounded particles. k is inversely proportional to specific surface area

C, Void ratio ÷

↳ To predict for a given soil the value of k at a void ratio other than the one at which it is determined

Taylor (1948) recommends the following relationship

$$k_1 : k_2 = \frac{C e_1^3}{1 + e_1} : \frac{C e_2^3}{1 + e_2}$$

C_1, C_2 are shape-factor which depend on manner of packing of grains & the shape characteristic of the pores. for sands C' changes only slightly with void ratio i.e. $C_1 \approx C_2$

$$k_1 : k_2 = \frac{e_1^3}{1+e_1} : \frac{e_2^3}{1+e_2}$$

Another relationship (some time used) is

$$k_1 : k_2 = C_1 e_1^2 : C_2 e_2^2$$

Assuming C' is constant for sands.

Unit weight of water: (γ_w):

$$K = C \Delta_{10}^2 \frac{\gamma_w}{4} \frac{e^3}{1+e}$$

$C \rightarrow$ Shape factor it depends on shape of particle

$K \rightarrow$ Co-eff. of permeability.

Temperature:

$K \propto \text{Temperature}$

Specific Surface Area:

$$SSA \propto \frac{1}{\text{size}} \quad (\text{size} \downarrow \text{SSA} \uparrow)$$

$$K \propto \frac{1}{SSA}$$

Effect of permeant & (it is viscosity of temperature) &

→ the factor (η) depends on the kind & physical state of pore fluid.

$$K \propto \frac{\eta}{\eta_1}$$

$$K_1 : K_2 = \frac{\eta_1}{\eta_2} : \frac{\eta_2}{\eta_1}$$

Since both viscosity & unit-weight of permeant vary with temperature K will be affected by changes in η . greater viscosity lower the permeability it is common practice to note the temp of water during permeability determination and specify the computed permeability volume - corresponding to 27°C

$$K_{27} = \frac{\eta_T}{\eta_{27}} K_T$$

$K_{27} \rightarrow$ Volume of K at 27°C

$K_T \rightarrow$ " " " " at $T^\circ\text{C}$

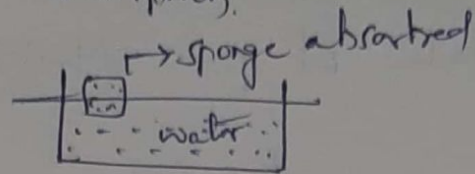
$\eta_{27} \rightarrow$ Viscosity of permeant at 27°C

$\eta_T \rightarrow$ Viscosity of " " at $T^\circ\text{C}$

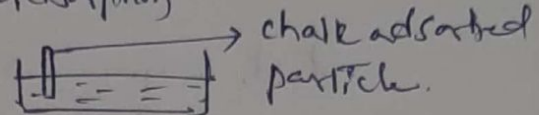
Adsorbed water:

$$K < \frac{1}{\text{adsorption}}$$

Absorption



Adsorption



permeability: k'

$$k = C D_o^2 \frac{\eta_w}{\mu} \frac{e^3}{1+e}$$

$k \Rightarrow$ Co-efficient of permeability

$C \rightarrow$ shape factor. it depends on shape of particle

$D_o \rightarrow$ effective grain size

$\mu \rightarrow$ Viscosity of water.

$e \rightarrow$ void ratio

$\eta \rightarrow$ unit weight of percolating water.

↳ The coefficient of permeability (Soil is $4 \times 10^{-5} \text{ cm/sec}$)
 If the viscosity of fluid is reduced to ($\frac{1}{2}$) other
 other things are remaining constant, then find the coefficient of permeability.

permeability & viscosity

$k \propto \mu$

Given:

$$k_1 = 4 \times 10^{-5} \text{ cm/sec}$$

$$\mu_1 = \mu_1$$

$$k_2 = ?$$

$$\mu_2 = \frac{\mu_1}{2}$$

$$k \propto \frac{1}{\mu}$$

$$\frac{k_1}{k_2} = \frac{\mu_2}{\mu_1} \Rightarrow \frac{k_2}{k_1} = \frac{\mu_1}{\mu_2}$$

$$\frac{k_2}{k_1} = \frac{\mu_1}{\frac{\mu_1}{2}}$$

$$\frac{k_2}{k_1} = 2$$

$$k_2 = 2k_1$$

$$k_2 = 2 \times 4 \times 10^{-5}$$

$$k_2 = 8 \times 10^{-5} \text{ cm/sec}$$

Measurement of permeability :-

→ The co-efficient of permeability can be determined by three ways.

1. laboratory 2. field test, 3. Empirical approach.

In the laboratory, it is possible to use either the constant head or the variable head test.

Constant head test :-

→ It is based on the measurement of the quantity of water that flows under a given hydraulic gradient through a soil sample of known length & cross-sectional area in given time.

→ Constant head permeameters are specially suited to the testing of pervious coarse-grained soil.

→ Measurable discharge is needed for the accurate determination of permeability by this method.

→ The soil sample is contained in a Perspex cylinder. At the cylinder, a number of manometer connection points are provided to enable pairs of pressure head readings to be taken. Water is allowable to flow through the sample from a reservoir designed to keep the water level constant by overflow.

→ The quantity of water flowing out of the soil or discharge Q during a given time t is collected in a vessel and weighed.

→ The presence of entrapped air in the soil can affect the results seriously.

→ To eliminate this possibility, firstly de-aired water is supplied to the reservoir and then vacuum is applied to the soil sample before commencing the test.

→ The test is started by closing the valve C and keeping valves A and B open with valve A being used to control the rate by constant level in the manometer tubes then the discharge is measured.

→ Several such test at varying rates of flow can be performed and the avg value of k determined.

$$Q = k i A$$

$$k = \frac{Q}{\frac{Q}{iA}} = \frac{Q}{A h t} \text{ cm/s.}$$

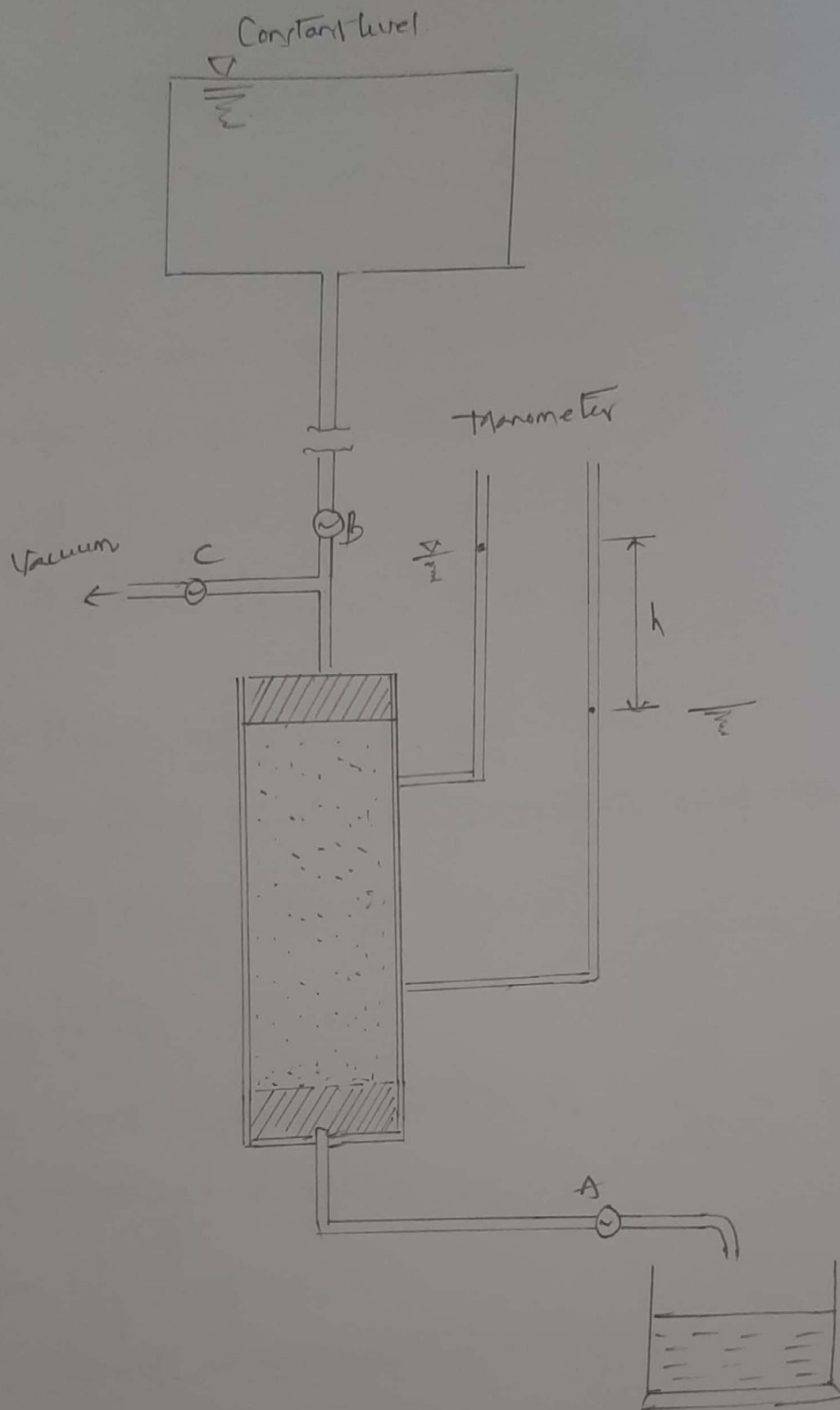
k = Co-efficient of permeability (cm/s)

Q = discharge (cm³) collected in time t (s)

A = cross-sectional area of sample (cm²)

h = difference in manometer level (cm)

L = distance between manometer tapping points (cm).



Constant head permeometer:

permeability in layered soil: ÷

↳ permeability of stratified soil deposits.

A stratified soil deposit consists of soil layers having different permeability. The avg permeability of deposit as a whole parallel to the planes of stratification, and normal to the planes of stratification are presented below.

* → flow through layers are parallel

* → flow of a normal to the plane

Flow through layer are parallel:

* → Considered two layers parallel to each other

Let q_1 → discharge through layer 1

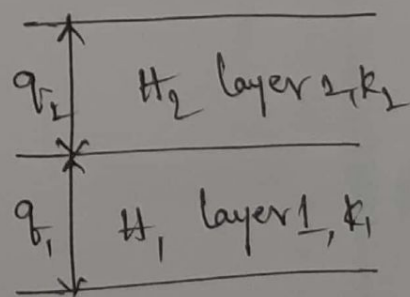
H_1 → height of layer 1

k_1 → Co-eff of permeability of layer 1

q_2 → discharge through layer 2

H_2 → height of layer 2

k_2 → Co-eff of permeability of layer 2.



Total discharge $(Q) = q_1 + q_2$

We know: $Q = A \times V$

$$A \times V = A_1 V_1 + A_2 V_2$$

$$(H_1 + H_2) \times K_i^p = (H_1 \times 1) \times K_1^p + (H_2 \times 1) \times K_2^p$$

$$(H_1 + H_2) \times K_i^p = (H_1 K_1^p + H_2 K_2^p)$$

$$(H_1 + H_2) \times K_i^p = (H_1 K_1^p + H_2 K_2^p)$$

$$K_i = \frac{H_1 K_1 + H_2 K_2}{H_1 + H_2}$$

Flow Normal to the plane of stratification:

→ let us consider a soil deposit consisting of 2 layers of thickness H_1, H_2 in which flow occurs Normal to the plane of stratification as shown fig.

from the fig it is $Q = Q_1 = Q_2$

$$K_v i_v = K_{v1} i_{v1} = K_{v2} i_{v2}$$

$$K_{v1} = \left[\frac{i_v}{i_{v1}} \right] K_v$$

$$K_{v2} = \left[\frac{i_v}{i_{v2}} \right] K_v$$

$$P_U = \left[\frac{k_U}{k_{U_1}} \right] P_U$$

$$P_{U_2} = \left[\frac{k_U}{k_{U_2}} \right] P_U$$

$$\text{Total head (h)} = h_1 + h_2$$

$$P_U H = P_{U_1} H_1 + P_{U_2} H_2$$

$$P_U H = \left[\frac{k_U}{k_{U_1}} \right] H_1 + \left[\frac{k_U}{k_{U_2}} \right] H_2$$

$$H = k_U \left[\frac{H_1}{k_{U_1}} + \frac{H_2}{k_{U_2}} \right]$$

$$k_U = \frac{H}{\left[\frac{H_1}{k_{U_1}} + \frac{H_2}{k_{U_2}} \right]}$$

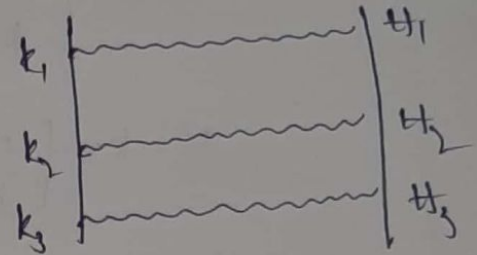
$$k_U = \frac{H_1 + H_2}{\left[\frac{H_1}{k_{U_1}} + \frac{H_2}{k_{U_2}} \right]}$$

A stratum of soil consists of three layers of equal thickness. The permeabilities of top and bottom layer are 1×10^{-4} cm/sec and that of middle layer is 1×10^{-3} cm/sec. Then the value of horizontal co-eff of permeability for the entire soil layer in cm/sec is:

Given data:

The layer of thickness is same

i.e. $H_1 = H_2 = H_3 = H$



permeability of top & bottom layers:

$$k_1 = k_3 = 1 \times 10^{-4} \text{ cm/sec}$$

$$\text{middle layer } k_2 = 1 \times 10^{-3} \text{ cm/sec}$$

$$kH = \frac{k_1 H_1 + k_2 H_2 + k_3 H_3}{H_1 + H_2 + H_3}$$

$$= \frac{H(k_1 + k_2 + k_3)}{3H}$$

$$= \frac{k_1 + k_2 + k_3}{3}$$

$$= \frac{1 \times 10^{-4} + 1 \times 10^{-3} + 1 \times 10^{-4}}{3}$$

$$kH = 4 \times 10^{-4} \text{ cm/sec}$$

$$k_v = \frac{H_1 + H_2 + H_3}{\left[\frac{H_1}{k_{v1}} + \frac{H_2}{k_{v2}} + \frac{H_3}{k_{v3}} \right]}$$

$$\left[\frac{H_1}{k_{v1}} + \frac{H_2}{k_{v2}} + \frac{H_3}{k_{v3}} \right]$$

$$= \frac{200 + 500 + 800}{\left[\frac{200}{5 \times 10^{-4}} + \frac{500}{2 \times 10^{-2}} + \frac{800}{3 \times 10^{-3}} \right]}$$

$$\left[\frac{200}{5 \times 10^{-4}} + \frac{500}{2 \times 10^{-2}} + \frac{800}{3 \times 10^{-3}} \right]$$

$$= \frac{1.90}{\left[\frac{200}{5 \times 10^{-4}} + \frac{500}{2 \times 10^{-2}} + \frac{800}{3 \times 10^{-3}} \right]}$$

$$\left[\frac{200}{5 \times 10^{-4}} + \frac{500}{2 \times 10^{-2}} + \frac{800}{3 \times 10^{-3}} \right]$$

$$k_v = 1.90 \times 10^3 \text{ cm/sec}$$

$$\frac{k_u}{k_v} = \frac{0.11}{1.90 \times 10^3}$$

$$\frac{k_u}{k_v} = 57889$$

The soil sample having permeability of 5×10^{-4} cm/sec for 1st 2m, 2×10^{-2} cm/sec for 2nd 5m, & 3×10^{-3} cm/sec for last 3m and the hydraulic gradient 0.3 in both horizontal & vertical permeability then find.

a, find the ratio of $K_H : K_V$

b, find the discharge & the value of discharge velocity for each layer of horizontal flow.

↳ Given data

$$k_1 = 5 \times 10^{-4} \text{ cm/sec}$$

$$k_2 = 2 \times 10^{-2} \text{ cm/sec}$$

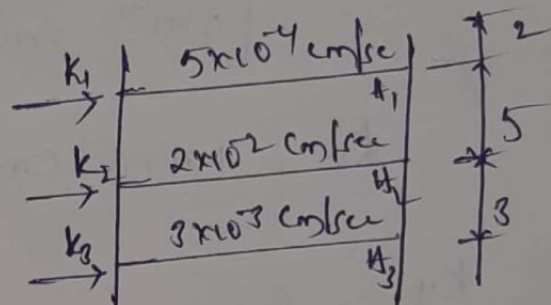
$$k_3 = 3 \times 10^{-3} \text{ cm/sec}$$

$$H_1 = 2 \text{ m}$$

$$H_2 = 5 \text{ m}$$

$$H_3 = 3 \text{ m}$$

$$i = 0.3$$



$$K_H = \frac{k_1 H_1 + k_2 H_2 + k_3 H_3}{H_1 + H_2 + H_3}$$

$$= \frac{5 \times 10^{-4} \times (2 \times 100) + 2 \times 10^{-2} \times (5 \times 100) + 3 \times 10^{-3} \times (3 \times 100)}{200 + 500 + 300}$$

$$K_H = 0.011 \text{ cm/sec} \Rightarrow 1.1 \times 10^{-2} \text{ cm/sec}$$

Specific yield (S_y): \leftarrow

\rightarrow Specific yield of an unconfined aquifer is the ratio of volume of water which will flow under saturated condition due to gravity effect to the total volume of aquifer (W)

$$S_y = \frac{V_{wy}}{V}$$

V_{wy} = Volume of water yielded under gravity effect

V = Total Volume of water.

Specific retention: \leftarrow

\rightarrow The specific retention of an unconfined aquifer is the ratio of volume of water retained against gravity effect to the total volume of aquifer (W)

$$S_r = \frac{V_{wr}}{V}$$

V_{wr} = Volume of water retained under gravity effect.

$$\boxed{S_y + S_r = n} \rightarrow \text{porosity}$$

Kozney - Karmen Equation: \div

$$K = \frac{1}{C} \cdot \frac{1}{S^2} \cdot \frac{70}{21} \cdot \frac{e^3}{1+e}$$

$C \rightarrow$ Shape coefficient ≈ 5 for spherical particle

$S \rightarrow$ Specific surface area = $\frac{\text{Area}}{\text{Volume}}$

Allen Hazen Equation:

$$K = C \cdot D_{10}^2$$

D_{10} = effective size in cm.

K is in cm/s.

$$C = 100 \text{ to } 150$$

Values of permeability: \div

<u>Soil</u>	<u>K (cm/sec)</u>	<u>Degree of permeability</u>
1. Coarse gravel	> 1	High
2. Fine gravel fine sand	$10^{-1} \text{ to } 10^{-2}$	Medium
3. Silt-sand admixture loose silts, rock flour and coarse	$10^{-2} \text{ to } 10^{-4}$	Low
4. Dense silt. clay silt admixture, non homo geneous clay	$10^{-4} \text{ to } 10^{-5}$	Very low
5. Homogeneous clay	$< 10^{-6}$	Impervious.

Consider the flow through an Elementary cylinder of soil having radius r , thickness dr , height h , Hydraulic gradient.

$$i = \frac{dh}{dr}$$

Area of flow, $A = 2\pi r h$

from Darcy's law $q = k i A$

$$= k \frac{dh}{dr} \cdot 2\pi r h$$

$$\frac{dr}{r} = 2 \cdot \frac{\pi}{q} \cdot k \cdot h \cdot dh$$

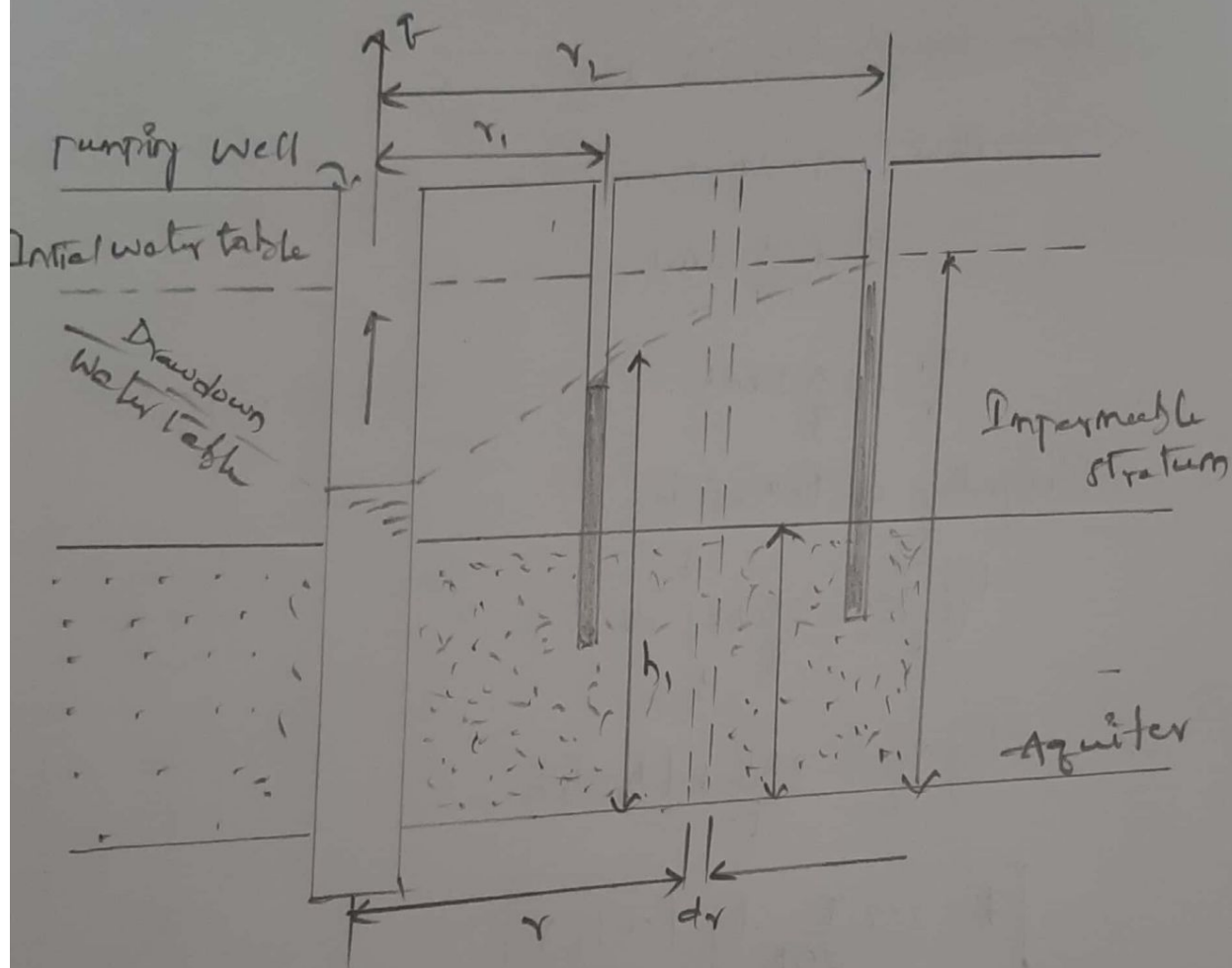
Integrating on both side.

$$\int_{r_1}^{r_2} \frac{dr}{r} = 2 \frac{\pi}{q} \cdot k \int_{h_1}^{h_2} h \cdot dh$$

$$\log_e \frac{r_2}{r_1} = \frac{\pi}{q} \cdot k (h_2^2 - h_1^2)$$

$$k = \frac{2.3 \cdot q}{\pi} \frac{\log_{10} \left(\frac{r_2}{r_1} \right)}{(h_2^2 - h_1^2)}$$

Confined Aquifer :-



- ↳ A confined flow condition occurs when the aquifer is confined both above and below by impermeable strata.
- ↳ The drawdown surface is for all values of r , above the upper surface of the aquifer

→ Consider the flow after steady state is obtained
(In some cases pumping at a steady rate must be continued for many days before a steady flow is reached).

from Darcy's law, $q = k i A$

Here, $A = 2\pi r D$

$$q = k \frac{dh}{dr} \cdot 2\pi r D$$

$$\frac{dr}{r} = \frac{2\pi D k h}{q}$$

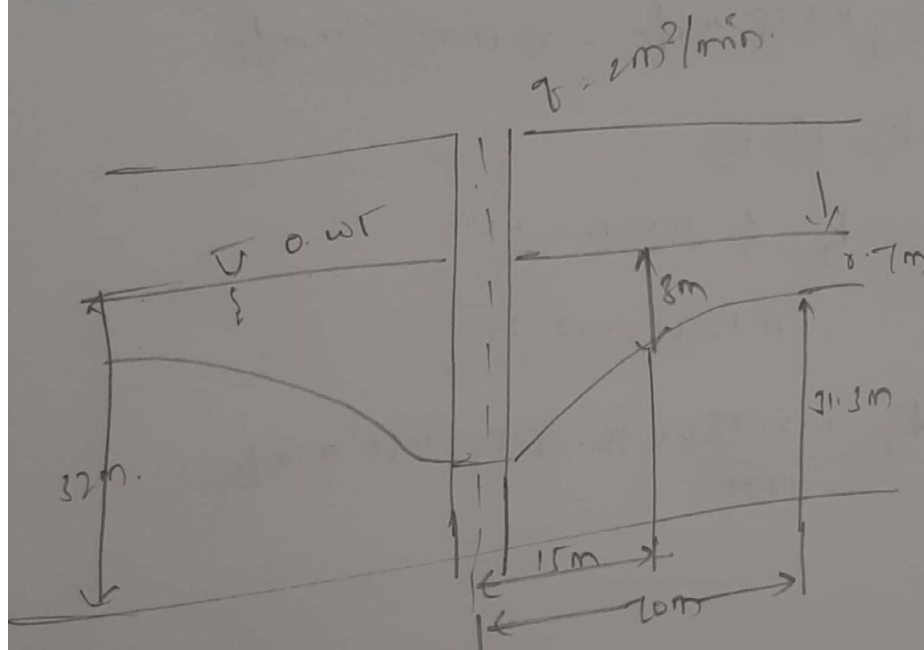
Integrating on both side.

$$\log \int_{r_1}^{r_2} \frac{dr}{r} = \frac{2\pi D k}{q} \int_{h_1}^{h_2} dh$$

$$\log \frac{r_2}{r_1} = \frac{2\pi D}{q} k \cdot (h_2 - h_1)$$

$$k = \frac{2.3}{2\pi D} \frac{q}{(h_2 - h_1)} \cdot \log_{10} \left(\frac{r_2}{r_1} \right)$$

An unconfined aquifer is known to be 32 m thick below the water table. A constant discharge of 2 cubic meter per minute is pumped out of the aquifer through a tubewell. Till the water level in the tube well becomes steady. Two observation wells at distance of 15 m & 20 m from the tube well shows fall of 8 m & 0.7 m resp. from their static water level. find the permeability of the aquifer.



$$K = \frac{q \cdot \log_e (r_2/r_1)}{\pi (z_2^2 - z_1^2)}$$

$$= \frac{2.803 \times 2 \log_{10} (20/15) \times 100}{60 \times \pi (31.3^2 - 29^2)} \text{ cm/sec}$$

$$= 1.18 \times 10^{-7} \text{ mm/sec}$$

A cohesionless soil has a permeability of 0.036 cm per sec. at a void ratio of 0.36. make prediction of the permeability of this soil, when it void ratio of 0.45 according to the two functions of void ratio, that are proposed.

$$k_1 : k_2 = \frac{e_1^3}{(1+e_1)} : \frac{e_2^3}{(1+e_2)}$$

$$0.036 : k_2 = \frac{(0.36)^3}{1.36} : \frac{(0.45)^3}{1.45} = 0.546 : 1$$

$$k_2 = \frac{1}{0.546} \times 0.036 \text{ mm/s} = 6.60 \times 10^{-4} \text{ mm/s}$$

$$k_1 : k_2 = e_1^2 : e_2^2$$

$$0.036 : k_2 = (0.36)^2 : (0.45)^2$$

$$= 0.1296 : 0.2025$$

$$k_2 = \frac{0.2025 \times 0.036}{0.1296} = 5.625 \times 10^{-4} \text{ mm/sec}$$

The Discharge of water collected from a constant head permeameter in a period of 15 min, is 500 ml. The internal diameter of the permeameter is 5 cm & the measured diff head b/w two gauging points 15 cm vertically apart is 40 cm. Calculate the coefficient of permeability.

If the dry weight of the 15 cm long sample is 4.86 N & sp-gravity of the solids is 2.65, Calculate the seepage velocity.

$$Q = 500 \text{ ml. } T = 15 \times 60 = 900 \text{ Sec}$$

$$A = \frac{\pi}{4} \times d^2 = \frac{\pi}{4} \times 5^2 = 6.25\pi \text{ cm}^2. \quad L = 15 \text{ cm, } h = 40 \text{ cm.}$$

$$K = \frac{QL}{At h} = \frac{500 \times 15}{6.25 \times \pi \times 900 \times 40} \text{ cm/s} = 0.106 \text{ mm/s.}$$

$$\text{Superficial Velocity: } U = Q/At = \frac{500}{900 \times 6.25\pi} \text{ cm/sec}$$

$$= 0.0283 \text{ cm/s.}$$

$$= 0.283 \text{ mm/s.}$$

Dry weight of Sample: 4.86 N

$$\text{Volume of Sample: } A \cdot L = 6.25 \times \pi \times 15 = 294.52 \text{ cm}^3$$

$$\text{Dry density} = \gamma_d = \frac{4.86}{294.52} \text{ N/cm}^3 = 16.5 \text{ kN/m}^3$$

$$\gamma_d = \frac{\gamma_{sw}}{(1+e)} \Rightarrow 1+e = \frac{2.65 \times 10}{16.5} = 1.606, \therefore \gamma_w \approx 10 \text{ kN/m}^3$$

$$e = 0.606$$

$$n = \frac{e}{1+e} = 0.3173 = 31.73\% \therefore \text{Seepage Velocity} = V_s = \frac{V}{n} = \frac{0.283}{0.317} = 0.75 \text{ cm/s}$$

Determine the Co-efficient of permeability from the following data.

Length of sand sample: 25 cm

Area of the cross of sample: 30 cm²

Head of water: 40 cm

Discharge: 200 ml in 110 s.

$$L = 25 \text{ cm}$$

$$A = 30 \text{ cm}^2$$

$$h = 40 \text{ cm (assumed constant)}$$

$$Q = 200 \text{ ml} \quad T = 110 \text{ s.}$$

$$q = \frac{Q}{T} = \frac{200}{110} \text{ ml/sec} = \frac{20}{11} = 1.82 \text{ cm}^3/\text{sec}$$

$$i = \frac{h}{L} = \frac{40}{25} = 8/5 = 1.60$$

$$q = k i A$$

$$K = \frac{q}{iA} = \frac{20}{11 \times 16 \times 30} \text{ cm/s.}$$

$$= 0.03788 \text{ cm/sec}$$

$$= 3.788 \times 10^{-1} \text{ mm/s.}$$

In falling head permeability test, head causing flow, was initially 50 cm, & it drops 2 cm in 5 min. How much time require for the head to fall to 25 cm

falling head permeability:

$$K = 2.303 \frac{aL}{At} \cdot \log_{10} (h_1/h_2)$$

Designating $2.303 \frac{aL}{At}$ as a constant, C

$$K = C \cdot \frac{1}{t} \cdot \log_{10} \left(\frac{h_1}{h_2} \right)$$

$$h_1 = 50 \text{ cm}, h_2 = 48, t = 300 \text{ s.}$$

$$\frac{K}{C} = \frac{1}{300} \cdot \log_{10} \left(\frac{50}{48} \right)$$

$$h_1 = 50, h_2 = 25.$$

$$\frac{1}{300} \log_{10} \left(\frac{50}{48} \right) = \left(\frac{1}{t} \right) \cdot \log_{10} \left(\frac{50}{25} \right)$$

$$t = 300 \cdot \frac{\log_{10} 2}{\log_{10} \left(\frac{25}{24} \right)} = 5093.555 = 84.9 \text{ min.}$$

A sample in a variable head permeameter is 8 cm. dia. & 10 cm high. The permeability of the sample is estimated to be 10×10^{-4} cm/sec. If it is desired that the head in the stand pipe should fall from 24 cm to 12 cm in 3 min, determine the size of the stand pipe which should be used.

Variable head permeameter:

Soil sample dia = 8 cm.

height (length) = 10 cm.

permeability = 10×10^{-4} cm/sec

$h_1 = 24$ cm, $h_2 = 12$ cm, $t = 180$ s.

$$k = \frac{2.303 a l}{A t} \cdot \log_{10} \left(\frac{h_1}{h_2} \right)$$

$$10^{-3} = \frac{2.303 \times a \times 10}{\pi \times 16 \times 180} \cdot \log_{10} (24/12)$$

$$a = \frac{\pi \times 16 \times 180}{2.303 \times 10^4 (\log_{10} 2)} \text{ cm}^2 = 1.805 \text{ cm}^2.$$

If the dia. of the stand pipe is d cm.

$$a = \left(\frac{\pi}{4} \right) d^2$$

$$d = \sqrt{\frac{4 \times 1.805}{\pi}} = 1.29 \text{ cm.}$$

Effective Stress:-

2.19

↳ Generally the soils are subjected to 3 types

- * → Total stress (or) Geostatic stress
- * → Neutral (or) pore water pressure
- * → Effective stress (or) Intergranular pressure

Total stress or Geostatic stress (σ):-

↳ Total stress developed by soil due to

- * Self weight of soil (Solid + water)
- * Over burden load [Surcharge (q)]

Self weight of soil:-

$$\sigma = \frac{\text{Self weight}}{\text{Area}} \quad \text{--- (1)}$$

We know. $\gamma = \frac{WT}{\text{Volume}}$

$$WT = \gamma \cdot \text{Volume} \quad \text{--- (2)}$$

② Sub in ①

$$\sigma = \frac{\gamma \cdot \text{Volume}}{\text{Area}}$$

but Volume = Area \times h

$$\sigma = \frac{\gamma \cdot \text{Area} \times h}{\text{Area}}$$

$$\boxed{\sigma = \gamma \cdot h}$$

$\sigma =$ Total stress

$h =$ height (or) depth of soil

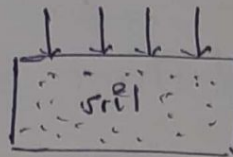
$\gamma =$ unit weight of soil

$l =$ length

$b =$ breadth.

2. Over burden load:

$$\sigma = \gamma h + q$$



2. Neutral or pore water pressure: (u):

→ Neutral stress is developed due to only water present in the voids of the soil.

$$\text{Neutral stress } (u) = \frac{\text{weight of water}}{\text{Area}} \quad \text{--- (1)}$$

$$\text{unit weight of water } (\gamma_w) = \frac{W_w}{\text{Volume}}$$

$$(\gamma_w) = \frac{\text{weight of water}}{\text{Volume}}$$

$$\text{weight of water } (W_w) = \text{Volume} \times \gamma_w \quad \text{--- (2)}$$

Then (2) sub (1)

$$u = \frac{\gamma_w \cdot \text{Volume}}{\text{Area}}$$

$$U = \frac{\gamma_w \cdot x \cdot A \cdot \gamma_w \cdot h}{\text{Area}}$$

$$\boxed{U = \gamma_w \cdot h}$$

$\gamma_w \rightarrow$ unit weight of water

$U \rightarrow$ neutral or pore water pressure

$h \rightarrow$ pressure head.

Effective stress or Intergranular pressure (σ'): \leftarrow

\hookrightarrow Effective stress developed due to particle to particle through their point of contact. which tends to decrease void ratio. \downarrow Increase in strength \uparrow

Increase in density \uparrow
decrease permeability \downarrow

$$\sigma' = \sigma - U$$

$\sigma' =$ effective stress

$\sigma =$ total stress

$U =$ neutral stress.

$$\sigma' = (\gamma - \gamma_w)h$$

$$\sigma = \gamma h$$

$$U = \gamma_w h$$

$$\sigma' = \gamma h - \gamma_w h$$

$$\boxed{\sigma' = (\gamma - \gamma_w)h}$$

→ it is equal to the total vertical reaction force transmitted at the point of contact of soil grains divided by the total area, including that occupied by water.

→ In other words it is the pressure transmitted from particle to particle through their points of contact through soil mass.

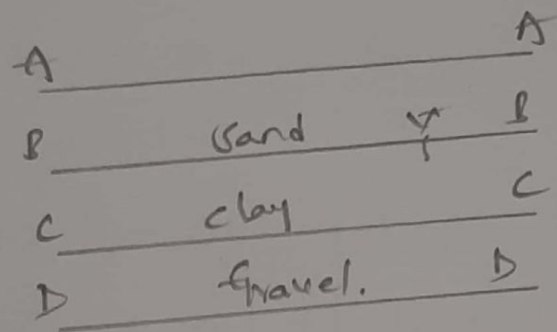
→ It has no physical meaning and it can not be directly measured.

→ It can only be computed knowing the σ & u

→ It is also called as intergranular pressure

→ It is not equal to the actual 'contact stress' it much smaller than the actual 'contact stress'

A soil profile consists of a surface layer of sand 4m thick ($\gamma = 1.6 \text{ t/m}^3$), an intermediate layer of clay 3.5m thick ($\gamma = 1.9 \text{ t/m}^3$) & the bottom layer of the gravel 4m thick ($\gamma = 1.925 \text{ t/m}^3$). The water table is the upper surface of the clay layer. Determine the effective stress at plane D-D.



$$\sigma' = \sigma - u$$

At D-D plane

$$\sigma' = \sigma - u$$

$$\sigma' = (1.6 \times 4) + (1.9 \times 3.5) + (1.925 \times 4) - (7.5 \times 1)$$

$$\sigma' = 13.25 \text{ t/m}^2$$

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* The water which is held in the soil against the gravity is divided into:

- a) Structural water
- b) Adsorbed water
- c) Capillary water.

Structural water :-

↳ It is chemically combined in the crystalline structure of the soil.

↳ Cannot be removed by simple oven drying at 105°C

↳ It is integral part of the soil.

Adsorbed water :-

↳ water held by electrochemical forces existing on the soil surface.

↳ It is important only for clays.

↳ for coarse grained soil the adsorbed water is negligible or zero.

↳ Also called 'hygroscopic water' (the amount of water in an air dried soil).

↳ Can be removed by oven drying.

Capillary water:

$$\text{Capillary rise. } h_c = \frac{4\sigma \cos \alpha}{\rho_w \cdot d}$$

σ = Surface tension of water

α = Contact angle

d = diameter of tube.

↳ In the soil Capillary height, $h_c = 0.8/d$

h_c = Capillary rise in cm.

d = dia of void in cm

$$\text{Note: } h_c \propto \frac{1}{d}$$

Seepage pressure:

→ Total head = pressure head + Velocity head + datum head:

→ The Velocity head in soil is neglected.

Total head = pressure head + datum head

$$\boxed{H = h_w + z}$$

Hydraulic Gradient: :-

→ It is the loss of head per unit seepage distance

$$i = \frac{h}{L}$$

Seepage pressure (P_s): :-

→ The pressure exerted by the water on the soil through which it percolates.

$$\text{Seepage pressure } P_s = \pm \gamma_w \cdot h = i \cdot z \cdot \gamma_w$$

↗ Downward flow
↘ Upward flow

h = net head causing flow

i = hydraulic gradient.

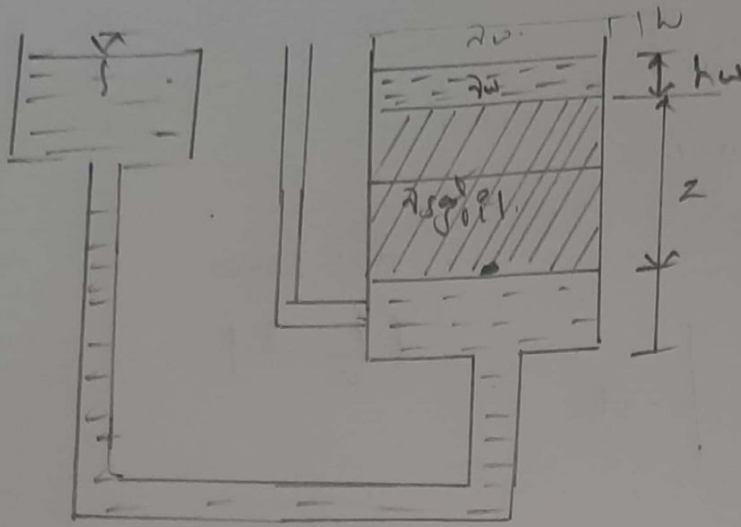
z = seepage length.

* Seepage force per unit volume: $i \cdot \gamma_w$

- i) Seepage pressure always act in the direction of flow
- ii) Due to seepage pressure vertical effective pressure may be increased or decreased based on the direction of the flow
- iii) Effective stress increase if flow is downward direction,
- iv) Effective stress decrease if flow is upwards

Derivation of critical hydraulic gradient ←

→ It is denoted by ' i_c '



→ Where the critical hydraulic gradient occurs when effective stress is equal to zero.

Total stress at point (A): ($\sigma = \gamma \cdot h$)

$$\sigma = \gamma_{sat} \cdot z + \gamma_w \cdot h_w$$

Neutral stress (U) = ($\gamma_w \cdot h$)

$$U = \gamma_w \cdot z + \gamma_w \cdot h_w + \gamma_w \cdot h$$

Effective stress ($\sigma' = (\sigma - U)$)

$$\sigma' = \gamma_{sat} \cdot z + \gamma_w \cdot h_w - (\gamma_w \cdot z + \gamma_w \cdot h_w + \gamma_w \cdot h)$$

$$\sigma' = \gamma_{sat} \cdot z + \gamma_w \cdot z - \gamma_w \cdot h$$

$$\sigma' = (\gamma_{sat} - \gamma_w) z - \gamma_w \cdot h$$

$$\boxed{\sigma' = \gamma' \cdot z - \gamma_w \cdot h}$$

Critical Hydraulic gradient occurs when: $\frac{dI}{dz} = 0$

$$I = \gamma' \cdot z - \gamma_w \cdot h$$

$$\frac{dI}{dz} = 0$$

$$\gamma' \cdot z - \gamma_w \cdot h = 0$$

$$\gamma' \cdot z = \gamma_w \cdot h$$

$$\frac{\gamma'}{\gamma_w} = \frac{h}{z}$$

$$\boxed{I_c = \frac{\gamma'}{\gamma_w}} \quad \text{--- (1)}$$

we know

$$\left(\frac{h}{z} = I \right)$$

$$I_c = \frac{\gamma'}{\gamma_w}$$

$$I_c = \frac{\gamma_{sat} - \gamma_w}{\gamma_w}$$

$$I_c = \frac{\gamma_{sat}}{\gamma_w} - 1$$

$$I_c = \frac{\gamma_w \left(\frac{\gamma_{sat}}{\gamma_w} - 1 \right)}{\gamma_w} - 1$$

$$I_c = \frac{\gamma_w \cdot \left(\frac{\gamma_{sat}}{\gamma_w} - 1 \right)}{\gamma_w} - 1$$

$$I_c = \frac{\gamma_{sat} - \gamma_w}{\gamma_w} - 1$$

$$\frac{\gamma_{sat} - (1 + \gamma_w)}{\gamma_w}$$

$$I_c = \frac{\gamma_{sat} - 1}{\gamma_w} \quad \text{--- (2)}$$

$$\therefore \gamma = (\gamma_{sat} - \gamma_w)$$

$$\gamma_{sat} - \gamma_w \left[\frac{\gamma_{sat} - \gamma_w}{1 + e} \right]$$

$$\gamma_w = 1$$

$$\gamma_{sat} = \gamma_w \left[\frac{\gamma_{sat}}{1 + e} \right]$$

$$\gamma_w = 0$$

$$\gamma_{dry} = \gamma_w \left[\frac{\gamma_{sat}}{1 + e} \right]$$

$$P_c = \frac{q-1}{1+e}$$

$$P_c = q-1 \times \frac{1}{1+e}$$

We know that

$$n = \frac{e}{1+e} \Rightarrow n \cdot (1+e) = e \Rightarrow n + ne = e \Rightarrow n = (e - ne)$$

$$\Rightarrow n = e(1-n) \Rightarrow \frac{n}{e} = (1-n)$$

$$= \frac{e}{1+e} \Rightarrow \frac{e}{1+e} \times \frac{1}{e} \Rightarrow \frac{1}{1+e}$$

$$\therefore 1-n = \frac{1}{1+e}$$

$$= \frac{1+e - e}{1+e}$$

$$\Rightarrow (1-n) = \frac{1}{1+e}$$

$$P_c = \frac{1}{1+e} \times (q-1)$$

$$P_c = (q-1) \times (1-n) \text{ --- (3)}$$

from (1) & (2) & (3).

$$\boxed{P_c = \frac{\sigma'}{\sigma_w} = \frac{q-1}{1+e} = (q-1)(1-n)}$$

A coarse soil having void ratio: 0.7 sp. gravity: 2.7
then find the critical hydraulic gradient.

Given: $e = 0.7$

$$G = 2.7$$

$$i_c = \frac{G - 1}{1 + e} = \frac{2.7 - 1}{1 + 0.7} = 1.$$

$$\boxed{i_c = 1}$$

Quick Sand Condition, or Boiling Condition or Hydraulic Condition:

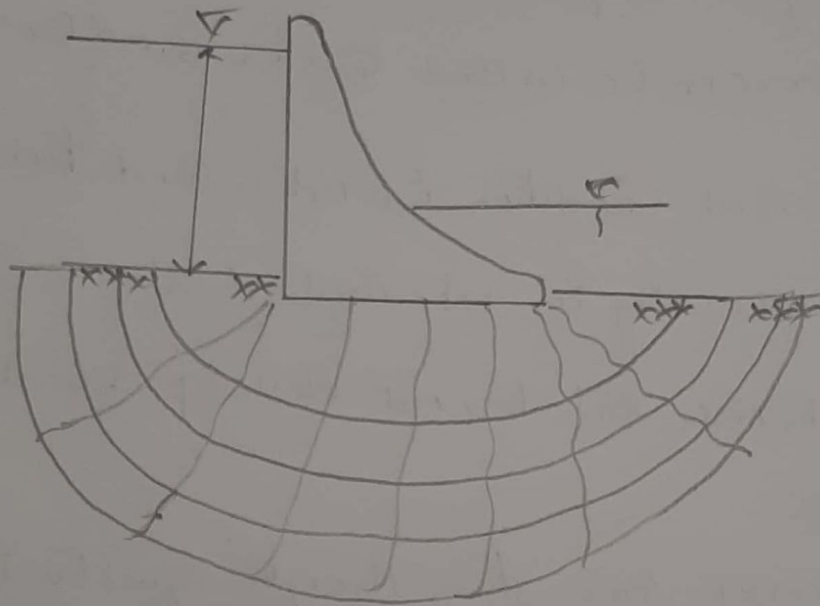
- ↳ The up ward seepage pressure become equal to submerged weight of soil. The effective pressure reduces to zero. In this case sand loses all its shear strength soil particle move in up ward direction. This phenomenon is called Quick sand condition.
- ↳ Quick sand condition is not a sand but flow condition occurring in cohesionless soil.
- ↳ The cohesive soil does not develop Quick sand condition.
- ↳ It possesses some shear strength equal to its cohesive strength even when the effective stress is zero.
- ↳ The Quick sand condition, is most likely to arise in Silt and fine sand.

Flow Net: \div

\rightarrow It is combination of flow line and equipotential lines

Flow line: \div

\rightarrow It is a path along which a water particle travels
It is also called as stream line



Equipotential line: \div

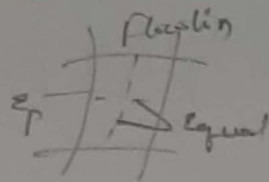
\rightarrow It is a line joining points having equal total head

\rightarrow If piezometer are inserted into the soil at different point along an equipotential line water would be rise to the same elevation in all these piezometer

Note: Along the Equipotential line the total head is constant. while the pressure heads different.
elevation heads are different.

Flow path: \div

→ The space between two adjacent flow lines
Also called as flow channel.



Field:

→ The space b/w any two adjacent flow lines & Equipotential lines.

Characteristic of flow net: \div

- Flow lines & Equipotential lines are orthogonal to each other. (i.e. 90°).
- The quantity of seepage in each flow channel is same.
- Drop in head b/w adjacent equipotential lines is the same.
- Two flow lines or two equipotential lines can never meet or cross each other.
- Fields are kept approximately square.
- Flow net does not depend on permeability of the soil (k) & head causing flow (H).
- Depends on boundary condition only.

uses of flow net:

- a) seepage loss b) seepage pressure
- c) uplift pressure. d) exit gradient.

Seepage Quantity:

$$q = k \cdot H \left[\frac{N_f}{N_d} \right]$$

$k \rightarrow$ permeability of soil.

for an isotropic soil, $k = \sqrt{k_x \cdot k_y}$.

$k_x =$ permeability in horizontal direction

$k_y =$ permeability in vertical direction.

$H =$ net head causing flow (d/bw of & D/c.
water level),

$N_f =$ No. of flow channel.

$N_d =$ No. of potential drops.

\rightarrow the ratio of N_f/N_d is called 'shape factor' of a flow net.

→ if a flownet there are '4' flow channels & 15 equipotential graph, then the estimate the quantity of seepage if head loss is 3m & $k = 2 \times 10^{-5} \text{ m/sec}$

$$N_f = 4$$

$$N_d = 15$$

$$k = 2 \times 10^{-5} \text{ m/sec}$$

$$H = 3 \text{ m}$$

$$Q = k \cdot H \left(\frac{N_f}{N_d} \right) = 2 \times 10^{-5} \times 3 \left(\frac{4}{15} \right)$$

$$Q = 1.6 \times 10^{-5} \text{ m}^3/\text{sec}$$

→ the flownet to determine the seepage through the soil which is an isotropic given 4 flow channels 15 equipotential graphs the coefficient of permeability horizontal & vertical direction are $4 \times 10^{-7} \text{ m/sec}$ & $1 \times 10^{-7} \text{ m/sec}$ resp the storage head is 20m the find seepage of dam.

$$N_f = 4$$

$$N_d = 15$$

$$k_H = 4 \times 10^{-7} \text{ m/sec}$$

$$k_v = 1 \times 10^{-7} \text{ m/sec}$$

$$H = 20 \text{ m}$$

$$K = \sqrt{K_h \cdot k_v}$$

$$= \sqrt{4 \times 10^{-7} \times 1 \times 10^{-7}}$$

$$K = 2 \times 10^{-7} \text{ m/sec}$$

$$Q = K \cdot H \left(\frac{N_f}{N_d} \right)$$

$$= 2 \times 10^{-7} \times 20 \times \left(\frac{4}{5} \right)$$

$$Q = 1.067 \times 10^{-6} \text{ m}^3/\text{sec}$$

UNIT - III

Shear distribution in soils: & Compaction: :-

Compaction: :-

→ It is compression of soil mass by mechanical means to improve engineering properties.

→ It is due to escape & compression of air present in the soil mass.

→ Volume reduction occurs due to escape of air under short term loading under constant water content.

Due to Compaction: :-

- permeability:
 - Void ratio:
 - Compressibility
 - Shear strength → Increase.
- } → Decrease

Compaction test are done to determine: :-

- a) Amount of compactive energy.
- b) The optimum moisture content. (OMC).

Indian Standard Light Weight Compaction Test:
(Similar to standard proctor test.)

- → The test results used for, highways, Embankments, Canal banks.
- → Mould Volume 1 lit. Soil in 3 layer
Each layer is given 25 hammer blows.
- → Hammer weight 2.60 kg & height of fall 31 cm.

Indian Standard Heavy Compaction Test:
(Similar to Modified proctor test):

- → Results used for modern express highways & runways.
- → Mould Capacity 1 lit. Soil in 5 layer
Each layer is given 25 hammer blows.
- → Hammer weight 4.90 kg & height of fall 45 cm.

* The compactive effort in the modified proctor test is about 4.55 times than that in the standard proctor test.

OMC: (Optimum Moisture Content): :-

→ The water content at which the density of the soil maximum is called optimum moisture content.

→ The compaction effect in modified proctor test is 4.55 times the standard proctor test.

Factor affecting the compaction: +

- * → Water content
- * → Type of soil
- * → Amount of compaction.

* → Water Content: :-

→ As a water content increase the dry density increases. reaches the maximum value then decrease

* Type of soil: Sandy soil & gravel soil are more comp to clay soil & silty soil.

* Amount of compaction: :-

→ As a load increase dry density increase, moisture content decrease

Compaction Equipment:

a) Tampers:

↳ for compacting in confined areas like French drains behind bridge abutments.

b) Smooth wheel rollers:

↳ for granular soil provide smooth surface at the end of the days. work to quickly drain off rain water.

c) pneumatic tyred rollers:

↳ for cohesive & non-cohesive soils

d) Sheep foot rollers:

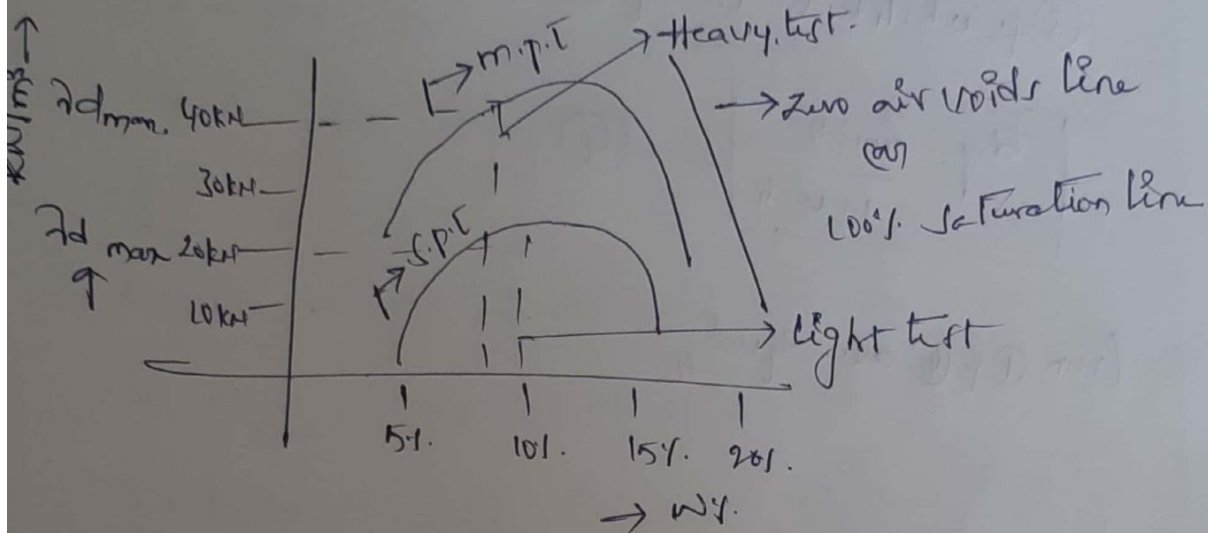
↳ for cohesive soil - (clays).

e) Vibratory compactors:

↳ for granular soil (forward best method).

**
Equation for zero air void line (or) 100% saturation line
(or) theoretical max dry density (theoretical):

→ the dry density which is achieved practically by the expansion of air from voids of soil.



$$\gamma_{dry} = \frac{(1 - a_v) \gamma_w \cdot G}{1 + w \cdot G}$$

for zero air voids line ($a_v = 0$)

$$\gamma_{dry} = \frac{\gamma_w \cdot G}{1 + w \cdot G} \quad \text{--- (V)}$$

When the soil is fully saturated the entire air replaced by water.

$$(G_r = 100\%)$$

100% Saturation ($G_r = 100\% = 1$).

$$\gamma_{dry} = \frac{\gamma_w \cdot q}{1 + e} \quad \text{--- (2)}$$

for 100% saturation $e = \frac{w \cdot q}{S_r} \quad \therefore S_r = 1$

$$e = w \cdot q \quad \text{--- (3)}$$

③ substitute in eq. ②

$$\boxed{\gamma_{dry} = \frac{\gamma_w \cdot q}{1 + w \cdot q}} \quad \text{--- (4)}$$

from ① & ④ are equal

procedure for find the Dry density:-

→ Take Soil 2.5 kg which is passed through 4.75mm sieve

Sieve

→ Add. Some wt. of water

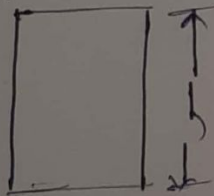
→ Let the weight of the empty proctor test mould be w_1

→ the weight of the wet soil + proctor mould be w_2

→ then weight of the wet soil is $w_2 - w_1$

→ Bulk density $(\gamma_{bulk}) = \frac{w_2 - w_1}{V} = \frac{w_2 - w_1}{\frac{\pi}{4} d^2 \times h}$

Round/dia



$$\gamma_{bulk} = \frac{w_2 - w_1}{\frac{\pi}{4} d^2 \times h}$$

Table $\gamma_{dry} = \frac{\gamma_{bulk}}{1+w}$

S.No:	water content (%)	γ_{bulk}	γ_{dry}
1	10 %	$\frac{w_2 - w_1}{\frac{\pi}{4} d^2 \times h}$	$\frac{\gamma_{bulk}}{1+w}$
2	20 %	✓	✓
3	30 %	✓	✓
4	40 %	✓	✓
5	50 %	✓	✓

An Earth Embankment is compacted at a water content of 18%. To bulk density of 19.2 kN/m^3 . If the sp. gravity of sand is 2.7. Find the void ratio & degree of saturation of the compacted Embankment.

Water content: $w = 18\%$.

Bulk density: $\gamma = 19.2 \text{ kN/m}^3$

Sp. Gravity, $G = 2.7$

$$\text{Dry density} = \gamma_d = \frac{\gamma}{1+w} = \frac{19.2}{(1+0.18)} = 16.27 \text{ kN/m}^3$$

$$\text{but: } \gamma_d = \frac{G \cdot \gamma_w}{1+e}, \text{ where } \gamma_w = 9.81 \text{ kN/m}^3$$

$$1+e = \frac{G \cdot \gamma_w}{\gamma_d} = \frac{2.7 \times 9.81}{16.27} = 1.63 \quad \therefore 1+e = 1.63$$

$$e = 1 - 103$$

$$e = 0.63$$

Void ratio: $e = 0.63$.

$$\text{Also: } wG = Se$$

$$\text{Degree of saturation: } S_r = \frac{w \cdot G}{e}$$

$$= \frac{0.18 \times 2.7}{0.63}$$

$$= 0.7714$$

$$= 77.14\%$$

Stress Distribution in Soil: -

Introduction: -

→ Stress in soil is caused by the soil. first or both of the following:

- 1) Self weight of soil.
- 2) Structural load applied at or below the surface

→ many problems in foundation engineering require a study of the transmission & distribution of stresses in large extensive masses of soil.

→ Some examples are wheel loads transmitted through Embankment to Culverts.

→ foundation pressure transmitted to soil strata below footing.

→ pressure from isolated footing transmitted to retaining walls, & wheel loads transmitted through stabilised soil pavement to subgrade below.

→ In such cases the stresses are transmitted both downward and lateral direction.

→ The vertical stress in soil owing to its self-weight also called 'geostatic stress'

$$\boxed{\sigma_z = \gamma \cdot z}$$

Point Load: ←

→ A point load or a concentrated load is strictly.

Speaking, hypothetical in nature, consideration of it serves a useful purpose in arriving at the solution.

for more loading complex in practice.

→ The most fundamental of the solution of stress distribution in soil is that for a point load applied at the surface.

→ Boussinesq & Westergaard have given the solution with the different assumptions regarding the soil media.

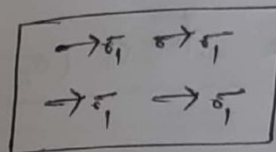
Boussinesq's Equation:

→ Boussinesq Equation has given the solution for the stresses caused by the application of point load at the surface of a "Homogeneous, Elastic, isotropic, & Semi-Infinite medium". weight less & the load is a point load acting on the ground surface.

Homogeneous:

→ A material is said to be homogeneous if it is identical properties at the different properties in identical direction.

(or)



→ At any point the given direction the properties are same. Ex: Wood, Copper.

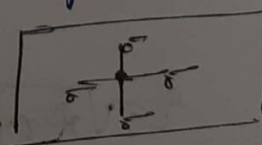
Isotropic:

→ At a given point that in any direction the properties are same.

(or)

→ A material is said to be isotropic when it has identical elastic properties in all direction at a point.

Ex: Steel, Iron, brass.



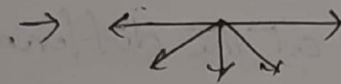
→ Strength of material should be applied for both
 - Homogenous, isotropic material.

* → All Homogenous material need not be the isotropic.

* → All isotropic materials need to be the homogenous.

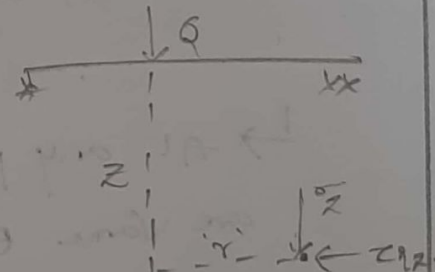
Semi infinite:

→ A material is said to be semi-infinite if it extends infinite in all directions below the horizontal surface.



* Vertical stress (σ_z):

$$\sigma_z = \frac{Q}{z^2} \cdot \frac{3}{2\pi} \left[\frac{1}{1 + \left(\frac{r}{z}\right)^2} \right]^{5/2}$$



z = Vertical distance of the point below the load.

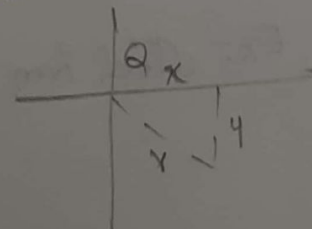
Q = point load

r = radial distance of the point = $\sqrt{x^2 + y^2}$

(or): $\sigma_z = \frac{Q}{z^2} \cdot k_B$ **

To find the settlement criteria.

$$r = \sqrt{x^2 + y^2}$$



where k_B = Boussinesq's constant.

$$k_B = \frac{3}{2\pi} \left[\frac{1}{1 + \left(\frac{r}{z}\right)^2} \right]^{5/2}$$

(or)

$$\sigma_z = 0.477 \frac{Q}{z^2}$$

→ The Vertical stress (σ_z) below the point load. ($\because r=0$)

$$\sigma_z = \frac{Q}{z^2} \cdot \frac{3}{2\pi}$$

$$\sigma_z = 0.477 \frac{Q}{z^2} **$$

A point load of 700kN is applied on the surface of clay using Boussinesq's Equation estimate the vertical stress at the depth of 2kN & radial distance of 1m from the point application of load

$$\text{point load} = (Q) = 700 \text{ kN}$$

$$\text{depth } (z) = 2 \text{ m}$$

$$r = 1 \text{ m}$$

$$\sigma_z = \frac{Q}{z^2} \cdot \frac{3}{2\pi} \left[\frac{1}{1 + \left(\frac{r}{z}\right)^2} \right]^{5/2}$$

$$\sigma_z = \frac{700}{2^2} \cdot \frac{3}{2\pi} \left[\frac{1}{1 + \left(\frac{1}{2}\right)^2} \right]^{5/2} \Rightarrow 47.63 \text{ kN/m}^2$$

A concentrated load of 200kN is applied on ground surface of clay. Find the vertical stress at the point which is 7m directly below the load using the Boussinesq's theorem:

point load: $Q = 200 \text{ kN}$

depth $(z) = 7 \text{ m}$

$$\sigma_z = 0.477 \frac{Q}{z^2}$$

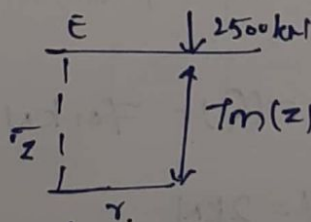
$$\sigma_z = 0.477 \times \frac{200}{7^2}$$

$$\sigma_z = 13.62 \text{ kN/m}^2$$

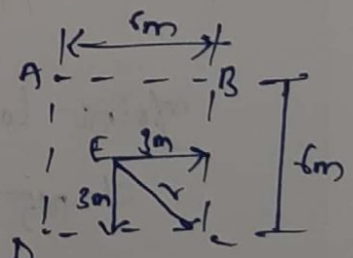
An elevated structure with a total weight of 2500kN is supported on a tower with 4 legs. The legs are on piers located at the corners of a square 6m on a side. What is the vertical stress increment due to this loading at point 7m beneath the centre of the structure.

Sol: $Q = 2500 \text{ kN}$

→ the load centre



approximated to a point load acting at the corners of a square of 6m side.



The vertical stress is to be calculated at 7m depth.

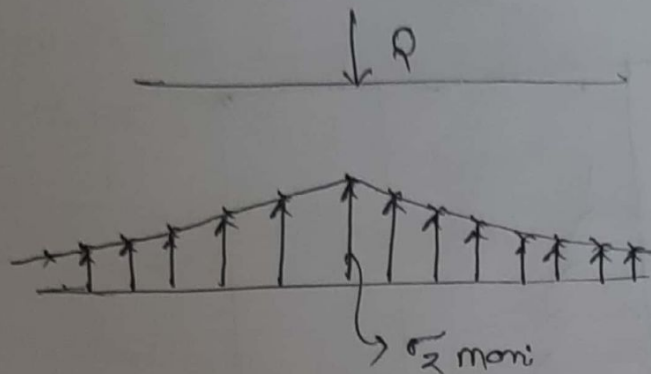
Horizontal distance r from each of the load is equal.

$$\sqrt{r^2 + r^2} = \sqrt{r^2} = 4.23 \text{ m}$$

$$= \frac{4 \times 7 \times 2500}{2\pi \times 7^2} \left[\frac{1}{1 + \left(\frac{4.23}{7}\right)^2} \right]^{\frac{5}{2}} = 4 \times 11.143 = 44.57 \text{ kN/m}^2$$

4

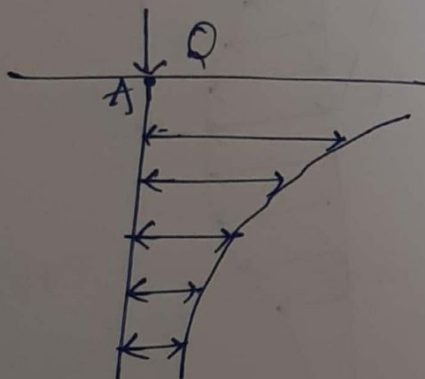
Vertical stress along the Horizontal plane:-



σ_z is max @ $r=0$.

Vertical stress Variation on Vertical plane: passing below the load

i.e. $r=0$.

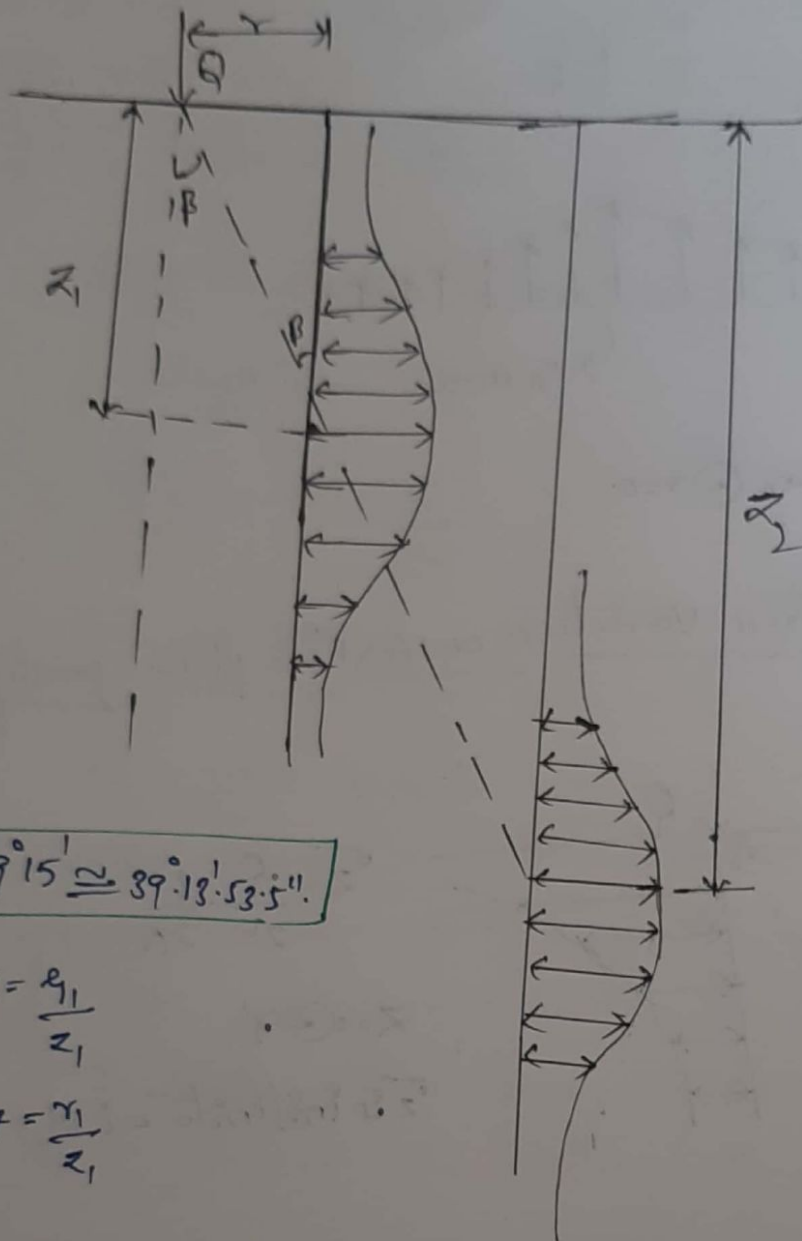


$$\sigma_z = \frac{Q}{z^2} \cdot \frac{3}{2\pi}$$

$z=0$ @ A'

σ_z is infinite at A'

2. Vertical stress variation on vertical plane away from the load



$$\beta = 39^{\circ}15' \approx 39.13^{\circ}53.5''$$

$$\tan \beta = \frac{r_1}{z_1}$$

$$0.817 = \frac{r_1}{z_1}$$

$$\sigma_{z_1} > \sigma_{z_2} \quad (\because z_1 < z_2).$$

If a vertical plane is drawn at radial distance of 2m. from a point. Determine the depths at which the max. vertical stress.

$$r_1 = 2\text{m.}$$

$$\tan \beta = \frac{r_1}{z_1}$$

$$\tan (39^{\circ}15') = \frac{2}{z_1} \Rightarrow z_1 = 2.44\text{m.}$$

A concentrated load of 50 kN is vertically applied at a point on the soil surface. If Boussinesq's eqⁿ is applied for computation of stress then the ratio of vertical stress at depths of 3m & 5m respectively, vertically below the point of application of load will be

Vertically below the load:

$$\sigma_z \propto \frac{1}{z^2}$$

$$\frac{\sigma_{z_1}}{\sigma_{z_2}} = \left(\frac{z_2}{z_1} \right)^2 = \left(\frac{5}{3} \right)^2$$

$$\frac{\sigma_{z_1}}{\sigma_{z_2}} = 2.77$$

σ_z doesn't depend upon young's modulus and poisson ratio of the soil.

→ Point load of 700 kN

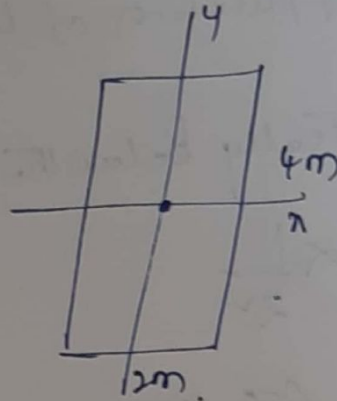
→ A rectangle area of $2\text{m} \times 4\text{m}$ carries a load of 8 ton/m^2 at a ground surface — find the vertical stress at 5m below the center and corner of loaded area using Boussinesq's theorem.

$$Q = 8 \text{ t/m}^2$$

$$Z = 5\text{m}$$

i) σ_z at Centre

ii) σ_z at corner



$$\sigma_z = \frac{Q}{Z^2} \cdot \frac{3}{2\pi} \left(\frac{1}{1 + \left(\frac{r}{Z}\right)^2} \right)^{5/2}$$

At Center: ($r=0$):

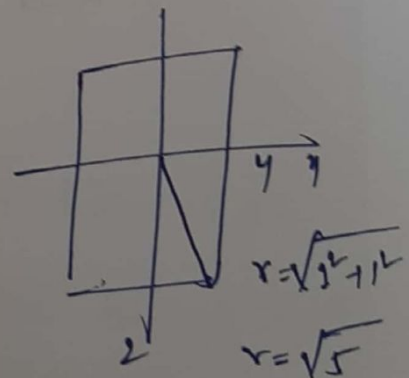
$$\sigma_z = \frac{8}{5^2} \cdot \frac{3}{2\pi} \left(\frac{1}{1 + \left(\frac{0}{5}\right)^2} \right)^{5/2}$$

$$\sigma_z = 0.152 \text{ t/m}^2$$

σ_z at corner:

$$\sigma_z = \frac{8}{5^2} \cdot \frac{3}{2\pi} \times \left[\frac{1}{1 + \left(\frac{\sqrt{5}}{5}\right)^2} \right]^{5/2}$$

$$\sigma_z = 0.095 \text{ t/m}^2$$



Westergaards Equation:-

Assumption:-

- The soil is homogeneous, Non isotropic & semi-infinite
- This theory is suitable for stratified soil.
- The soil is only vertical deformation not a horizontal deformation.
- The theory is suitable for only, sedimentary soil.
Not suitable for residual soil.

$$\sigma_z = \frac{Q}{z^2} \cdot \frac{1}{\pi} \left[\frac{1}{1+2\left(\frac{r}{z}\right)^2} \right]^{3/2}$$

σ_z = Vertical stress in Westergaards Equation:

Q = point load.

z = depth

r = radial distance

$$\sigma_z = \frac{Q}{z^2} \cdot k_w$$

k_w = Westergaards constant.

$$k_w = \frac{1}{\pi} \left[\frac{1}{1+2\left(\frac{r}{z}\right)^2} \right]^{3/2}$$

Westergaard's Equation:-

Assumptions:-

- The soil is homogeneous, Non isotropic & semi-infinite
- The theory is suitable for stratified soil.
- The soil is only vertical deformation not a horizontal deformation.
- The theory is suitable for only, sedimentary soil.
Not suitable for granular soil.

$$\sigma_z = \frac{Q}{z^2} \cdot \frac{1}{\pi} \left[\frac{1}{1 + 2\left(\frac{r}{z}\right)^2} \right]^{3/2}$$

σ_z = Vertical stress in Westergaard's Equation:

Q = point load.

z = depth

r = radial distance

$$\sigma_z = \frac{Q}{z^2} \cdot k_w$$

k_w = Westergaard's constant.

$$k_w = \frac{1}{\pi} \left[\frac{1}{1 + 2\left(\frac{r}{z}\right)^2} \right]^{3/2}$$

the Westergaards Vertical stress directly below the point load ($r=0$).

$$\bar{\sigma}_z = 0.318 \frac{Q}{z^2}$$

↳ A concentrated load of 2500 kN is applied ground surface determine the vertical stress at a point 'p' which is at a depth of 5m but a horizontal distance of 4m from the axis of the load:

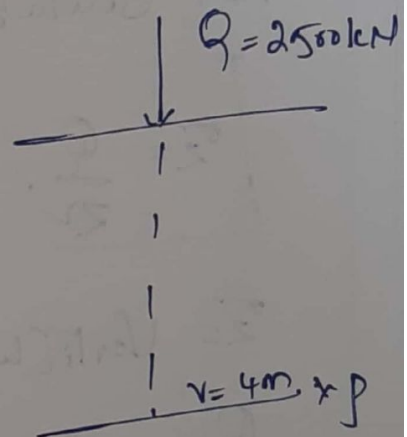
$$Q = 2500 \text{ kN}$$

$$z = 5 \text{ m}$$

$$\bar{\sigma}_z = \frac{Q}{z^2} \cdot \frac{1}{\pi} \left[\frac{1}{1 + 2\left(\frac{r}{z}\right)^2} \right]^{3/2}$$

$$\frac{2500}{5^2} \cdot \frac{1}{\pi} \left[\frac{1}{1 + 2\left(\frac{4}{5}\right)^2} \right]^{3/2}$$

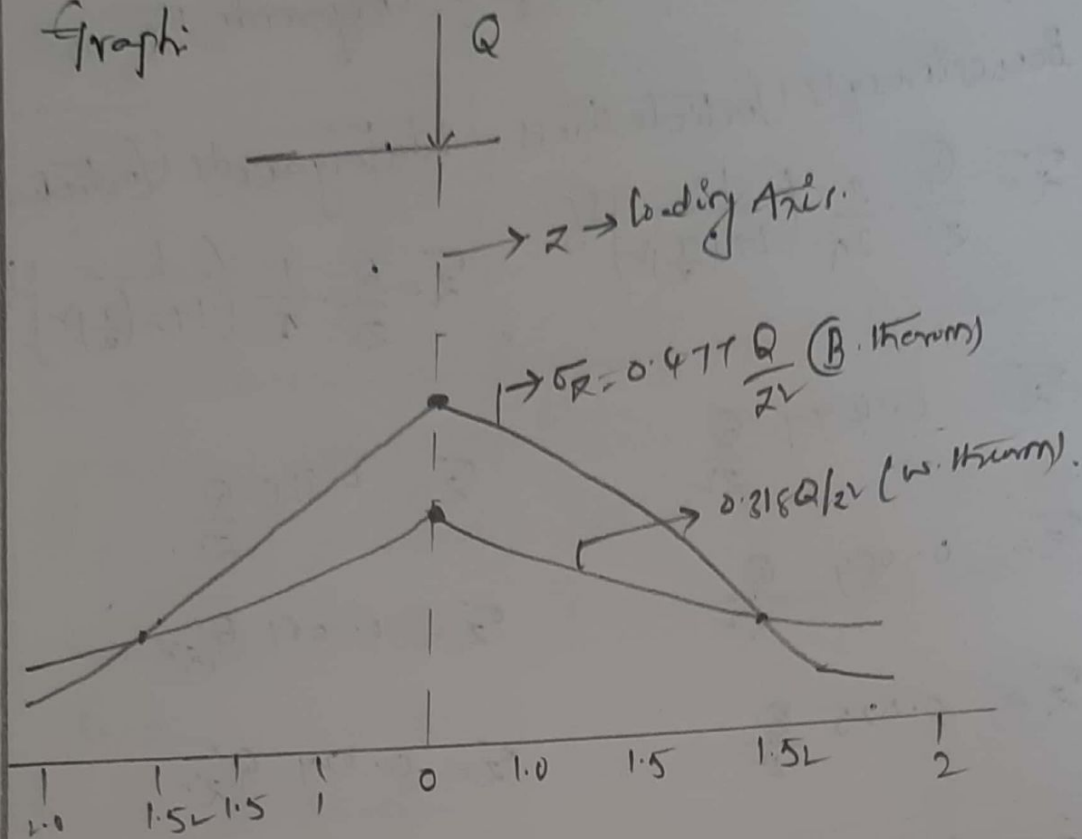
$$\bar{\sigma}_z = 9.245 \text{ kN/m}^2$$



Comparison b/w Boussinesq's & Westergaard's theory:

$\frac{r}{z}$	Boussinesq's Vertical stress $\sigma_z = \frac{Q}{z^2} \cdot \frac{3}{2\pi} \left(\frac{1}{1 + (\frac{r}{z})^2} \right)^{3/2}$	Westergaard's Vertical stress $\sigma_z = \frac{Q}{z^2} \cdot \frac{1}{\pi} \left(\frac{1}{1 + 2(\frac{r}{z})^2} \right)^{3/2}$
0	$\sigma_z = 0.477 \frac{Q}{z^2}$	$\sigma_z = 0.318 \frac{Q}{z^2}$
1	$\sigma_z = 0.084 \frac{Q}{z^2}$	$\sigma_z = 0.061 \frac{Q}{z^2}$
1.5	$\sigma_z = 0.025 \frac{Q}{z^2}$	$\sigma_z = 0.024 \frac{Q}{z^2}$
4.5	$\sigma_z = 0.023 \frac{Q}{z^2}$	$\sigma_z = 0.023 \frac{Q}{z^2}$
2.0	$\sigma_z = 0.0085 \frac{Q}{z^2}$	$\sigma_z = 0.11 \frac{Q}{z^2}$

Graph:



Comparison: (k_w & k_B):

$$\text{If } \frac{r}{2} = 1.52 \quad k_w = k_B$$

$$\text{If } \frac{r}{2} > 1.52 \quad k_w > k_B$$

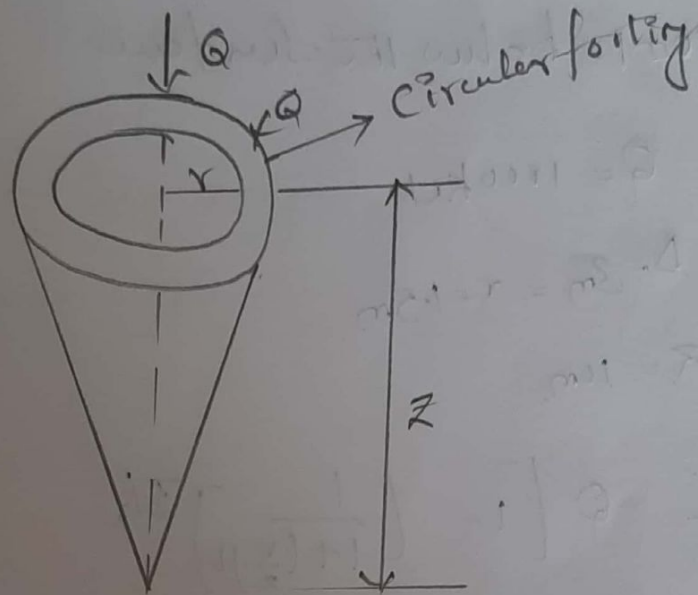
$$\text{If } \frac{r}{2} < 1.52 \quad k_w < k_B$$

The value is 1.52

8

Vertical stress distribution below uniformly-
Circular loaded areas:

↳ Generally Circular foundation is adopted.
beneath the Circular water tank, oil storage
tank, well foundation:



$$\sigma_z = Q \left[1 - \left(\frac{1}{1 + \frac{r^2}{z^2}} \right)^{3/2} \right]$$

σ_z = Vertical stress due to Circular load area

Q = Vertical load

r = radius Circular area

z = depth.

A circular foundation is rest on horizontal surface of soil the load of a foundation 1000kN. the diameter of the foundation is 3m, determine the vertical stress on horizontal plane along the central axis of the foundation to a depth of 10m. below the surface

$$Q = 1000 \text{ kN}$$

$$D = 3\text{m} = r = 1.5\text{m}$$

$$z = 10\text{m}$$

$$\sigma_z = Q \left[1 - \left(\frac{1}{1 + \left(\frac{r}{z} \right)^2} \right)^{3/2} \right]$$

$$1000 \left[1 - \left(\frac{1}{1 + \left(\frac{1.5}{10} \right)^2} \right)^{3/2} \right]$$

$$\sigma_z = 32.825 \text{ kN/m}^2$$

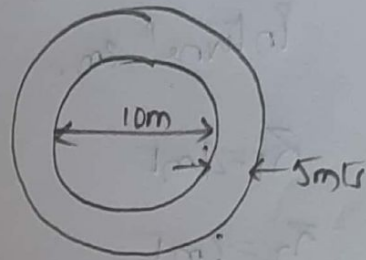
A loading of 50 kN/m^2 is acting on circular foundation of width of 5m & inside dia of 10m .
find the vertical stress intensity at depth of 10m below the centre of foundation.

load: $Q = 50 \text{ kN/m}^2$

width $(w) = 5\text{m}$

Inside dia $(d) = 10\text{m}$

Depth $(z) = 10\text{m}$



$D_i = 10\text{m}$ $r_i = 5\text{m}$

$D_o = 20\text{m}$ $r_o = 10\text{m}$

$\bar{\sigma}_z = \sigma_z \text{ outlet} - \sigma_z \text{ inlet}$

$$\sigma_z = Q \left[1 - \left(\frac{1}{1 + \left(\frac{r_o}{z} \right)^2} \right)^{3/2} \right] - Q \left[1 - \left(\frac{1}{1 + \left(\frac{r_i}{z} \right)^2} \right)^{3/2} \right]$$

$$50 \left[1 - \left(\frac{1}{1 + \left(\frac{10}{10} \right)^2} \right)^{3/2} \right] - 50 \left[1 - \left(\frac{1}{1 + \left(\frac{5}{10} \right)^2} \right)^{3/2} \right]$$

$\bar{\sigma}_z = 18.1 \text{ kN/m}^2$

A circular ring footing of external & internal diameter of 6m & 3m deep transmit a pressure of 200 N/mm². Calculate vertical stress at depths of 1m & 3m.

$$\text{Load } Q = 200 \text{ N/mm}^2$$

External 6m

Internal 3m.

$$Z_1 = 1 \text{ m}$$

$$Z_2 = 3 \text{ m}$$

$$D_i = 3 \text{ m } r_i = 1.5$$

$$D_o = 6 \text{ m } R_o = 3 \text{ m}$$

$$\sigma_z = \sigma_{z \text{ outlet}} - \sigma_{z \text{ inlet}}$$

$$\sigma_z = Q \left[1 - \left(\frac{1}{1 + \left(\frac{r_o}{z} \right)^2} \right)^{3/2} \right] - Q \left[1 - \left(\frac{1}{1 + \left(\frac{r_i}{z} \right)^2} \right)^{3/2} \right]$$

$$200 \left[1 - \frac{1}{1 + \left(\frac{3}{1} \right)^2} \right]^{3/2} - 200 \left[1 - \frac{1}{1 + \left(\frac{1.5}{1} \right)^2} \right]^{3/2}$$

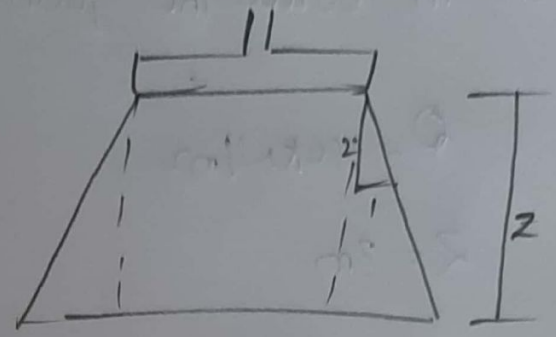
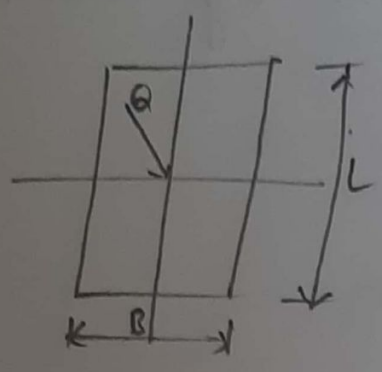
$$\boxed{\sigma_z = 55.55 \text{ N/mm}^2}$$

Case ii $z = 3 \text{ m}$

$$200 \left[1 - \frac{1}{1 + \left(\frac{3}{3} \right)^2} \right]^{3/2} - 200 \left[1 - \frac{1}{1 + \left(\frac{1.5}{3} \right)^2} \right]^{3/2}$$

$$\boxed{\sigma_z = 52.38 \text{ N/mm}^2}$$

To find Vertical Stress by Approximate method
i.e. 2 Vertical 1 Horizontal method (2V:1H):



Formula:

$$\sigma_z = \frac{Q}{(L+Z)(B+Z)} \rightarrow \text{rectangle} \rightarrow \text{for 2V:1H}$$

σ_z = Vertical Stress Approximate -

Q = load

L = length

B = Breadth

Z = depth

A rectangle area of $2\text{m} \times 4\text{m}$ carries a load of 180 kN/m^2 at the ground surface find the vertical stress 3m below the foundation using 2D: 1/4 method.

$$Q = 180\text{ kN/m}^2$$

$$Z = 3\text{m}$$

$$\sigma_z = \frac{Q}{(L+Z)(B+Z)}$$

$$= \frac{180}{(4+3)(2+3)}$$

$$\sigma_z = 14.28\text{ kN/m}^2.$$

UNIT - 4:

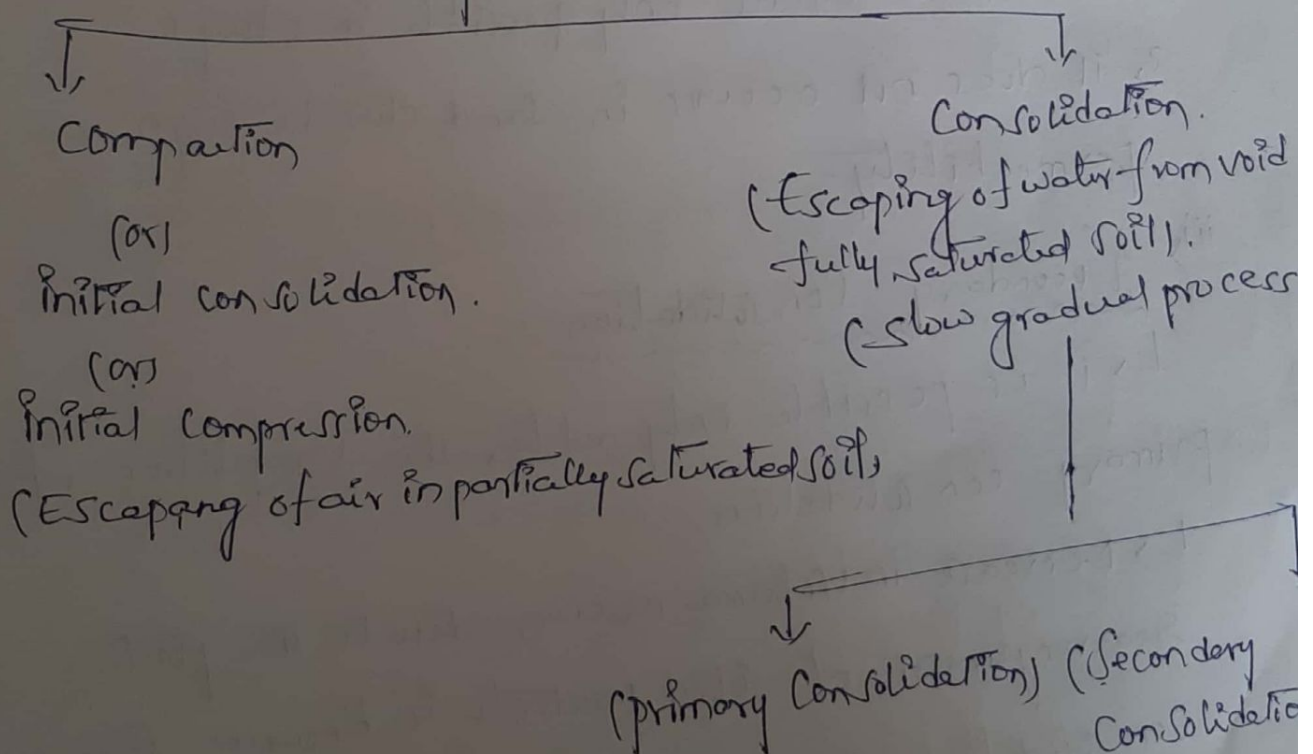
Consolidation of Soil:

↳ Compressibility: Gradual decrease in the volume of soil due to application of load on soil mass.

* → The volume change take place may be due to.

- 1) Compression & Expulsion of pore air.
- 2) Expulsion of pore water.
- 3) plastic rearrangement of soil particle.

Compression:



i) Initial Consolidation or Compaction :-

↳ Escaping of air or Compression of the air in Voids immediately after loading is initial consolidation.

ii) Primary Consolidation :-

↳ After completion of compaction the further decrease in volume due to escaping of water from the Voids in primary Consolidation.

↳ It is slow & gradual process & it occurs under long term static loading.

2, Consolidation is only possible in clays.

3, It does not occur in sand, due to high permeability.

iii) Secondary Consolidation :-

↳ It is possible only after the completion of primary consolidation.

↳ Decrease in volume occurs due to the plastic rearrangement of solid particle is known as Secondary Consolidation or Creep.

↳ Generally 10-20% of primary Consolidation is possible.

Consolidation:

→ It is the compression of soil mass due to expulsion of removed water from the voids. under steady, static long term loading.

Compaction:

→ escape of Air voids from voids

→ short term loading

→ Quick process.
Take less time.

Consolidation

→ escape of water from voids.

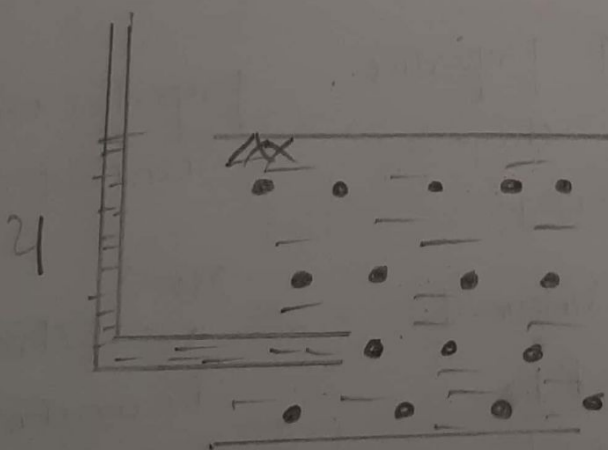
→ long term or static or steady loading.

→ slow process
Take more time

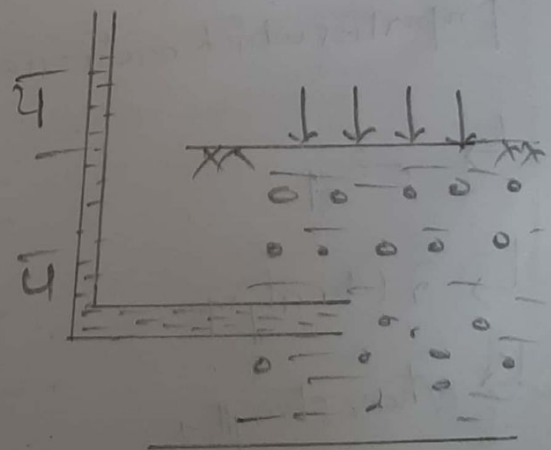
Compressibility

→ escape of water.

During Consolidation process:



u → pore water pressure
or hydrostatic pressure



u → Excess of pore water
hydrodynamic pressure

At Beginning of consolidation

$$\sigma = u$$

$$\sigma' = \sigma - u$$

$$\sigma = 0$$

σ constant

At during of consolidation

$$u < \sigma$$

$$\sigma' = \sigma - u$$

$$\sigma' > 0$$

σ constant

At the end of consolidation

$$u = 0$$

$$\sigma' = \sigma - u$$

$$\sigma' = \sigma$$

σ constant

During consolidation:-

- ↳ excess pore water pressure is u decrease
- ↳ effective stress (σ') is increase
- ↳ Total stress is σ is constant.

During consolidation:-

properties which are increase ↑

properties decrease ↓

properties which constant.

$$\rightarrow \sigma' \uparrow$$

$$\rightarrow \gamma \text{ (density)} \uparrow$$

$$\rightarrow \text{shear strength} \uparrow$$

$$\rightarrow u \downarrow$$

$$\rightarrow \text{volume} \downarrow$$

$$\rightarrow K \downarrow$$

$$\rightarrow \text{water content} \downarrow$$

$$\rightarrow e \downarrow$$

$$\rightarrow (\sigma) \text{ Total stress is constant}$$

Compressibility:-

↳ Reduction in Volume of the soil due to escape of air and water from the voids.

Co-efficient of compressibility (a_v)

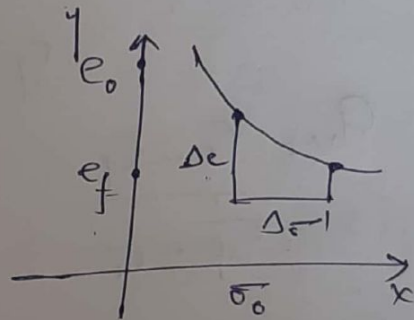
($e-p$ Curve or $e-\sigma'$ Curve)
(Void ratio - pressure) (Void ratio - effective stress)

↳ It is the ratio of decrease in void ratio per unit increase of effective stress.

$$a_v = \frac{\Delta e}{\Delta \sigma'}$$

$$a_v = \frac{e_0 - e_f}{\sigma'_f - \sigma'_0}$$

units: m^2/kN



$a_v \rightarrow$ Co-efficient of compressibility.

$e_0 \rightarrow$ initial void ratio.

$e_f \rightarrow$ final void ratio.

$\sigma'_f \rightarrow$ final effective stress

$\sigma'_0 \rightarrow$ initial effective stress.

↳ The consolidation test on clay sample of
 Co-efficient of compressibility is $50 \text{ m}^2/\text{kN}$
 the initial void ratio is 0.6 . the stress intensity increase
 from 100 to 300 kN/m^2 . then find the final void ratio

Sol: Co-efficient of compressibility: $C_v = 50 \text{ m}^2/\text{kN}$

Initial void ratio: $e_0 = 0.6$

the stress intensity $= \sigma'_0 = 100 \text{ kN/m}^2$

$\sigma'_f = 300 \text{ kN/m}^2$

$e_f = ?$

$$C_v = \frac{e_0 - e_f}{\frac{1}{\sigma'_f} - \frac{1}{\sigma'_0}}$$

$$50 = \frac{0.6 - e_f}{\frac{1}{300} - \frac{1}{100}}$$

$$50 \times 200 = 0.6 - e_f$$

$$-10 \times 10^3 + 0.6 = e_f$$

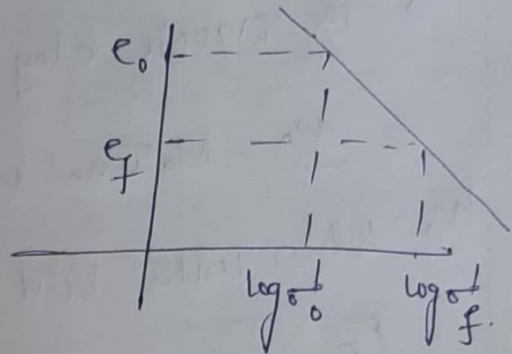
$$e_f = 9.994 \times 10^3$$

→ C-log p or e-log σ' curve or

Co-efficient of compression index (C_c):-

↳ The slope linear portion of e-log σ' curve is called co-efficient of compressibility.

$$C_c = \frac{e_0 - e_f}{\log \frac{\sigma'_f}{\sigma'_0}}$$



$$C_c = \frac{\Delta e}{\log \left(\frac{\sigma'_f}{\sigma'_0} \right)}$$

C_c = co-efficient of compressibility index.

e_0 → Initial void ratio.

e_f → final void ratio.

σ'_0 → initial effective stress

σ'_f → final effective stress

for most of the clays C_c lies in between, 0.1 to 0.8.

Empirical relation for determination of C_c :-

i) for undisturbed clay $C_c = 0.009 (w_L - 10)$

w_L = Liquid Limit in %

ii) for remoulded clay $C_c = 0.007 (w_L - 10)$

iii) for organic clay $C_c = 0.015 w_n$

w_n = Natural water content in %

iv) When initial void ratio is known as

$$C_c = 1.15 (e_0 - 0.35) \quad e_0 = \text{initial void ratio}$$

→ The consolidation test remoulded clay sample of liquid limit 50%. The initial void ratio is 0.6

The stress increasing intensity from 100 kPa. 300 kPa. then find the final void ratio.

Sol: $C_c = (0.007) (w_L - 10)$ for remoulded clay.

Initial void ratio: $e_0 = 0.6$

Stress intensity $(\sigma'_0) = 100 \text{ kPa.}$

$$\sigma'_f = 300 \text{ kPa.}$$

$$C_f = ?$$

$$C_c = \frac{e_0 - e_f}{\log \frac{\sigma_f'}{\sigma_0'}}$$

$$C_c = \frac{e_0 - e_f}{\log \left(\frac{\sigma_f'}{\sigma_0'} \right)}$$

$$= \frac{0.007(40\%) = 0.6 - e_f}{\log \left(\frac{300}{100} \right)}$$

$$= 0.007 \left(\frac{40}{100} \right) \times \log \left(\frac{300}{100} \right) = 0.6 - e_f$$

$$\boxed{e_f = 0.467}$$

Co-efficient of Volume Compressibility (M_v):

→ it is change in volume of the soil, per unit initial volume due to increase in stress.

$$M_v = \frac{\Delta v}{V_0 \cdot \Delta \sigma} \quad \text{① Unit } \sigma \rightarrow \text{m}^2/\text{KN}$$

$M_v \rightarrow$ Co-efficient of Volume Compressibility (M_v).

$\Delta v \rightarrow$ change in volume

$V_0 \rightarrow$ initial volume

$\Delta \sigma \rightarrow$ change in stress.

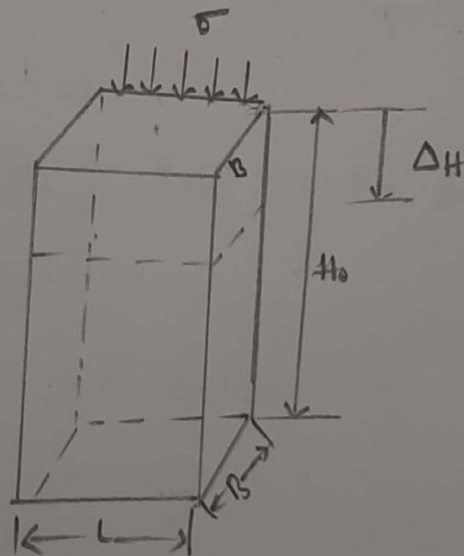
$$\frac{\Delta v}{V_0} = \frac{A \times \Delta H}{A \times H_0} \quad \text{② (A is constant for confined soil).}$$

$$\frac{\Delta v}{V_0} = \frac{\Delta H}{H_0} \quad \text{③}$$

We know that:

$$\frac{\Delta v}{V_0} = \frac{\Delta e}{1+e_0}$$

$$\frac{\Delta v}{V_0} = \frac{\Delta H}{H_0} = \frac{\Delta e}{1+e_0}$$



$$M_v = \frac{\Delta v}{V_0 \cdot \Delta \sigma} = \frac{\Delta H}{H_0 \cdot \Delta \sigma} = \frac{\Delta e}{(1+e_0) \Delta \sigma}$$

The following data is given in laboratory $\sigma_0 = 175 \text{ kPa}$
 $e_0 = 1.1$, $\sigma_0 + \Delta\sigma = 300 \text{ kPa}$, $e_f = 0.9$ If the thickness of clay
 Specimen, is 25 mm. Then find Volume & co-eff. of
 Volume compressibility. (2002 - Gate).

Sol: $\sigma_0 = 175 \text{ kPa}$

$e_0 = 1.1$

$e_f = 0.9$

$\sigma_0 + \Delta\sigma = 300 \text{ kPa}$

Thickness of clay specimen, = 25 mm.

Co-efficient of compressibility $(M_v) = \frac{\Delta e}{(1+e_0)\Delta\sigma}$

$\sigma_0 + \Delta e = 300$

$\Delta e = 300 - 175$

$\Delta\sigma = 125 \text{ kPa}$

$\Delta e = e_0 - e_f$

$= 1.1 - 0.9$

$\Delta e = 0.2$

$M_v = \frac{\Delta e}{(1+e_0)\Delta\sigma}$

$= \frac{0.2}{(1+1.1)(125)}$

$M_v = 7.61 \times 10^{-4} \text{ m/kN}$

→ In a Consolidation test, the void ratio of specimen is 1.052 under the effective pressure is 207 kN/m². The void ratio changed to 0.932 when pressure was increased to 430 kN/m². Then find the:

- i) Co-efficient of compressibility.
- ii) Co-efficient of Volume - compressibility.
- iii) Co-efficient of compression index

Void ratio of specimen. $e_0 = 1.052$

effective pressure $(\sigma'_0) = 207 \text{ kN/m}^2$

Void ratio changed to $= e_f = 0.932$

pressure was increased $= (\sigma'_f) = 430 \text{ kN/m}^2$

→ Co-efficient of compressibility index.

$$C_c = \frac{e_0 - e_f}{\log \sigma'_f - \log \sigma'_0}$$

$$= \frac{\Delta e}{\log \left(\frac{\sigma'_f}{\sigma'_0} \right)}$$

$$= \frac{1.052 - 0.932}{\log \left(\frac{430}{207} \right)} = 0.377$$

a) Co-efficient of compressibility:-

$$\alpha_v = \frac{C_0 - C_f}{T_f - T_0}$$
$$= \frac{1.052 - 0.932}{420 - 207}$$

$$\alpha_v = 5.470 \times 10^{-4} \text{ m/K}.$$

b) Co-efficient of Volume compressibility:

$$\beta_v = \frac{\alpha_v}{1 + C_0}$$
$$= \frac{5.470 \times 10^{-4}}{1 + 1.052}$$
$$= 2.66 \times 10^{-4}$$

→ ultimate settlement (or) final settlement (S_f) (or)
change in thickness (ΔH)

a) When change in void ratio. S_f (or) ΔH :-
from Eq. (8).

$$\frac{\Delta H}{H_0} = \frac{\Delta e}{1+e_0}$$

$$\therefore \boxed{\Delta H = H_0 \left(\frac{\Delta e}{1+e_0} \right)}$$

ΔH (or) S_f = final settlement.

H_0 = initial thickness (or) initial height.

Δe = change in void ratio.

$$= e_0 - e_f$$

$e_0 \rightarrow$ initial void ratio

$e_f \rightarrow$ final void ratio.

Co-efficient of Volume Compressibility (M_v) :-

If know S_f (or) ΔH .

from Eq. (4)

$$M_v = \frac{\Delta H}{H_0 \cdot \Delta \sigma}$$

$M_v \rightarrow$ Co-efficient of Volume compressibility

$H_0 \rightarrow$ initial thickness (or) height.

$\Delta \sigma \rightarrow$ change in stress.

$$\boxed{\Delta H \text{ (or) } S_f = M_v \cdot H_0 \cdot \Delta \sigma}$$

Co-efficient of compression Index (C_c):

$$C_c = \frac{\Delta e}{\log\left(\frac{\sigma_f}{\sigma_0}\right)}$$

$$\Delta e = C_c \cdot \log\left(\frac{\sigma_f}{\sigma_0}\right)$$

$$\Delta H = H_0 \cdot \frac{\Delta e}{1 + C_c}$$

$$\Delta H = \frac{H_0 \cdot C_c \cdot \log\left(\frac{\sigma_f}{\sigma_0}\right)}{1 + C_c}$$

$$\boxed{\sigma_f = \sigma_0 + \Delta \sigma}$$

$\sigma_0 \rightarrow$ Initial effective stress at the middle of the clay layer

$\Delta \sigma_f \Rightarrow$ Increase in stress due to applied loads at middle clay layer.

$C_c \rightarrow$ Co-efficient of compressibility Index.

→ The change in void ratio due to increase in effective pressure is 0.1 the initial void ratio is 0.4 the thickness of the soil strata is 1m. then find consolidation settlement in cm.

Sol: change in void ratio (Δe) = 0.1

Initial void ratio (e_0) = 0.4

the thickness of soil strata = $H = 1\text{m}$,

$$\Delta H = H_0 \left(\frac{\Delta e}{1 + e_0} \right)$$

if

$$= 1 \left(\frac{0.1}{1 + 0.4} \right)$$

$$= 0.5 \times 100$$

$$= \frac{5}{10} \times 100$$

$$= 50\text{cm}$$

→ The clay layer of thickness 10cm & initial void ratio is 0.5 & final void ratio is 0.2 find the ultimate settlement of layer.

Sol: layer of thickness $H_0 = 10\text{cm}$

Initial void ratio: (e_0) = 0.5

final " " (e_f) = 0.2

ultimate settlement layer?

$$\Delta H(m) \cdot S_f = H_0 \left(\frac{\Delta e}{1+e_0} \right)$$

$$= 10 \cdot \left(\frac{0.5 - 0.2}{1 + 0.5} \right)$$

$$= 10 \times \left(\frac{0.3}{1.5} \right)$$

$$\frac{\Delta H}{cm} = 2 cm$$

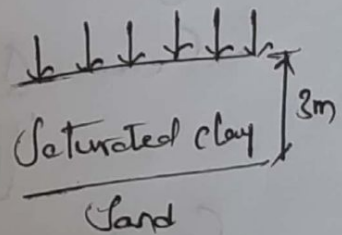
$$S_f.$$

→ A clay of layer of thickness 3m, (m_v) Co-efficient of Volume compressibility $5 \times 10^{-4} m/kN$. If sand is fill of unit weight $20 kN/m^3$. & 2m depth is dumped on clay layer. Then find the ultimate settlement of clay layer. is — m

Sol: $\gamma = 20 kN/m^3$

$$H_0 = 3$$

$$m_v = 5 \times 10^{-4}$$



$$\Delta H(m) S_f = H_0 \cdot m_v \cdot \Delta \sigma \Rightarrow 3 \times 5 \times 10^{-4} \times 70$$

$$\Rightarrow 0.105 m. = 60 mm$$

$$\Delta \sigma' = \gamma h$$

$$= 20 \times 2.5$$

$$\Delta \sigma = 70.$$

A saturated soil specimen as compression index of 0.28
thickness 6m, its void ratio at stress of 12 kN/m².
E_v 2.05 then compute.

- a) change in void ratio if stress increased to 21.6 kN/m²
b) final settlement.

sol: Compression index (C_c) = 0.28

thickness (H) = 6m

void ratio at stress of = 12 kN/m² is 2.05

- a) change in void ratio if stress increased 21.6 kN/m².

$$C_c = \frac{\Delta e}{\log\left(\frac{\sigma_f}{\sigma_0}\right)}$$

$$C_c = \log\left(\frac{\sigma_f}{\sigma_0}\right) = \Delta e$$

$$0.28 \times \log\left(\frac{21}{12}\right) = \Delta e$$

$$\Delta e = 0.07$$

$$\Delta e = e_0 - e_f \Rightarrow 0.07 = 2.05 - e_f \Rightarrow e_f = 2.05 - 0.07$$

$$\boxed{e_f = 2.01}$$

- b) final settlement

$$\Delta H = \frac{H_0 \cdot C_c \log\left(\frac{\sigma_f}{\sigma_0}\right)}{1 + e_0}$$

$$= \frac{6 \times 0.28 \times \log\left(\frac{21.6}{12}\right)}{1 + 2.05} \Rightarrow 0.15 \text{ m}$$

Co-efficient of consolidation: (C_v):-

↳ function of permeability & Volume Compressibility

$$C_v = \frac{k}{m_v \cdot \gamma_w}$$

Unit: - m/sec

k → permeability m/sec

m_v → Co-efficient of Volume Compressibility.

$$m_v = \frac{\Delta v}{v_0 \Delta \sigma} ; \frac{\Delta u}{u_0 \Delta \sigma} ; \frac{a}{(1+e) \Delta \sigma}$$

γ_w → unit weight of water.

$$\gamma_w = 10 \text{ kN/m}^3$$

$$= \frac{k}{m_v \cdot \gamma_w} = \frac{\text{m/sec}}{\frac{\text{m}^3}{\text{kN}} \times \frac{\text{kN}}{\text{m}^3}} = \frac{\text{m}^2}{\text{sec}}$$

→ Co-efficient of permeability in m/sec if co-efficient of consolidation & volume compressibility are $4.8 \text{ mm}^2/\text{min}$ & $1.02 \times 10^{-3} \text{ m}^2/\text{kN}$.

Co-efficient of consolidation, $C_v = 4.8 \text{ mm}^2/\text{min}$

Volume of compressibility (m_v) = $1.02 \times 10^{-3} \text{ m}^2/\text{kN}$

unit weight (γ_w) = 10 kN/m^3

permeability (k) = ? m/sec

$$C_v = \frac{k}{m_v \cdot \gamma_w}$$

$$k = C_v \cdot m_v \cdot \gamma_w$$

$$= \frac{4.8}{60} \times 1.02 \times 10^{-3} \times 10$$

$$\frac{\text{mm}^2}{\text{sec}} \times \frac{\text{m}^2}{\text{kN}} \times \frac{\text{kN}}{\text{m}^3}$$

$$\frac{\text{mm}^2}{\text{sec}} \times \frac{1}{\text{m}} \times \frac{1}{1000 (\text{mm})}$$

$$\frac{4.8}{60} \times 1.02 \times 10^{-3} \times 10 \times \frac{1}{10^3} \Rightarrow \frac{4.8}{60} \times 1.02 \times 10^{-3} \times 10 \times 10^{-3}$$

$$\Rightarrow 8.16 \times 10^{-7} \text{ m/sec}$$

$$8.16 \times 10^{-7} \times 10^{-3} \text{ m/sec.}$$

↳ Consolidation of undisturbed specimen :-

Based on history of loading, soil deposits are divided into 3 stages:

a) pre consolidated (or) pre compressed (or) over consolidated

↳ If a soil has ever been subjected to a pressure in excess of its present over burden, it is said to be over consolidated.

(or):

$$\sigma_{\text{present}} < \sigma_{\text{past}}$$

↳ if the applied present effective stress is less than past applied effective stress is called pre consolidation, (or) over consolidated clays.

b) Normally Consolidated clay → (N.C.C).

↳ if the present applied effective stress is equal to past applied effective stress is called normally consolidated clay.

c) Under Consolidated clays (U.C.C) :-

↳ if the present applied effective stress is greater than past applied effective stress is called under consolidated clay.

↳ Over Consolidated ratio. (OCR): :-

$$OCR = \frac{\sigma'_c}{\sigma'_p} = \frac{\text{maximum applied } \sigma' \text{ in past}}{\text{Maximum applied } \sigma' \text{ at present.}}$$

σ'_c = the maximum pressure to which an o.c.c had been subjected (consolidated) in the past pre consolidation stress.

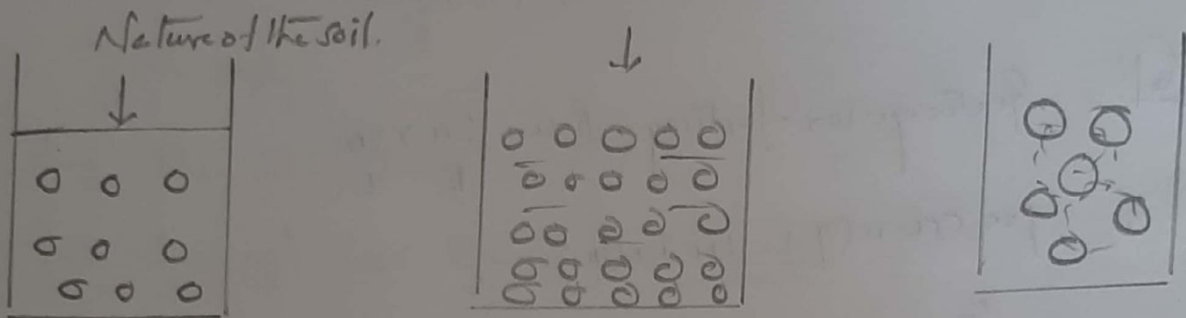
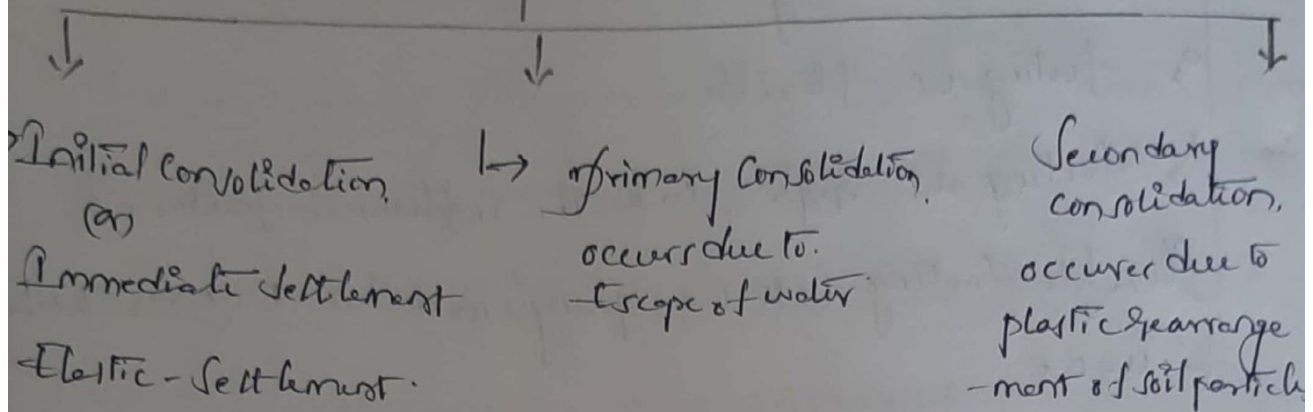
σ'_p = the present existing pressure on the soil.

for o.c.c $\rightarrow OCR > 1$;

N.C.C $\rightarrow OCR = 1$;

U.C.C $\rightarrow OCR < 1$;

Stages in consolidation.



Initial/Immediate Settlement:

→ which occurs due to elastic nature of the soil.

$$S_e = \frac{q}{E} \cdot B \cdot I (1 - \mu^2) \quad \text{units: m.}$$

→ All highly permeable soil undergoes immediate settlement
ex: sand

→ q → Constant pressure per unit area KN/m^2

I of rigid footing = $1.8 \times I$ of flexible footing.

E → young's modulus $\frac{\text{KN}}{\text{m}^2}$

B → least dimension of area (m).

μ → poisson's ratio.

I → Influence factor.

→ A rectangular footing of size $2\text{m} \times 3\text{m}$ extends a pressure of 100 kN/m^2 . Determine the immediate settlement assuming -

9 footing is flexible -

↳ footing is rigid take the influence factor of flexible footing is 1.2-6 if young's modulus $E = 5 \times 10^4 \text{ kN/m}^2$
 $\mu = 0.5$

Q.1: Rectangular footing size = 2m x 3m.
B. L.

pressure (p) = 100 kN/m^2

$$S_I = 9$$

$$E = 5 \times 10^4 \text{ kN/m}^2 \quad \mu = 0.5$$

9) footing flexible.

$$S_1 = \frac{q}{E} \times I \times B \times (1 - \mu^2)$$

$$= \frac{600}{5 \times 10^4} \times 2 \times 1.36 (1 - (0.5)^2)$$

$$r_2 = 4.07 \times 10^3 \text{ m}$$

Footing right:

$$G_1 = \frac{100}{5 \times 10^4} \times 2 \times 1.36 \times 1.8 (1 - 0.5)^2$$

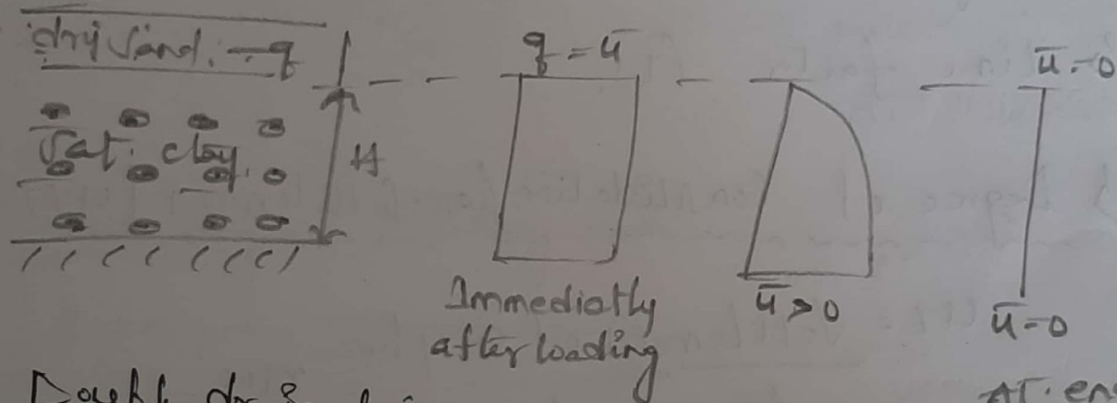
$$f_1 = 7.94 \times 10^5 \text{ m.}$$

Terzaghi - 1-Dimensional Consolidation theory

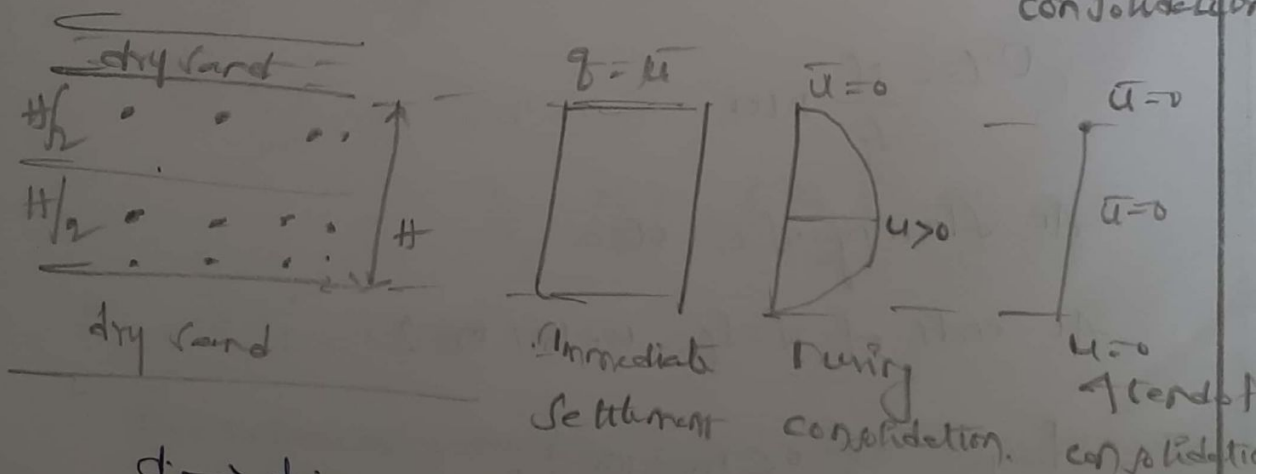
Assumption:

- ↳ The soil is homogeneous & isotropic.
- ↳ The consolidation only in 1-Dimension it means the escape of the water only in 1-Dimension (vertical).
- ↳ There is no change in area. Volume change due to only depth only.
- ↳ The soil is saturated.
- ↳ Darcy's law Equation. $[k \cdot A = Q]$

Single drained:



Double drained:



- $d \rightarrow$ drainage path.
- $d \rightarrow$ single drained.
- $d \rightarrow H/2$ for double drained.

Terzaghi - 1-Dimensional Consolidation Eq:

$$\boxed{\frac{\partial u}{\partial t} = C_v \cdot \frac{\partial^2 u}{\partial z^2}}$$

$\frac{\partial u}{\partial t} \rightarrow$ Rate of change of pore water pressure with respect to time

$\frac{\partial^2 u}{\partial z^2} \rightarrow$ Rate of change of pore water pressure with respect to depth.

$C_v \rightarrow$ Co-efficient of Consolidation, $C_v = \frac{k}{m_v \cdot \gamma_w}$

The solution of for above eq' give in form of

- 1) Degree of consolidation for settlement (U%)
- 2) Time factor (Tv).

1) Degree of consolidation for settlement (U%) :-

$$U\% = \frac{\text{Settlement of any time}}{\text{final settlement}(S_f)} \times 100$$

$$U\% = \frac{S}{S_f} \times 100$$

At starting $S=0$, $U=0$.

At ends of $S=S_f$, $U=100\%$ or 1.

Range, $0 \leq U \leq 100\%$ or 1.

↳ It is the function of ultimate consolidation, which is completed at any stage of time during consolidation

↳ It is defined only for 1^o consolidation process.

↳ At the beginning ($t=0$) %U is 0

↳ At $t=\infty$ at the end of the primary consolidation, %U is 100%

2) Time factor (T_v):

↳ It is the parameter which relates to the degree of consolidation & time required for that consolidation

$$T_v = c_v \cdot \frac{T}{d^2}$$
$$c_v = \frac{k}{m_v \cdot \gamma_w}$$

d → length of drainage path

2-way drainage path. $d_2 = \frac{H_0}{2}$

1-way drainage path $d_1 = H_0$

$$T_v = c_v \cdot \frac{t}{d^2} \Rightarrow T_v \cdot d^2 = c_v \cdot t$$

$$\frac{t_2}{t_1} = \left(\frac{d_2}{d_1} \right)^2 \Rightarrow \left(\frac{H_1/2}{H_1} \right)^2 \Rightarrow \frac{t_2}{t_1} = \frac{1}{4}$$

$$\Rightarrow t_2 = t_1 \times \frac{1}{4}$$

Time taken under double drained = $\frac{1}{4}$ × Time taken under single drained

→ The time required for consolidation with double drainage estimate as 8 yr. All other remaining conditions are same. Estimate the time required for single drained.

(i). Time req. for double drained $t_2 = 8$.

$$t_2 = \frac{1}{4} \times t_1$$

$$t_1 = t_2 \times 4$$

$$t_1 = 8 \times 4$$

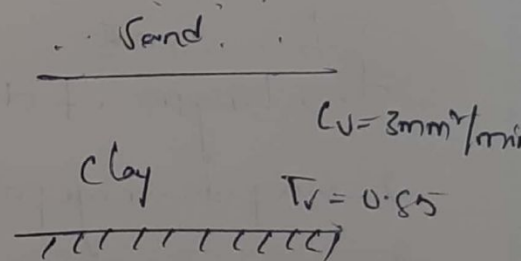
$$t_1 = 32 \text{ yr}$$

→ A 3m thick clay layer is subjected to an initial pore water pressure of 145 kN/m^2 as shown in fig. given ground condition find the time req. for 90% consolidation.

$$C_v = 3 \text{ mm}^2/\text{min}$$

$$T_v = 0.85$$

$$\text{for } H = 3 \text{ m} \Rightarrow 3 \times 10^3 \text{ mm}$$



$$T_v = \frac{C_v \cdot t}{d^2} \Rightarrow t = \frac{T_v \cdot d^2}{C_v}$$

$$t = \frac{0.85 \times (3 \times 10^3)^2}{3}$$

$$= 2.55 \times 10^6 \text{ min}$$

$$= \frac{2.55 \times 10^6}{24 \times 60}$$

$$t = 1771 \text{ days}$$

$$\left\{ \begin{array}{l} 1 \text{ day} = 24 \times 60 \text{ min} \\ \frac{1}{24 \times 60 \text{ min}} \end{array} \right.$$

Relationship between Time factor. (T_v) & degree of consolidation (U%).

$$T_v = \frac{\pi}{4} \left(\frac{U\%}{100} \right)^2$$

↳ A saturated clay layer 5m thickness takes 1.5yr. for 50% consolidation, when drained both sides if co-eff of volume compressibility is $1.5 \times 10^{-3} \text{ m}^2/\text{kN}$. Then find the co-eff of permeability.

Thickness (d) or $H = 5\text{m} = 5/2 = 2.5\text{m}$.

$T = 1.5\text{yr}$

The co-eff of volume compressibility. $\alpha_v = m_v = 1.5 \times 10^{-3} \text{ m}^2/\text{kN}$.

U% = 50%.

find co-eff of permeability k .

$$C_v = \frac{k}{m_v \gamma_w} \quad \text{--- (1)}$$

but

$$T_v = \frac{C_v \cdot T}{d^2} \quad \text{--- (2)}$$

We know that:

$$T_v = \frac{\pi}{4} \left(\frac{U\%}{100} \right)^2 \quad \text{--- (3)}$$

$$= \frac{\pi}{4} \left(\frac{50}{100} \right)^2 \Rightarrow \frac{\pi}{4} \left(\frac{50}{100} \right)^2$$

$$\Rightarrow 0.196$$

$$T_v = \frac{C_v \cdot t}{t} \Rightarrow C_v = \frac{T_v \cdot dr}{t}$$

$$= \frac{0.196 \times (1.5)^2}{1.5}$$

$$C_v = 0.826$$

from: 1.

$$k = C_v \times m_r \times \omega$$

$$= 0.826 \times 1.5 \times 10^{-3} \times 10$$

$$k = 0.0122 \text{ m/yr}$$

→ Isochrone :-

↳ the graph which represents the variation of hydrodynamic pore water pressure with respect to depth is called 'Isochrone'

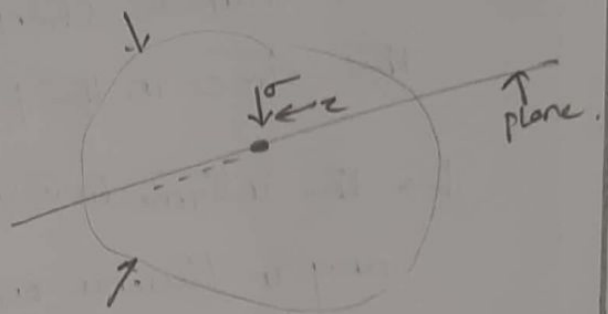
Shear Strength : UNIT-5:

→ The shear strength of soil is constituted by.

- a) Structural resistance due to interlocking
- b) frictional resistance
- c) cohesion.

σ = Normal stress

τ = shear stress



3 → principal planes on which ($\tau=0$).

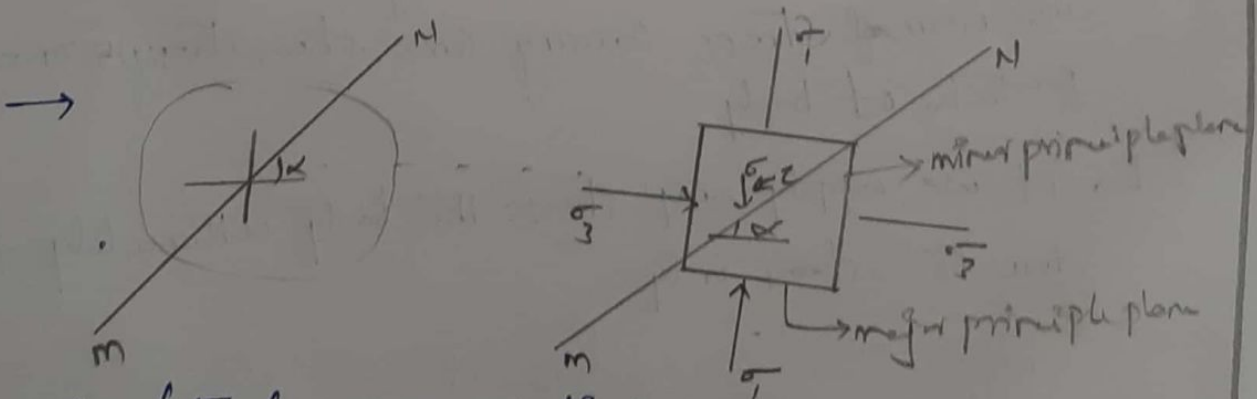
3 → principal stress ($\sigma_1 : \sigma_2 : \sigma_3$)

Generally

σ_1 = Major principal stress. ($\sigma_1 > \sigma_2 > \sigma_3$)

σ_2 = Intermediate , , (but always not correct)

σ_3 = Minor , ,



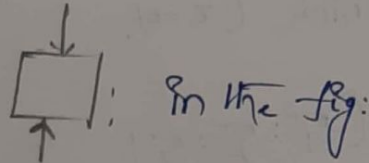
Analytical method to find (σ & τ): -

$$\sigma = \frac{\sigma_1 + \sigma_3}{2} + \frac{\sigma_1 - \sigma_3}{2} \cos 2\alpha ; \tau = \frac{\sigma_1 - \sigma_3}{2} \sin 2\alpha$$

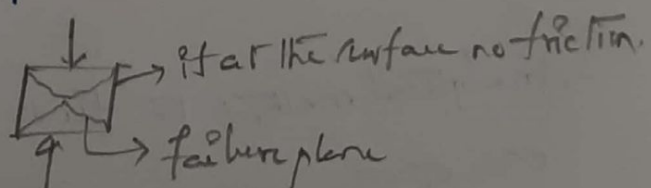
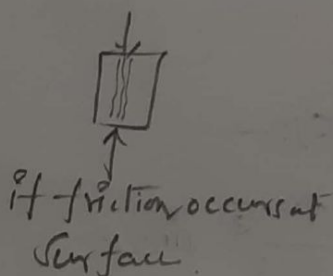
Mohr's theory:

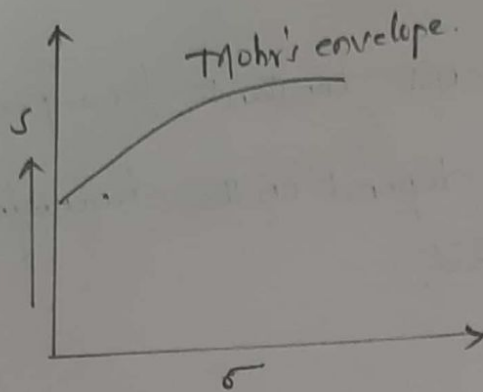
- The material essentially fails due to shear stress.
- The critical shear stress causing failure depends upon the properties of the material as well as normal stress on the failure plane.
- The ultimate strength of the material is determined by the stress in the potential failure plane.
- The intermediate (σ_2) principal stress does not have any influence on the strength of the material.

Note:



- We are applying the normal stress. It fails. but it is not the normal stress causing the any stress failure (flexural, twisting etc).
- It is the shear stress causing the failure i.e. this normal stress causing some shear stress on each particle of body.
- If we apply any stress: the body ultimately fails due to shear only.





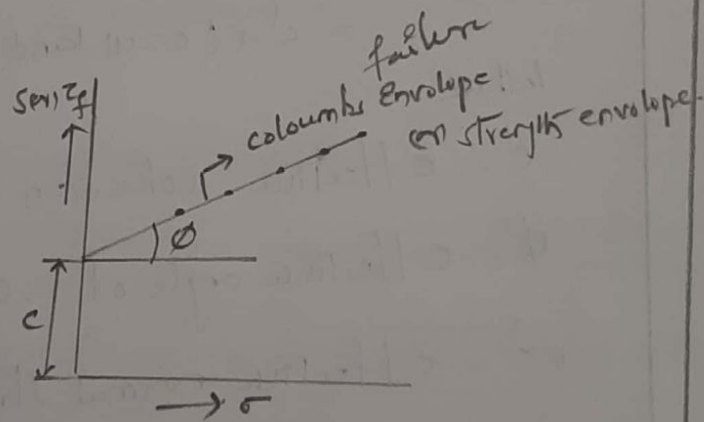
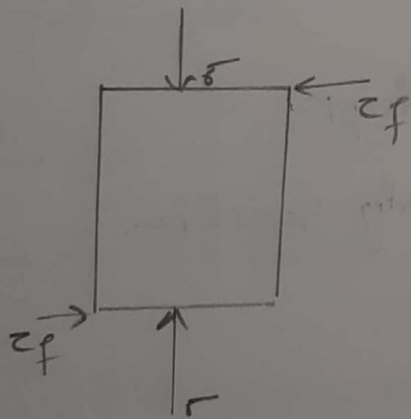
$\tau = f(\sigma)$. \rightarrow Shear strength is function of normal stress.

τ is a function of normal stress.

σ_2' have no effect on behaviour of soil.

$$\boxed{\tau = f(\sigma)}$$

Coulomb's law:-



$$\tau = c + \sigma \tan \phi$$

where: c & ϕ are empirical constants.

$\tau \rightarrow$ shear strength $\rightarrow \text{KN/m}^2$.

$c \rightarrow$ Cohesion $\rightarrow \text{KN/m}^2$.

$\phi \rightarrow$ slope of failure envelope or Angle of internal friction or Angle of shearing resistance.

Note:

- ↳ c' & ϕ are not constant for a particular soil.
- ↳ In fact they depend on the drainage conditions & test conducted.

Terzaghi's Concept: (the effective stress principle):

- ↳ the effective normal stress control the shearing resistance of soil.

Revised Mohr-Coulomb equation:

$$\begin{aligned} S &= c' + \sigma' \tan \phi \\ &= c' + (\sigma - u) \tan \phi. \end{aligned}$$

Where:

c' = effective cohesion intercept.

ϕ' = effective angle of shearing resistance.

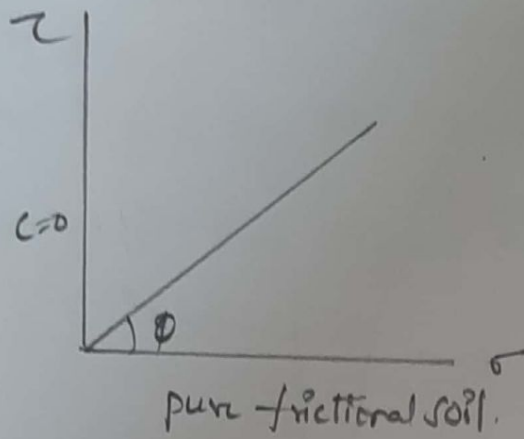
σ' = effective normal stress.

σ = Total normal stress.

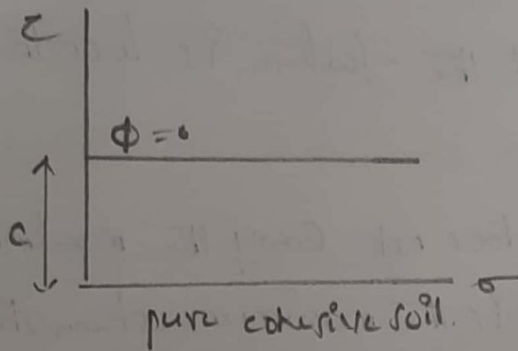
for any combination of applied principle effective stress σ_1' , σ_3' , failure will occur

only if the stress circle touches the failure envelope.

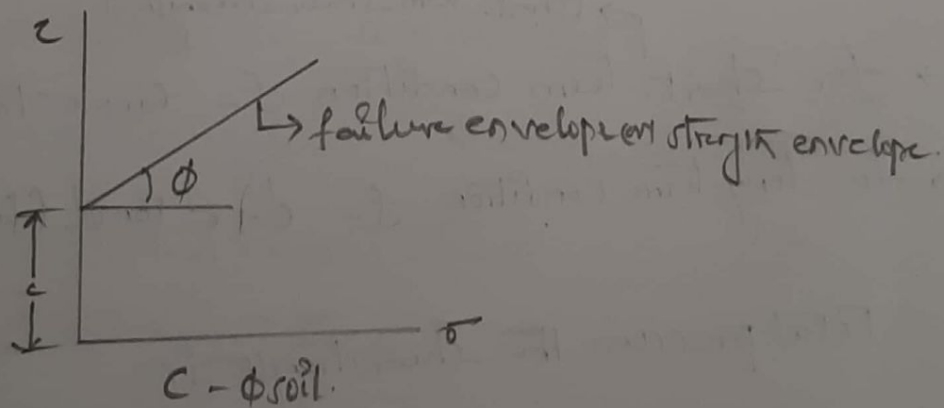
β = angle of obliquity.



Eg: dry sand ~~or~~ Granular soil.
 $c=0$
 cohesionless soil.



Ex: plastic clay.



ex: 1) clayey sand
 2) clayey gravel.

failure envelope:

→ locus of point - having combination of critical stress.

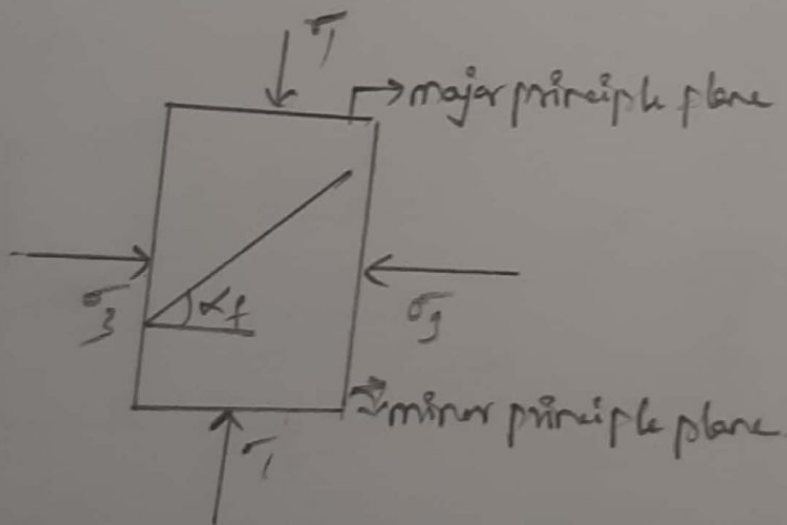
failure plane:

→ plane at which the material fails.

$$\text{Here: } 90 - \phi = 180 - 2\alpha_f$$

$$\Rightarrow \alpha_f = 45 + \phi/2$$

* failure plane always makes an angle of $45 + \phi/2$ w.r.to. major principal plane.



$\tau < s \rightarrow \text{Safe}$

$\tau \leq s \rightarrow \text{Critical condition}$

$\tau > s \rightarrow \text{failure}$

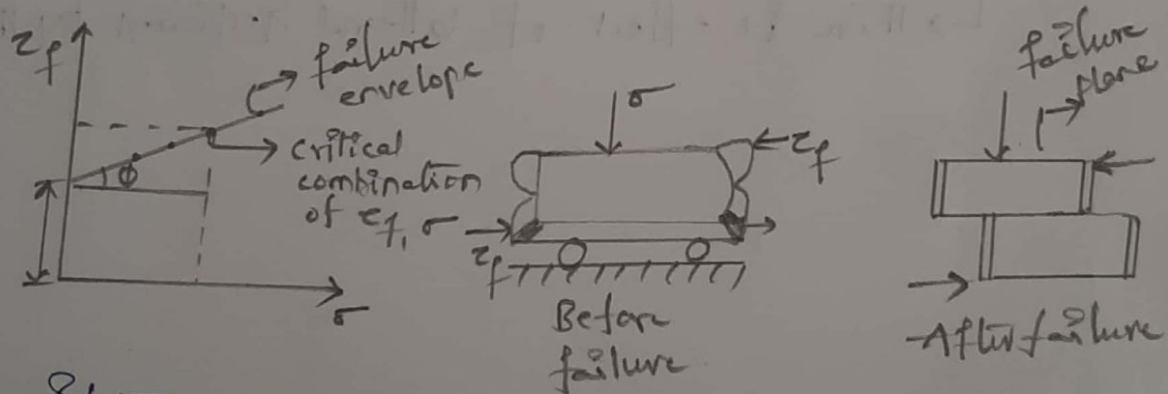
Laboratory test for strength parameters:

- ↳ Box-shear test / Direct shear test.
- ↳ Tri-axial shear test
- ↳ unconfined compression test.
- ↳ Vane shear test.

* Box-shear test / Direct shear test:

↳ Soil specimen of size $60 \times 60 \times 25 \text{ mm}$ is used generally.

↳ It is suitable for cohesionless soil as drained test.



↳ If the condition is drained (i.e., drained holes are open) use c', ϕ'

↳ If the condition is undrained (i.e., drained hole is plugged) use c_u, ϕ_u .

usually $c' \neq c_u$ & $\phi' \neq \phi_u$.

According to Coulomb's theory $\tau_{\text{failure}} = c + \sigma \cdot \tan \phi$

Demerits: ÷

↳ The stress distribution across the soil sample is very complex.

↳ As the test progresses the area under shear gradually decrease.

↳ The orientation of failure plane is fixed (horizontal). The plane may not be the weakest one.

↳ Little control on drainage of soil.

↳ Consequently only drained test can be conducted on highly permeable soil.

↳ Measurement of pore pressure is not possible

↳ There is effect of lateral restraint by the video

A direct shear stress are conducted on cohesionless soil specimen under a Normal stress of 200 kN/m^2 . The specimen of will failed at shear stress of 100 kN/m^2 . then find the angle of internal friction in Degrees?

Sol:

$$\text{Normal Stress } (\sigma) = 200 \text{ kN/m}^2$$

$$\tau = 100$$

$$\phi = ?$$

$$\tau = c + \sigma \cdot \tan \phi$$

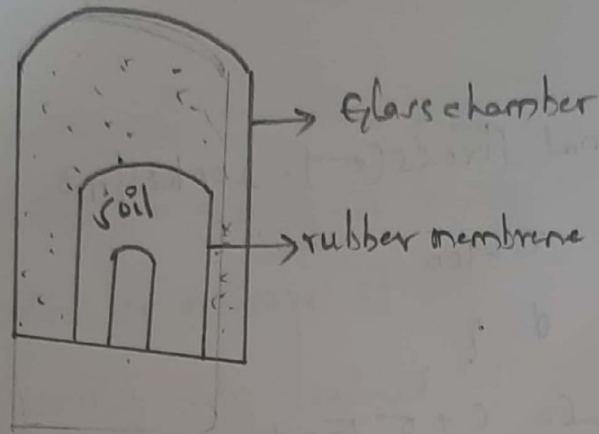
$$100 = 0 + 200 \tan \phi$$

$$\frac{100}{200} = \tan \phi$$

$$\phi = 26.56^\circ$$

Tri-axial shear strength test:-

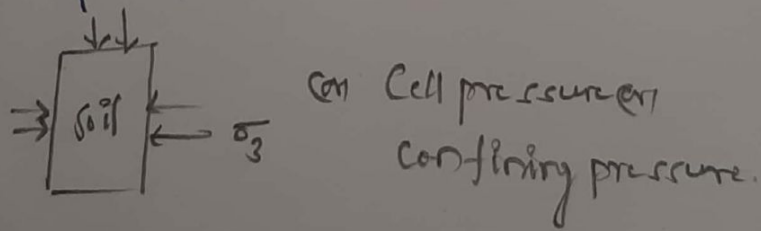
→ Take a cylindrical saturated soil sample of height
= 2 x dia of the sample.



Stage 1:

→ All around the soil the confining pressure or cell pressure (σ_3) is applied using external water pressure.

→ when expulsion of pore water is stop the first stage is stage completed.

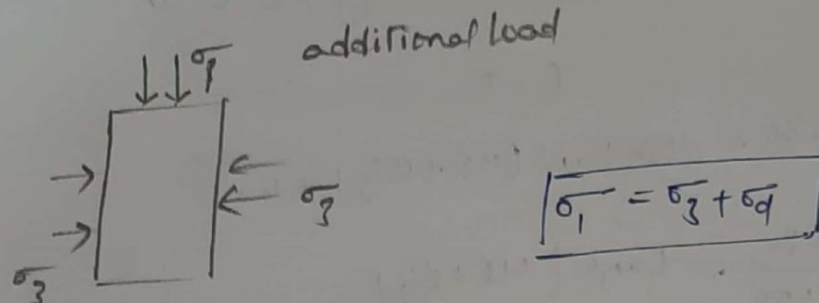


Stage 2:

→ the confining pressure (σ_3) is kept constant & additional axial stress is applied is called as

~~Direction~~ stress (σ_1)
Deviator.

→ The ^{deviator} ~~deviator~~ stress increase gradually and till soil specimen is failure.



$\sigma_d \rightarrow$ Deviator stress.

The tri-axial strength is based on Mohr's theory

$$\sigma_1 = \sigma_3 \tan^2 \alpha + 2c \tan \alpha$$

$$\alpha = 45 + \phi/2$$

$$\sigma_1 = \sigma_3 \tan^2 (45 + \phi/2) + 2c \tan (45 + \phi/2)$$

$$\sigma_1' = \sigma_3' \tan^2 (45 + \phi/2) + 2c \tan (45 + \phi/2) \rightarrow \text{According to Terzaghi}$$

A triaxial test was conducted on granular soil under drained condition. The soil sample failed when the effective minor principle stress was 150 kN/m^2 and principle effective stress ratio was 4.2. Then find ϕ value & Direct stress at failure.

→ effective minor principle stress $(\sigma_3') = 150 \text{ kN/m}^2$

principle effective stress $\frac{\sigma_1'}{\sigma_3'} = 4.2$

$$\phi = 9$$

$$\sigma_1' = 4.2 \times 150 = 630 \text{ kN/m}^2$$

$$\sigma_1 = \sigma_3 + \sigma_d$$

According to Mohr's theory.

$$\sigma_1' = \sigma_3' \tan^2(45 + \phi/2) + 2c \tan(45 + \phi/2)$$

$$c = 0$$

$$630 = 150 \tan^2(45 + \phi/2) + 0$$

$$\frac{630}{150} = \tan^2(45 + \phi/2)$$

$$\tan^2(45 + \phi/2) = 4.2$$

∴ b. u. side:

$$\tan(45 + \phi/2) = \sqrt{4.2}$$

$$\tan(\sqrt{4.2}) = 45 + \phi/2$$

$$\phi/2 = 63.98 - 45$$

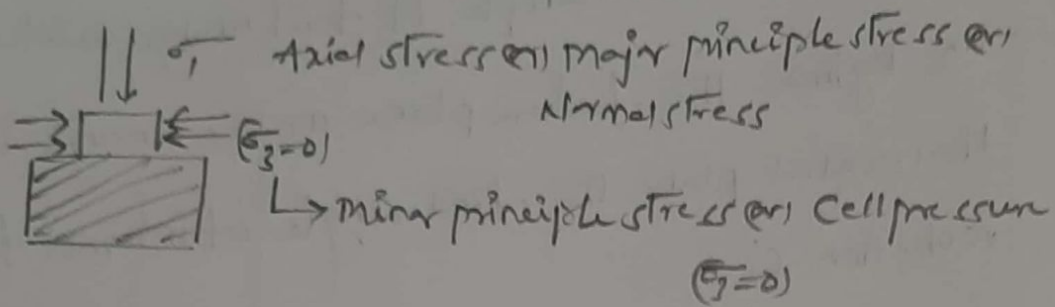
$$\phi = 37.97$$

$$\therefore \sigma_1 = \sigma_3 + \sigma_d$$

$$\sigma_d = 630 - 150$$

$$\boxed{\sigma_d = 480 \text{ kN/m}^2}$$

Un confined compressive strength test:-



$$\sigma_1 = \sigma_3 + \tan^2 \alpha + 2c \tan \alpha$$

* \rightarrow The cylindrical soil sample is subjected only major principal stress or Normal or axial load (σ i.e. axial).

* The cell pressure or minor pressure is $\sigma_2 = 0$.

$$\sigma_1 = \sigma_3 \tan^2 \alpha + 2c \tan \alpha$$

$$= 2c \tan \alpha$$

$$= 2c \tan (45^\circ + \phi/2)$$

If soil is clay ($\phi = 0$)

$$\sigma_1 = 2c \tan (45^\circ + \phi/2)$$

$$\sigma_1 = 2c$$

\rightarrow It is special form of tri-axial test in which the confining pressure is zero. It can be conducted only on clayey soil. which can withstand without coefficient. It is an undrained test.

$\sigma_1 = 2c_u \tan (45^\circ + \phi_u/2)$ here: $\sigma_1 = q_u$.
 $q_u =$ unconfined compression strength for pure clays $\phi_u = 0$, $q_u = 2c_u$
 $c_u = (q_u/2)$.

When confined compression strength is conducted on cylindrical soil sample it fail under axial stress of 1.2 kg/cm^2 . The failure plane makes an angle of 50° with horizontal plane. Find Angle of internal friction & cohesion C .

Axial stress (σ_1) = 1.2 kg/cm^2

The failure plane makes angle $\alpha = 50^\circ$

$$\sigma_1 = \sigma_3 \tan^2 \alpha + 2c \tan \alpha$$

$$\boxed{\alpha = 45 + \phi/2}$$

$$50 - 45 = \phi/2$$

$$5 = \phi/2$$

$$\boxed{\phi = 10^\circ}$$

$$\tau = 2c \tan \alpha$$

$$\frac{\sigma_1}{2 \tan \alpha} = c$$

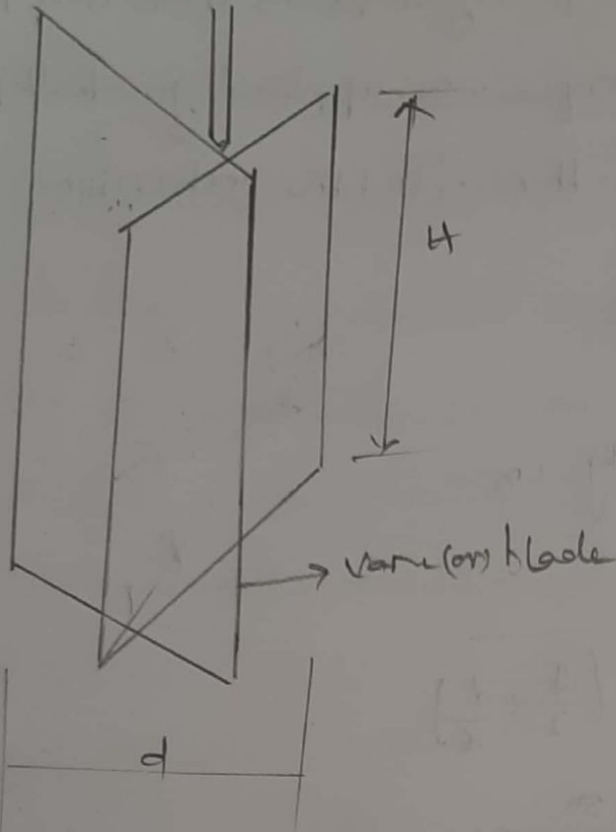
$$= \frac{1.2}{2 \times \tan(50)} = c$$

$$\boxed{c = 0.503 \text{ kg/cm}^2}$$

The $\gamma/\text{New. soil}$ cohesion C & unconfined compression strength fail

$$\gamma_u = \frac{2c_u}{\gamma_u}$$

Vane shear test:-



→ To find the shear strength of clay

$$C_u = \frac{T}{9.54 \pi \left(\frac{H}{2} + \frac{d}{6} \right)}$$

→ Quick test to determine the undrained shear strength of soft clay in the lab or field.

→ When both ends part take in shearing

C_u → undrained cohesion.

H → Height of the Vane

d → dia of the Vane

T → Torque

$C_{u(r)}$ → kn/m^2 .

The vane 10 cm ϕ height 4 cm India was pressed into the clay. The torque was applied gradually increased to 450 kg-cm. Then find the cohesion.

$$H = 10 \text{ cm}$$

$$\phi = 8 \text{ cm}$$

$$T = 450 \text{ kg-cm}$$

$$C = \frac{T}{\pi d^2 \left(\frac{H}{2} + \frac{d}{6} \right)}$$

$$C = \frac{450}{\pi \times (8)^2 \left(\frac{10}{2} + \frac{8}{6} \right)}$$

$$C = 0.353 \text{ kg-cm.}$$

-Application:

↳ for sudden drawdown causes.

C. Consolidated - Drained Test: +

↳ Drainage is permitted through out the test during the application of both normal and shear test so that full consolidation occurs and excess pore pressure is setup any stage of test. Generally takes 2 to 5 days.

Application: +

↳ cohesionless soils and for soils having high permeability

↳ for ascertaining long term stability of clays.

Sensitivity: +

↳ it can be easily determined using the unconfined compression test.

$$\text{Sensitivity} = (s_t) = \frac{q_u (\text{undisturbed})}{q_u (\text{remoulded})}$$

If Sensitivity = 1 \Rightarrow insensitive soil

If Sensitivity $> 16 \Rightarrow$ quick soil.

Depending upon the drainage condition: \leftarrow

\rightarrow There are three types:

\rightarrow 1, Unconsolidated - Undrained Test (or)
Quick Test (Q-test or) UU-test:

\rightarrow 2, Consolidated undrained test (CU-test).

\rightarrow 3, Consolidated drained test (or) slow test

* Unconsolidated - Undrained test: \leftarrow

\rightarrow No drainage is permitted either during consolidation stage or shear stage. Therefore, there is no dissipation of pore pressure during the test & test can be conducted in few minutes (5-10).

Application:

Generally done for less permeable soil such as clays for short-term stability analysis and also for earth dams during construction.

Consolidated, undrained test: \leftarrow

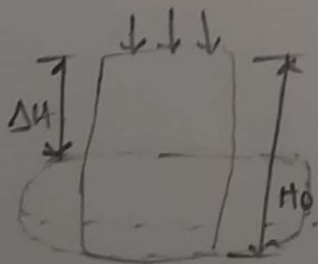
\rightarrow Drainage is permitted under the initially applied normal stress only and fully primary consolidation, or softening is allowed to take place. No drainage allowed in shear stage.

Liquefaction:

- When saturated sandy soil is subjected to earth quaker loads, the pore pressure suddenly increases and thus decreases the shear strength of soil and it may become zero also.
- The soil momentarily liquefies and behaves as dense fluid. This phenomena when sand loses its shear strength due to oscillatory motion is called liquefaction of sand.
- The soil most susceptible to liquefaction are saturated fine sand and saturated medium sand.

Dilatancy:

- The phenomenon of increase in volume of soil during the shear is called Dilatancy.



Critical Void ratio: \rightarrow

\rightarrow Critical void ratio is defined as the ratio at which there is no change in void. with an increase in strain.

\rightarrow The properties of change in volume rely upon different factor such as shape, grain size, principle stress

\rightarrow The representation of shear strain versus void ratio are shown below in the graph.

